



# *Integral Quantities Calculated from ENDF Libraries*

*B. Pritychenko\**

*National Nuclear Data Center  
Brookhaven National Laboratory*

*\*Email: [pritychenko@bnl.gov](mailto:pritychenko@bnl.gov)*

# Evaluated Reaction Libraries

---

- ❖ *ENDF/B-VII.0 (USA, 2006)*
- ❖ *JEFF-3.1 (Europe, 2005)*
- ❖ *JENDL-3.3 (Japan, 2002)*
- ❖ *ROSFOND (Russia, 2008)*
- ❖ *ENDF/B-VI.8 (USA, 2001)*

*How we can quickly validate nuclear data and select better evaluations using a few benchmarks?*

# ENDF Benchmarks

---

- ❖ Selected benchmarks (observables):  $\sigma^{\text{thermal}}$ ,  $\sigma^{14 \text{ MeV}}$ , Resonance Integrals,  $\sigma^{\text{Maxw}(30 \text{ keV})}$ ,  $\sigma^{\text{Maxw}(252\text{Cf})}$
- ❖ The reaction of interest: (n,tot), (n,el), (n,inel), (n,2n), (n,fission), (n, $\gamma$ ), (n,p), (n, $\alpha$ )
- ❖ One may compare observables for each library however good agreement makes sense only if we deal with independent evaluations
- ❖ ENDF independent evaluations: *Atlas of Neutron Resonances*, *Standards Evaluation*, KADONIS/Bao *et al.*, ROSFOND (?)

# Benchmark Calculations



No



“E

th

p

o



O



C

using process

Wolfram Mathematica

ONLINE INTEGRATOR

The world's only full-power

$$\int (s1 + ((x - E1) * (s2 - s1)) /$$

Compute Online With Math

$$\int \frac{(x - E1) (s2 - s1)}{E2 - E1} +$$

$$\frac{(s1 - s2) x^2}{2 (E1 - E2)} + s1 x -$$

Wolfram Mathematica

ONLINE INTEGRATOR

The world's only full-power integration solver

$$\int (d1 + (x - d3) ((d2 - d1) / (d4 - d3))) x \exp(-(ax) / (kT)) dx$$

Compute Online With Mathematica

HOW TO ENTER INPUT | RANDOM EXAMPLE

Traditional Form | Input Form | Output Form

$$\int \left( d1 + \frac{(d2 - d1) (x - d3)}{d4 - d3} \right) x e^{-\frac{ax}{kt}} dx =$$

$$\frac{1}{a^3 (d3 - d4)} e^{-\frac{ax}{kt}} k t (x (d1 (d4 - x) + d2 (x - d3)) a^2 +$$

$$k t (-d2 d3 + d1 d4 - 2 d1 x + 2 d2 x) a +$$

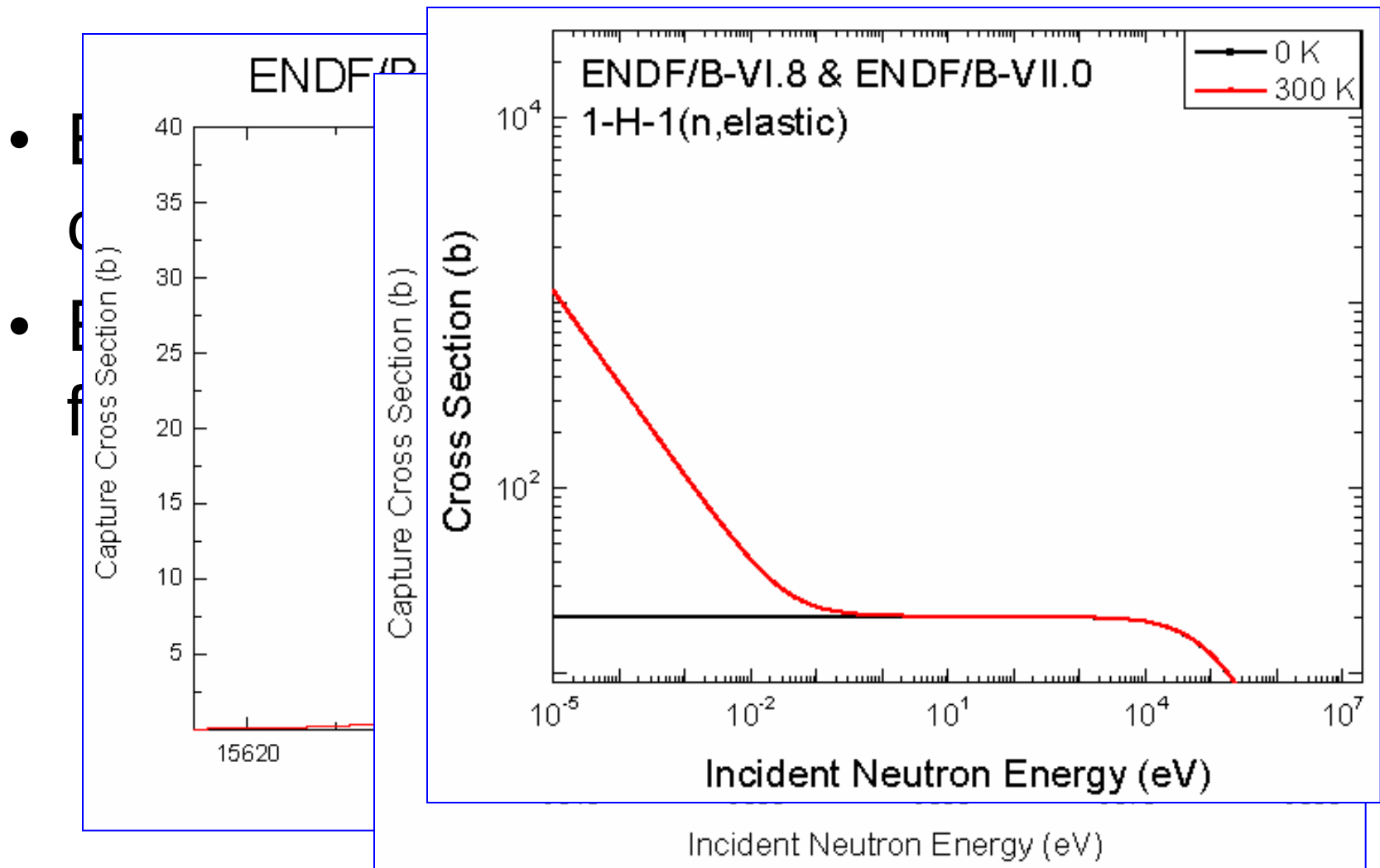
$$2 (d2 - d1) k^2 t^2)$$

Time to compute: 0.11 second

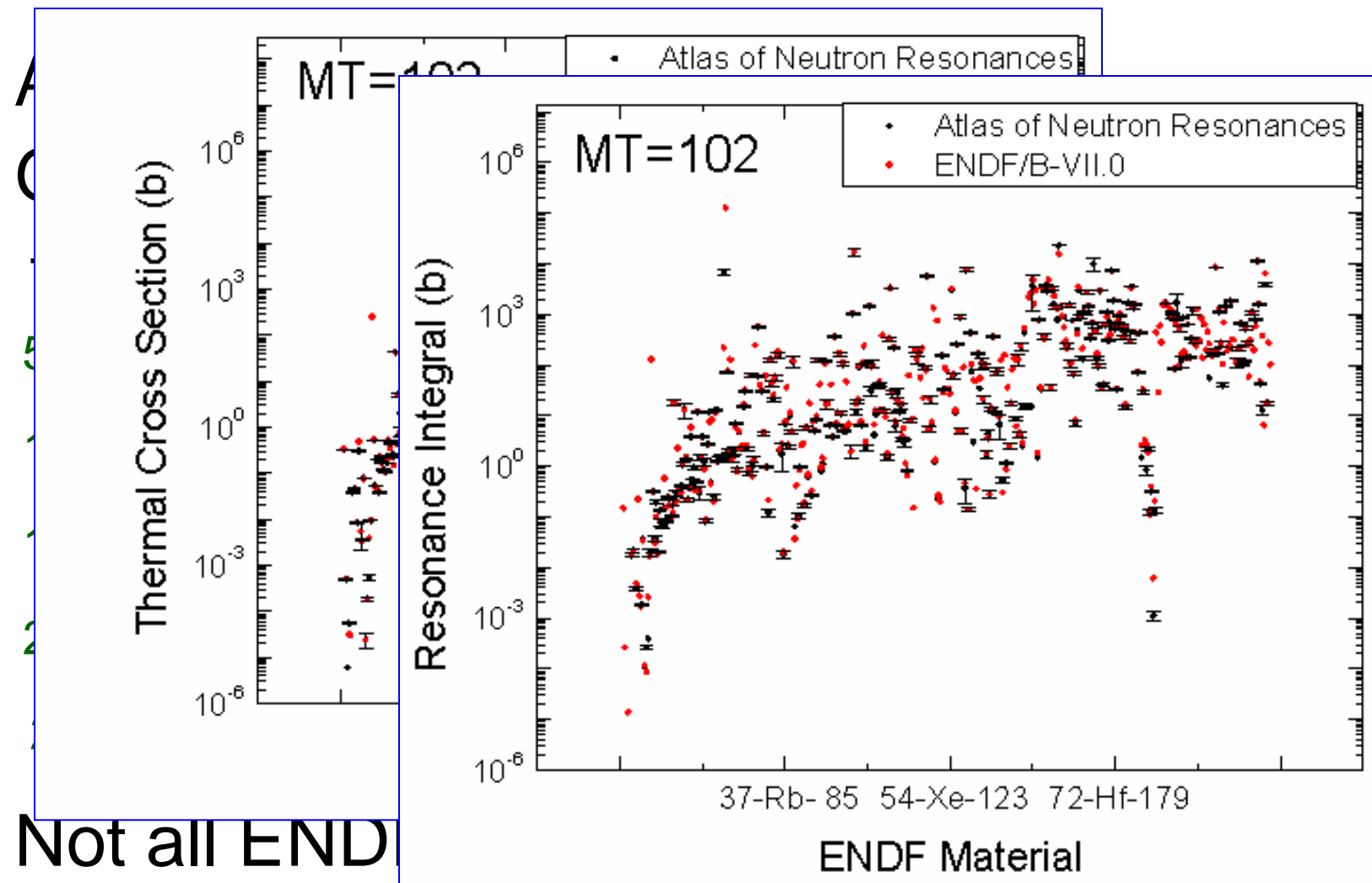
d on the fact  
ithin a

Java

# Benchmark Validation

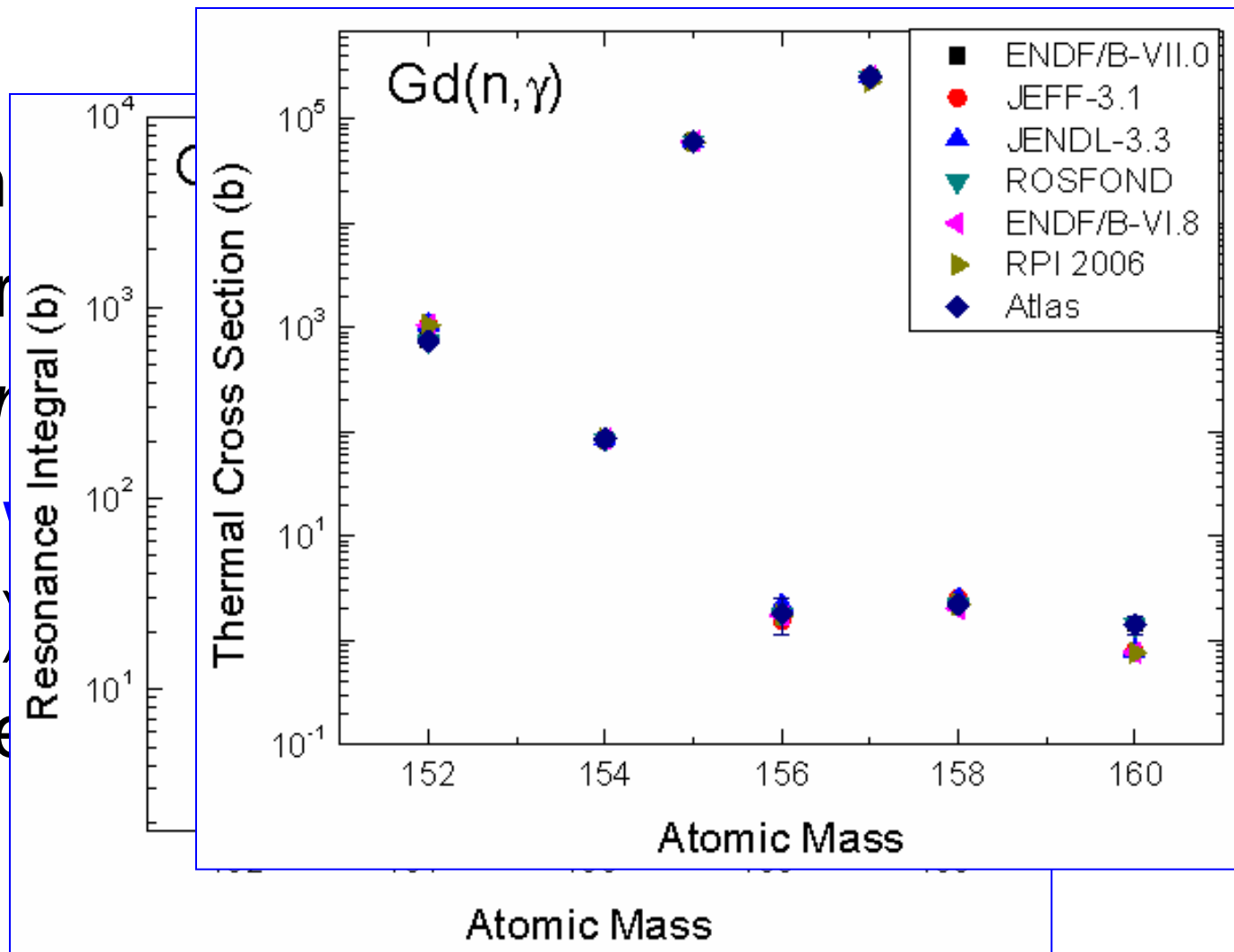


# Results



# Results

- ❖ Gadolinium
- ❖ Comparison of Neutron Data (G. Leininger (2006))
- ❖ Possible



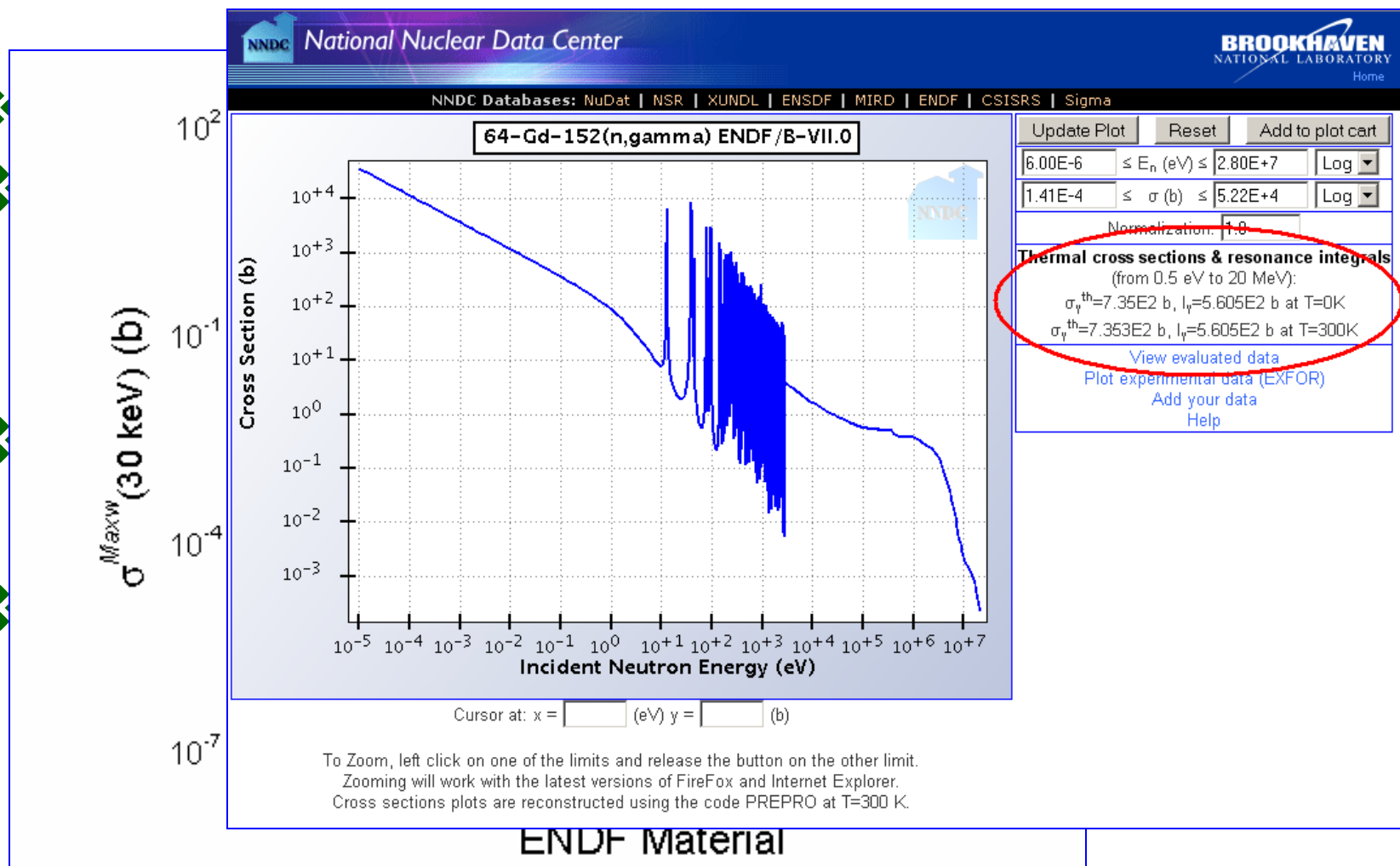
# Results

Table I. ENDF/B-VII.0 pre-calculated thermal neutron cross sections and resonance integrals (0.5 eV – 20 MeV) for elastic scattering, neutron capture and fission at  $T = 0^0$  K; corresponding values from the *standards evaluation* and *Atlas of Neutron Resonances* are shown in round and square brackets, respectively.

Material	$\sigma_{n,el}$ (b)	$I_{n,el}$ (b)	$\sigma_{n,\gamma}$ (b)	$I_{n,\gamma}$ (b)	$\sigma_{n,f}$ (b)	$I_{n,f}$ (b)
$^{233}\text{U}$	12.15116 (12.11(66)) [12.7(3)]	168.6988	45.23763 (45.56(68)) [45.5(7)]	141.0432 [138(6)]	531.2151 (531.22(133)) [529.1(12)]	775.4899 [775(17)]
$^{235}\text{U}$	15.08416 (14.087(220)) [14.02(22)]	170.07	98.68643 (99.40(72)) [98.8(8)]	140.426 [146(6)]	585.0856 (584.33(102)) [582.6(11)]	275.94 [275(5)]
$^{238}\text{U}$	9.279782 [9.075(15)]	346.8409	2.682608 (2.677(12)) [2.680(19)]	275.5847 [277(3)]	1.679455E-5 [3E-6]	2.691588 [0.00163(16)]
$^{239}\text{Pu}$	7.975233 (7.8(96)) [7.94(36)]	178.3488	270.3295 (271.5(214)) [269.3(29)]	181.3443 [180(20)]	747.4013 (750(183)) [748.1(20)]	302.5637 [303(10)]
$^{241}\text{Pu}$	11.23797 (12.13(261)) [9(1)]	175.1174	363.0489 (361.79(496)) [362.1(51)]	179.9437 [162(8)]	1011.852 (1013.96(658)) [1011.1(62)]	569.6337 [570(15)]



# Results



# Conclusion

---

- ❖ Integral quantities have been calculated for five major ENDF Libraries and eight MT numbers
- ❖ *Comparison between calculated quantities and independent benchmarks allow to identify potential problems*
- ❖ These results are analyzed and loaded into Sigma databases
- ❖ Future plans will include extension of the current project for Westcott factor calculations
- ❖ Many thanks to M. Herman, S. Mughabghab, V. Zerkin