



The Nickel Isotopes – Status of Theory - Then and Now

Alex Brown – Michigan State University

KARLSRUHER NUKLIDKARTE

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核素图, 第7版

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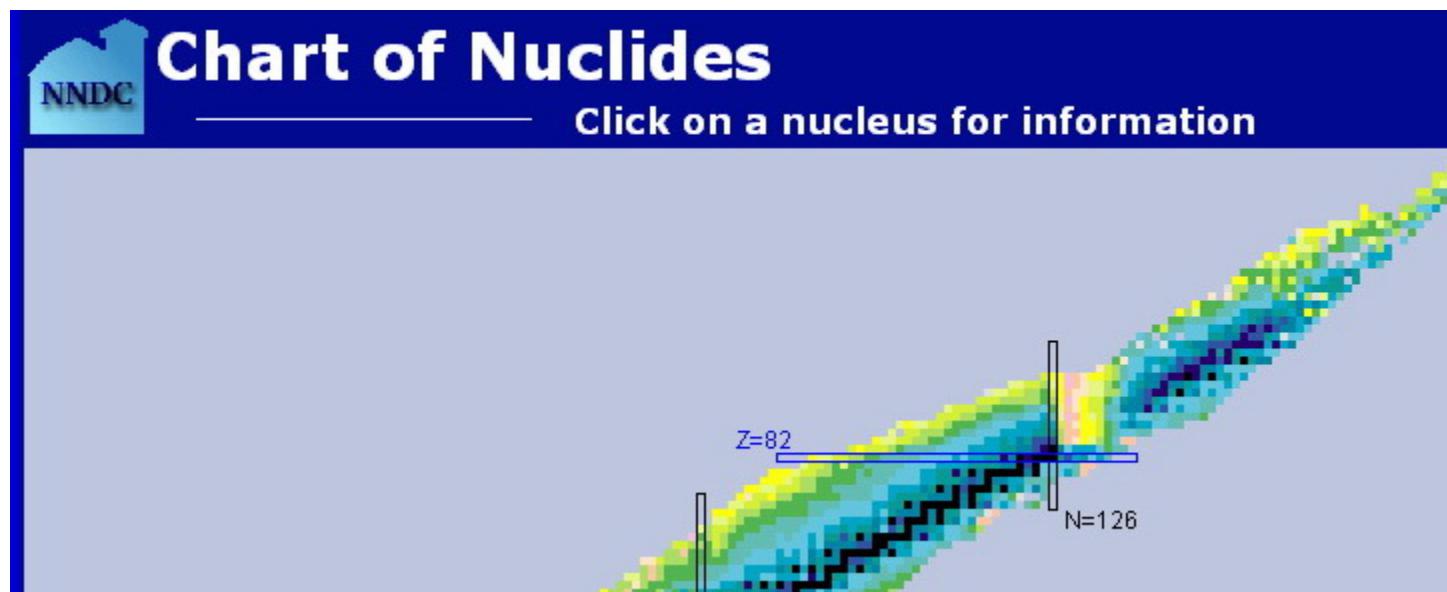
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Li 6.941 σ_{abs} 71	Li 4 5.0 MeV $91 \cdot 10^{-24}$ s $370 \cdot 10^{-24}$ s p	Li 5 1.23 MeV $370 \cdot 10^{-24}$ s p	Li 6 7.59 α 0.039 σ_{abs} 940	Li 7 92.41 α 0.045	Li 8 840.3 ms β^- 12.5 $\beta\alpha$ ~1.6	Li 9 178.3 ms β^- 13.6... $\beta\alpha$ 0.7... $\beta\alpha$	Li 10 230 keV $2.0 \cdot 10^{-21}$ s n	Li 11 8.5 ms β^- ~18.5; 20.4 γ 3368°; 320... $\beta\alpha$; β^2n ; β^3n ; $\beta\alpha$; β^2 ; βd
He 4.002602 $\sigma_{abs} < 0.05$	He 3 0.000134 α 0.00005 σ_{abs} p 5330	He 4 99.999866	He 5 648 keV $700 \cdot 10^{-24}$ s n	He 6 806.7 ms β^- 3.5 βd	He 7 159 keV $2.9 \cdot 10^{-21}$ s n	He 8 119 ms β^- 9.7... γ 981; 478° $\beta\alpha$; βt	He 9 65 keV $7 \cdot 10^{-21}$ s n	He 10 0.17 MeV $2.7 \cdot 10^{-21}$ s 2n

0.75E-4



B. Alex Brown, USNDP, BNL, Nov 6, 2008



Ni 48 ~2 ms ? 2p 1.35 ?	Ni 49 13 ms	Ni 50 12 ms	Ni 51 >200 ns	Ni 52 38 ms	Ni 53 45 ms	Ni 54 104 ms	Ni 55 209 ms	Ni 56 6.075 d
β^+ $\beta\bar{p}$ 3.7	β^+ $\beta\bar{p}$	β^+	$\beta^+ ?$	β^+ $\beta\bar{p}$ 1.34; 1.06	β^+ $\beta\bar{p}$ 1.90	β^+ γ 937 g	$\beta^+ 7.7\dots$ γ (2919; 2976; 3303)	ϵ ; no β^+ γ 158; 812; 750; 480; 270...

Ni 56 6.075 d	Ni 57 36.0 h	Ni 58 68.0769	Ni 59 $7.5 \cdot 10^4$ a	Ni 60 26.2231	Ni 61 1.1399	Ni 62 3.6345	Ni 63 100 a	Ni 64 0.9256	Ni 65 2.52 h	Ni 66 54.6 h	Ni 67 21 s	Ni 68 29 s
ϵ ; no β^+ γ 158; 812; 750; 480; 270...	ϵ β^+ 0.8... γ 1378; 1920; 127...	σ 4.6 $\sigma_{n,\alpha} < 0.00003$	ϵ ; $\beta^+ ...$ no γ ; σ 77.7 $\sigma_{n,\alpha}$ 14; $\sigma_{n,p}$ 2 σ_{abs} 92	σ 2.9	σ 2.5 $\sigma_{n,\alpha}$ 0.00003	σ 15	$\beta^- 0.07$ no γ σ 20	σ 1.6	$\beta^- 2.1\dots$ γ 1482; 1115; 366...	$\beta^- 0.2$ no γ σ 22	$\beta^- 3.8\dots$ γ (1937; 1115; 822...)	β^- γ 758; 84 g

Ni 68 29 s	Ni 69 11.4 s	Ni 70 6.0 s	Ni 71 2.56 s	Ni 72 1.57 s	Ni 73 0.84 s	Ni 74 0.9 s	Ni 75 344 ms	Ni 76 238 ms	Ni 77 128 ms	Ni 78 110 ms
β^- γ 758; 84 g	β^- γ 1871; 680; 1213; 1483...	β^- 3.3... γ 1036; 78... m_2	β^- γ 534; 2016	β^- γ 376; 94	β^- γ 166; 1010	β^- γ 166*; 694 $\beta\bar{n}$	β^-	β^-	β^-	β^-



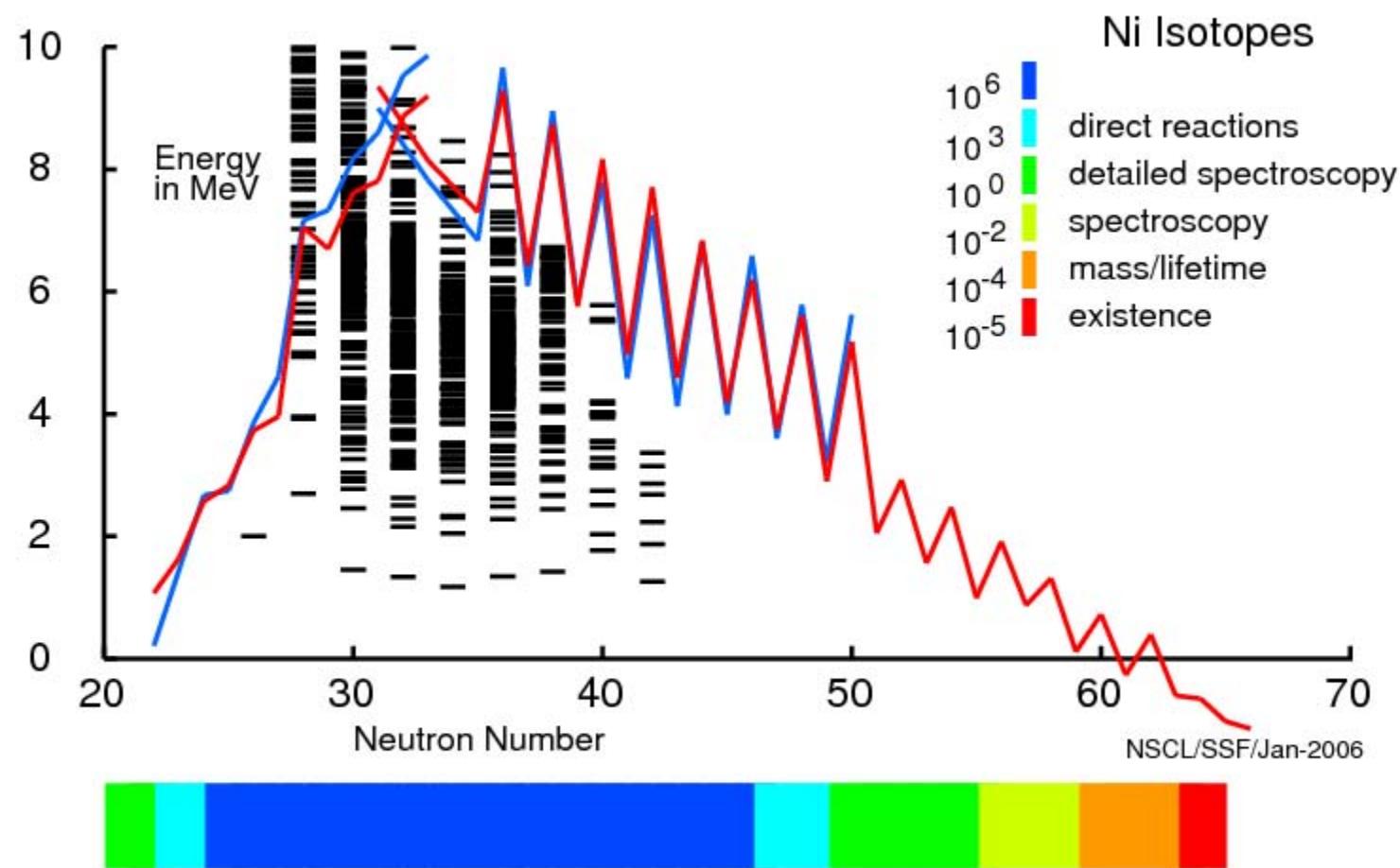
B. Alex Brown, USNDP, BNL, Nov 6, 2008

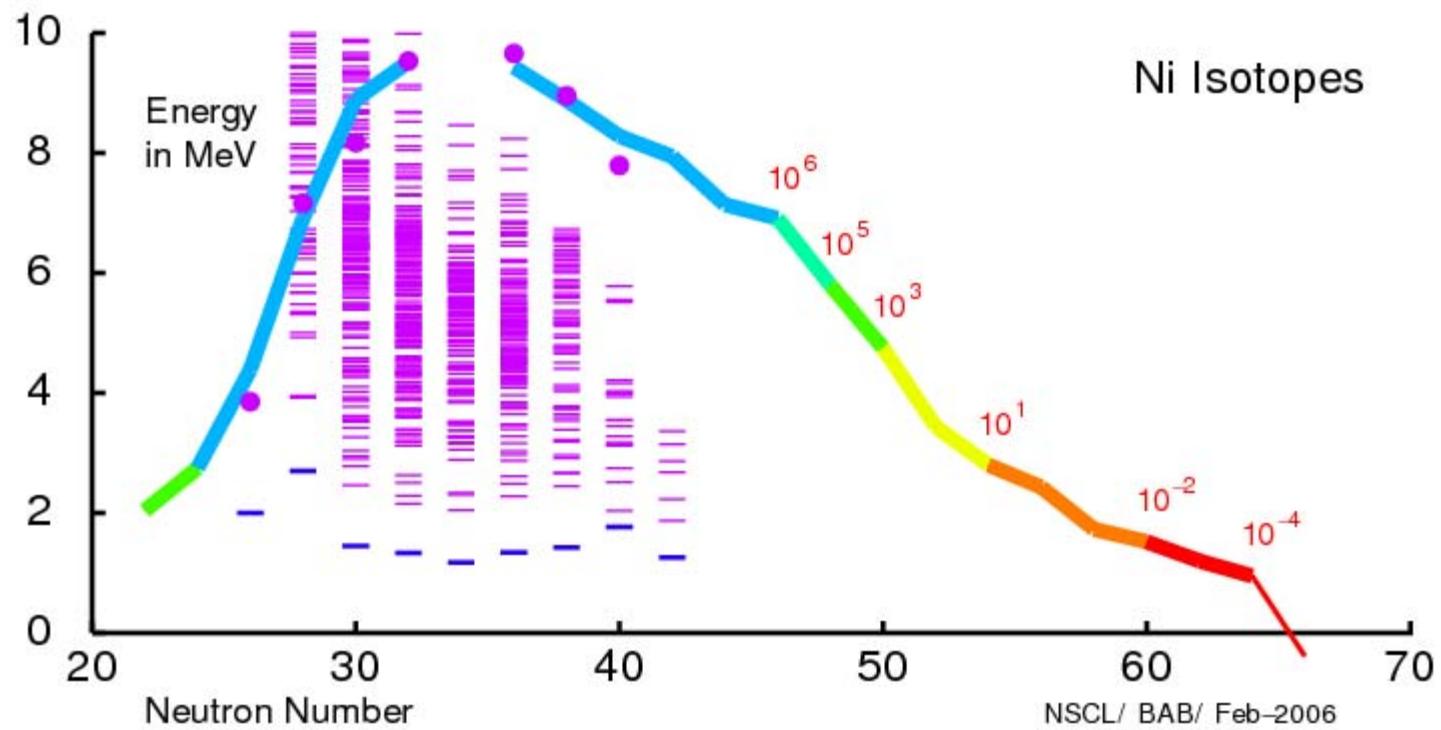


Isotope Science Facility at Michigan State University

Upgrade of the NSCL rare isotope
research capabilities

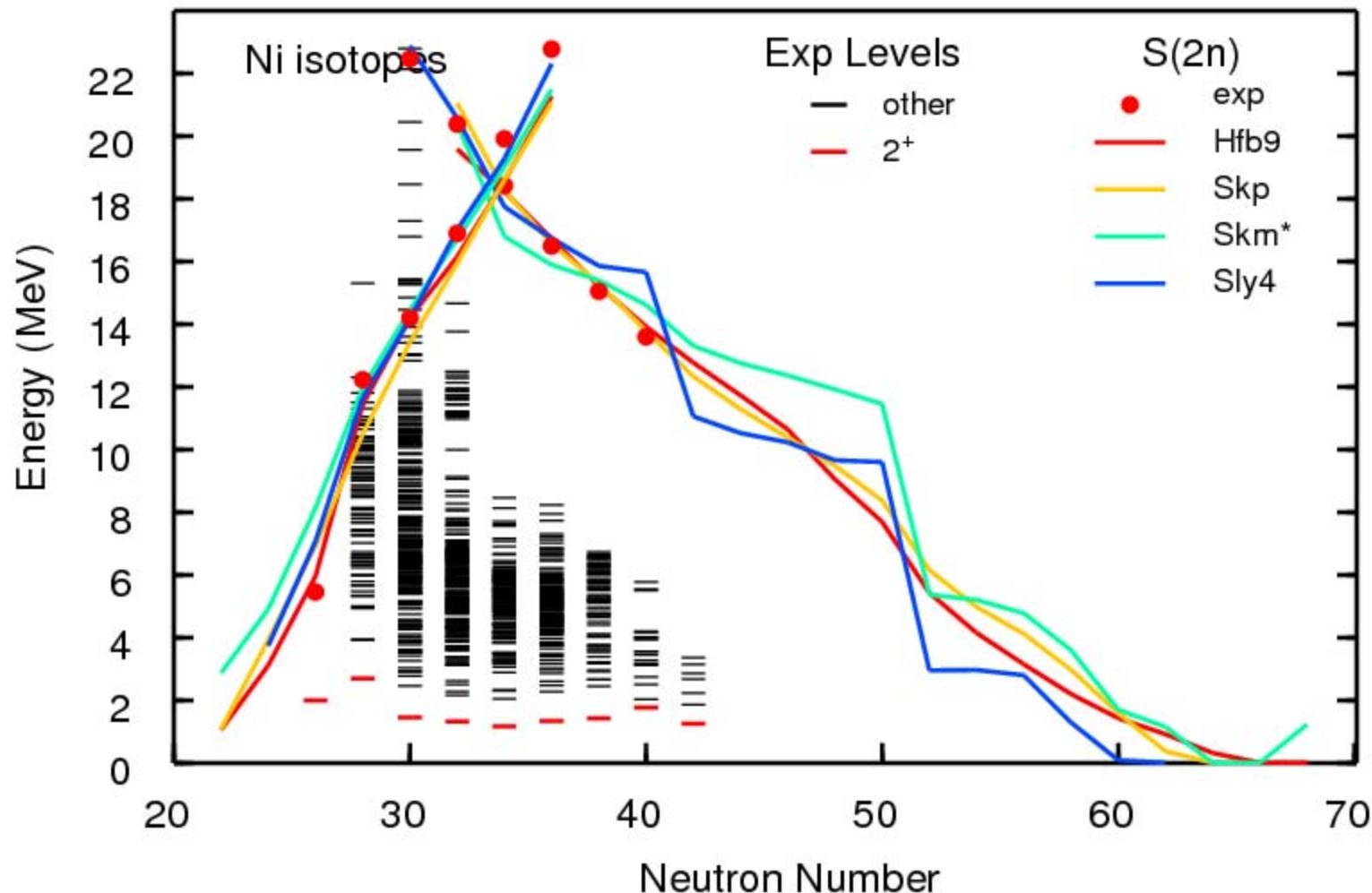


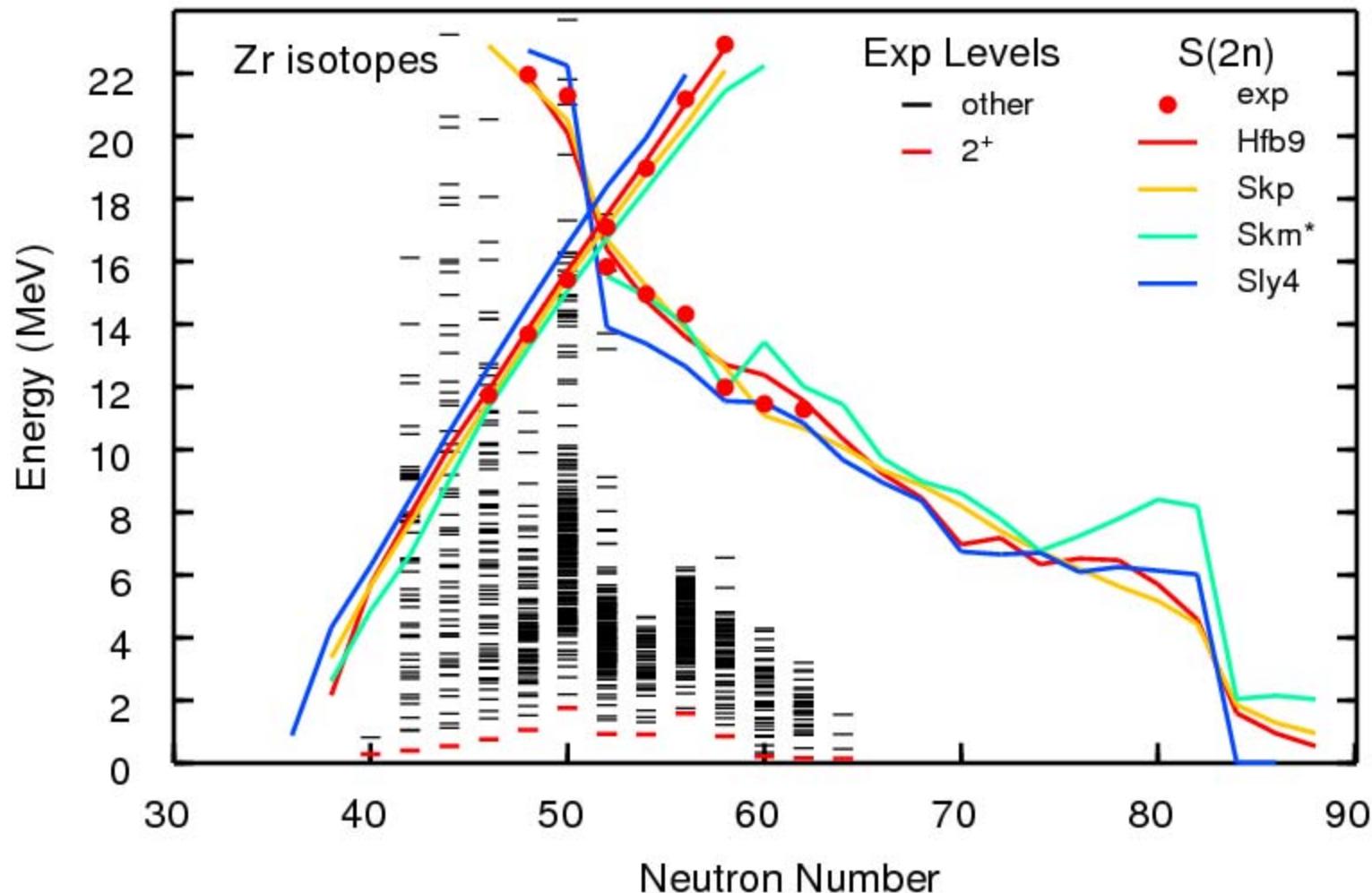


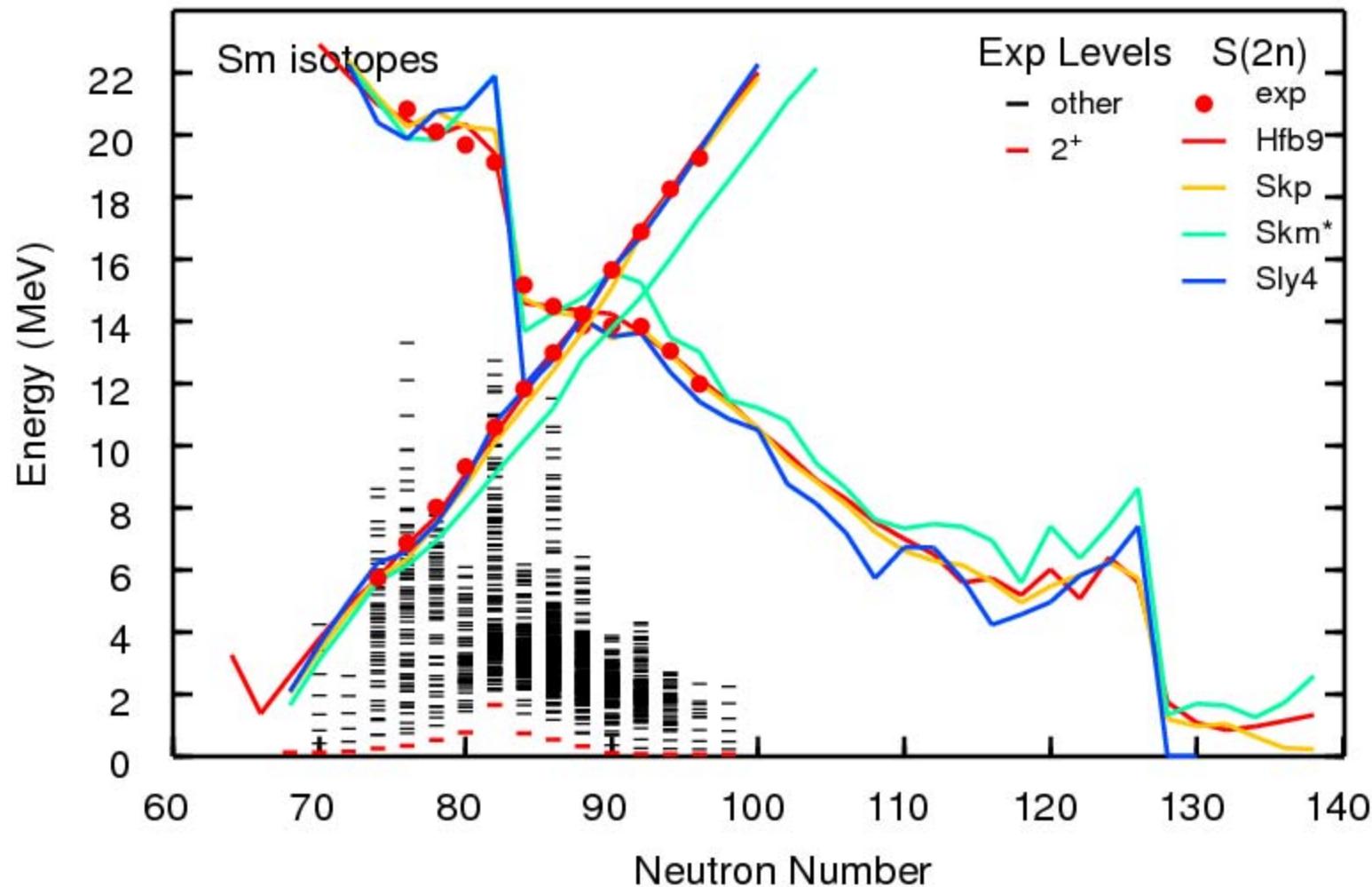


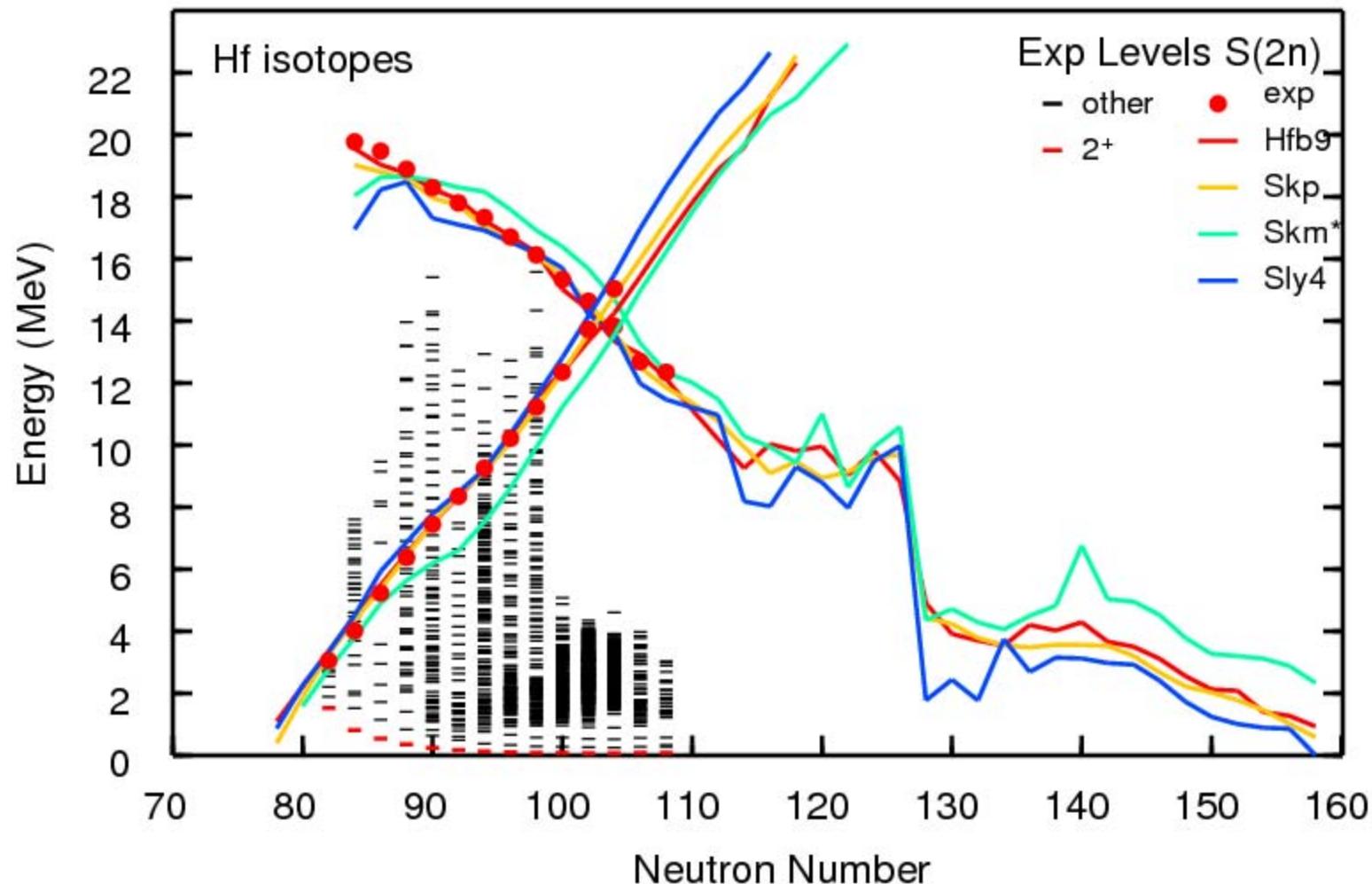
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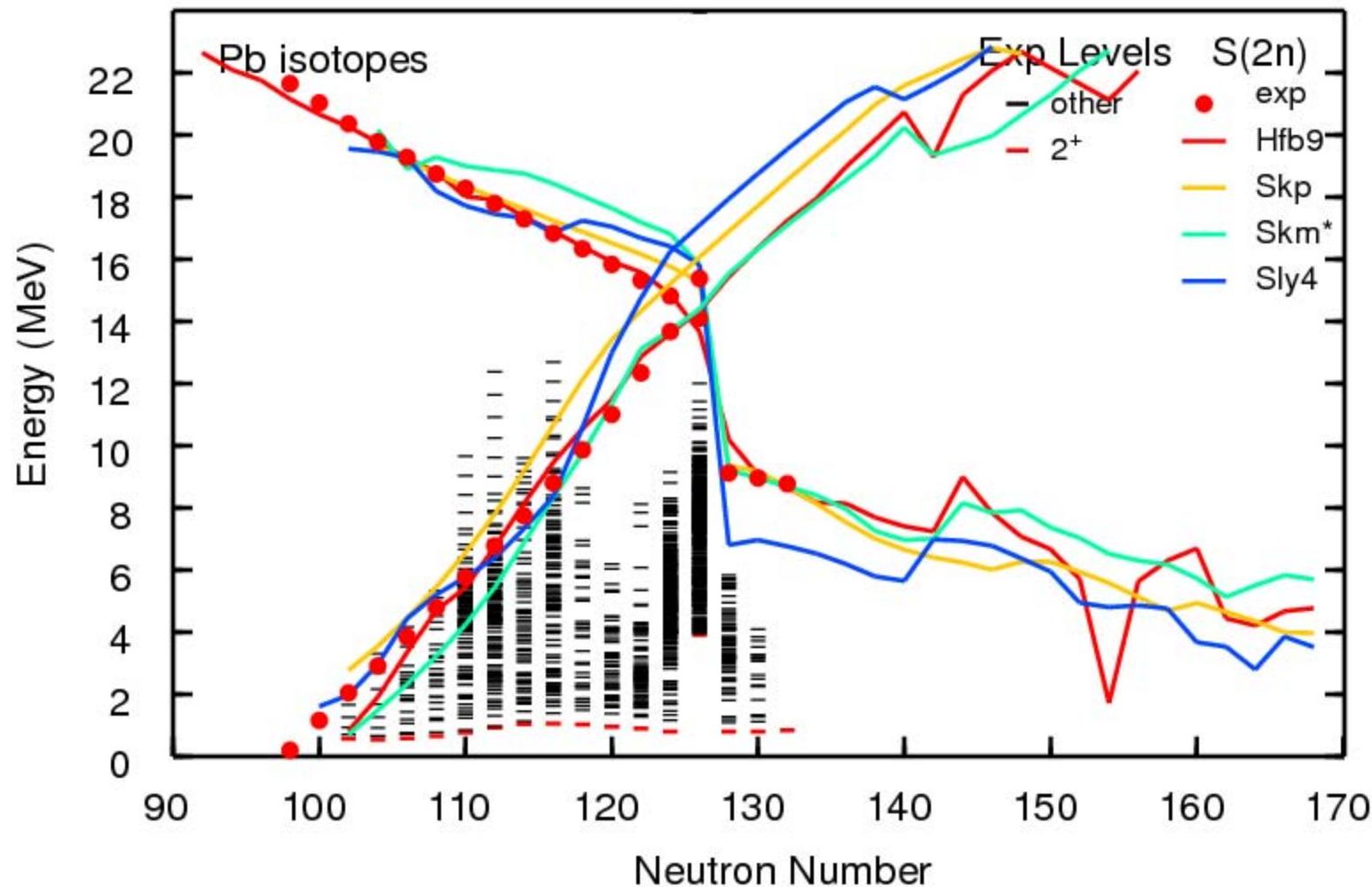


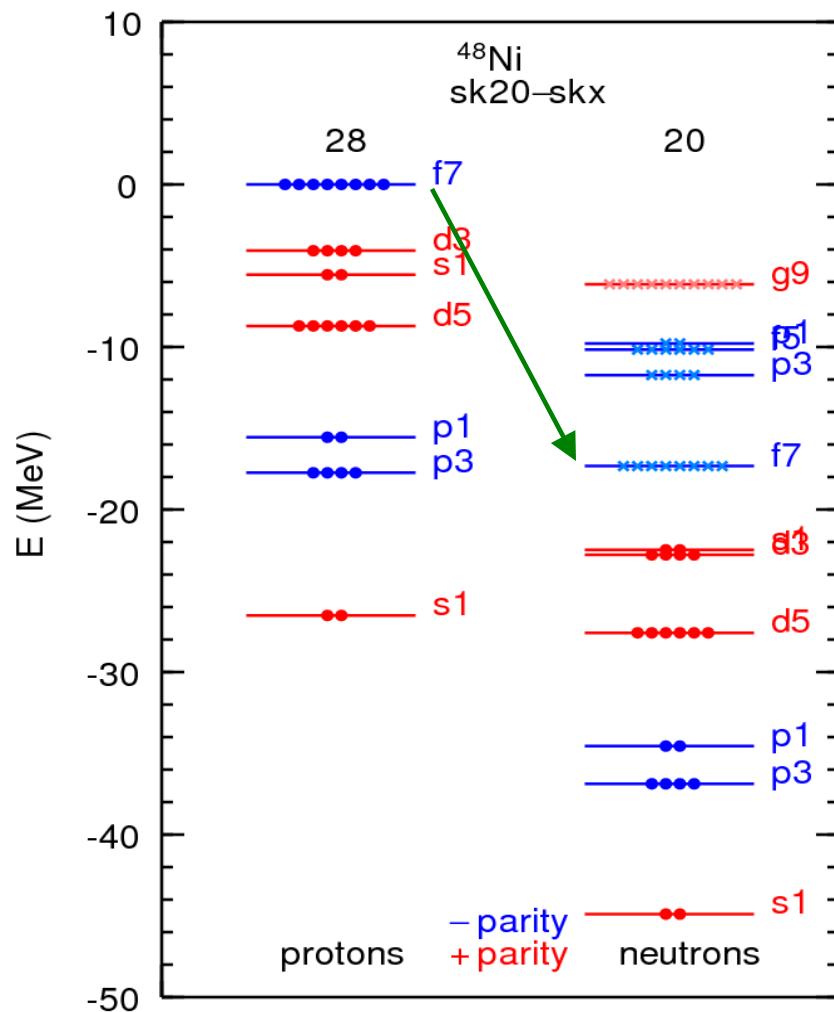


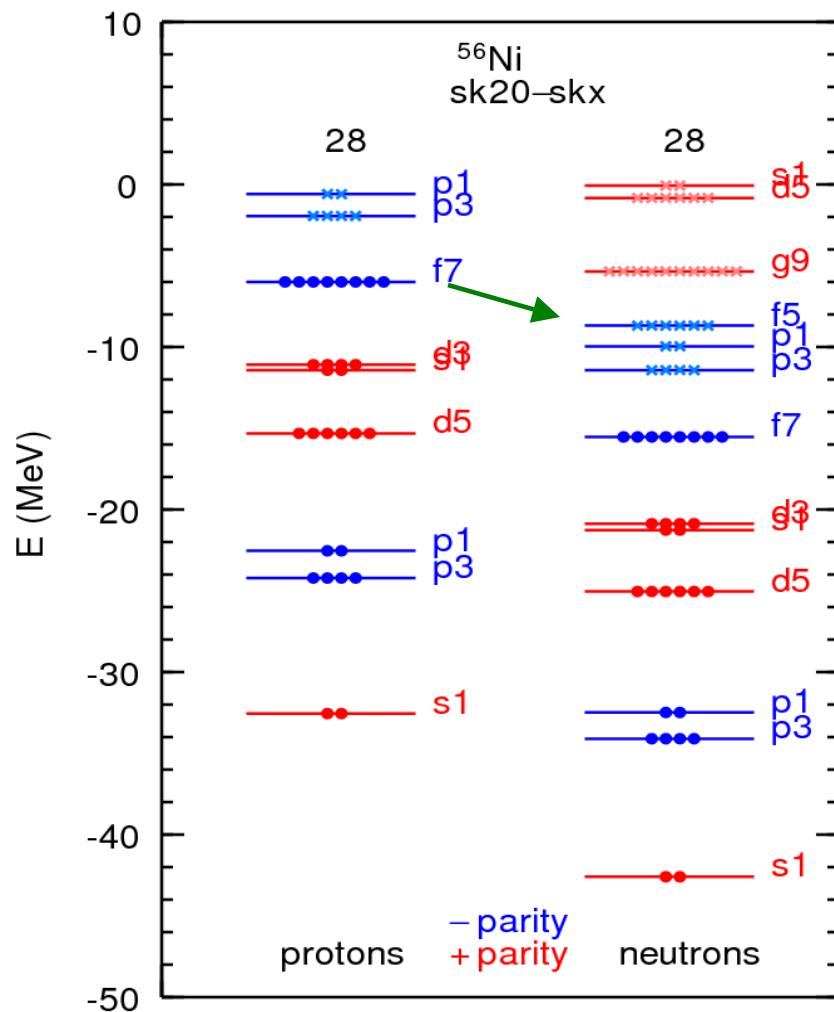


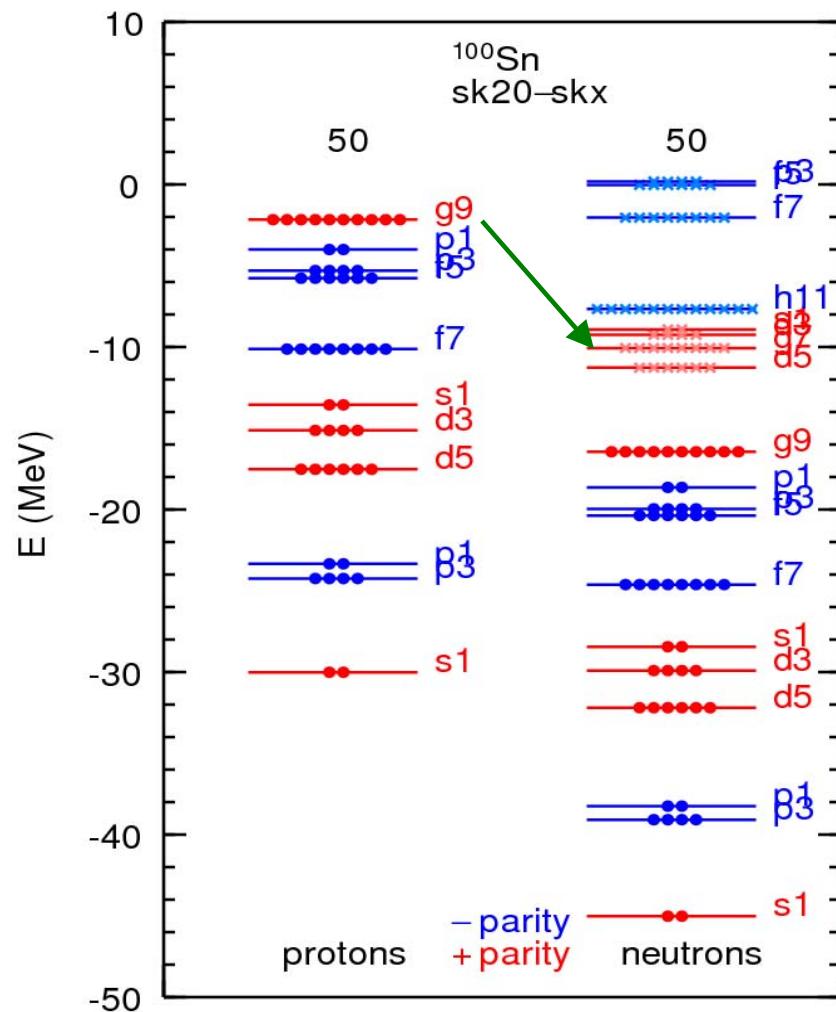


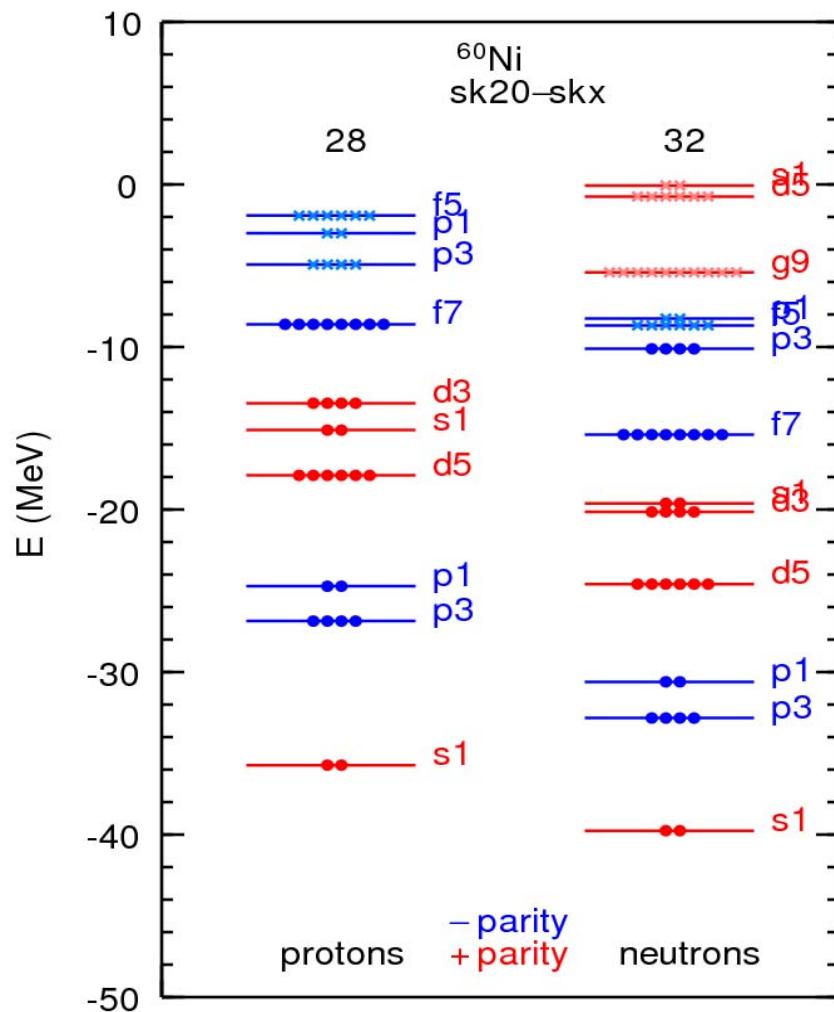


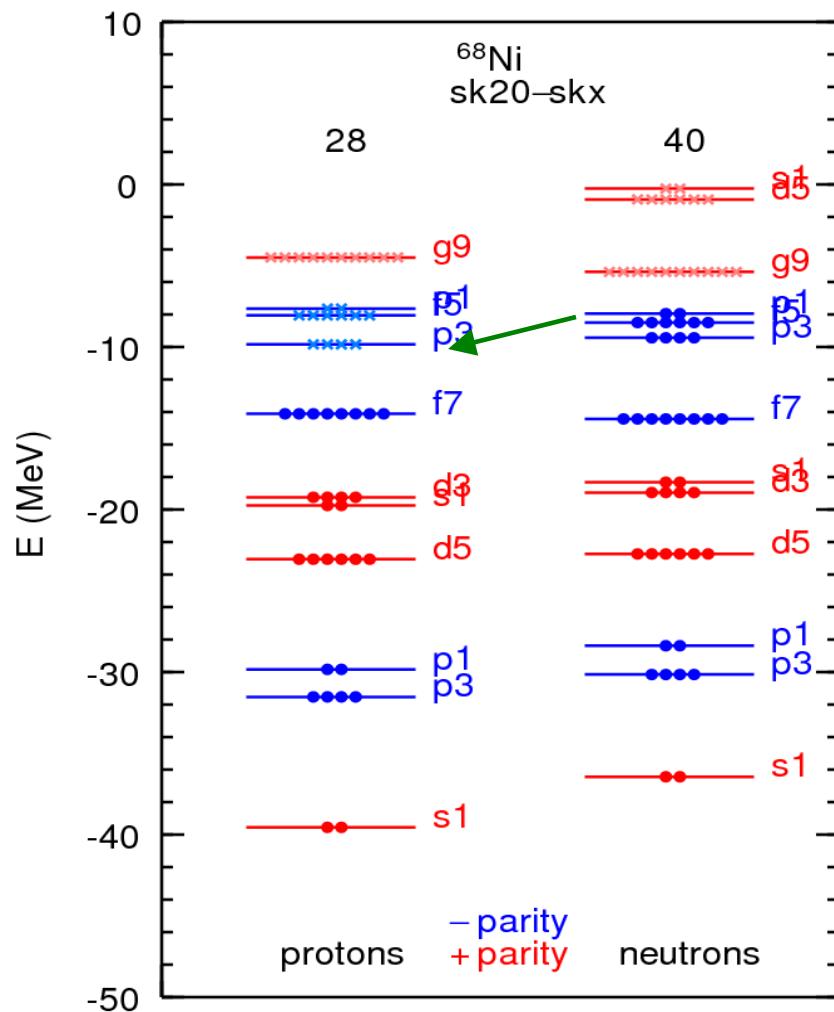


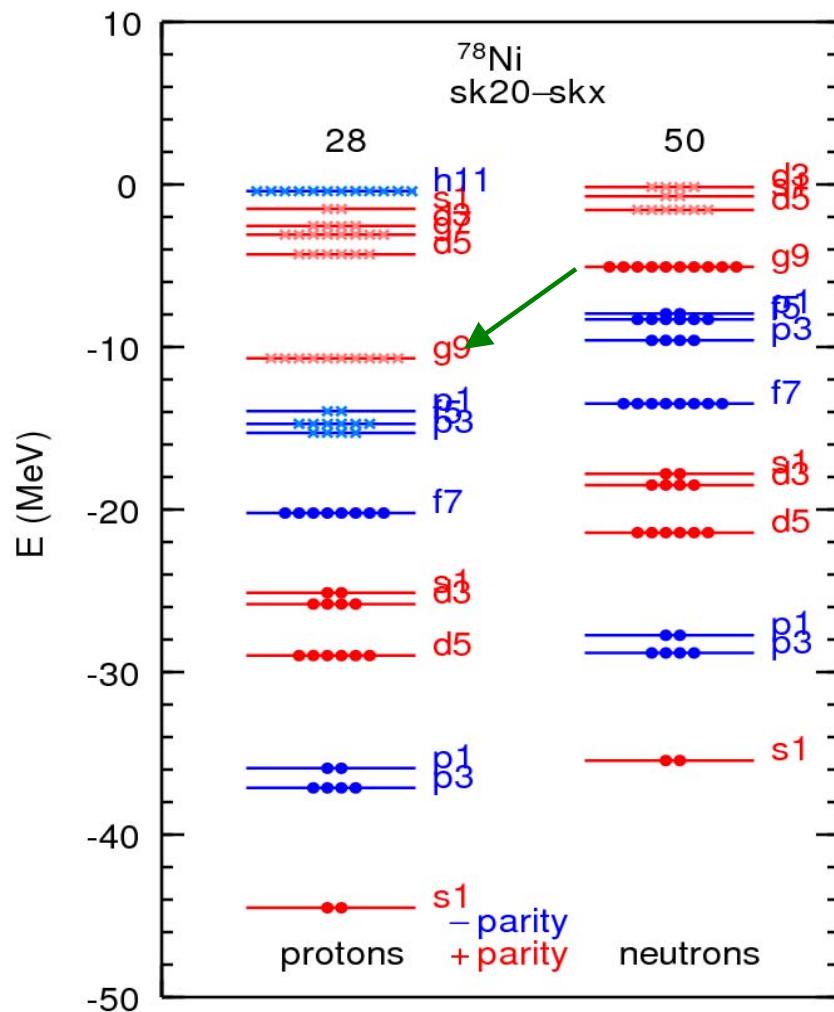












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**CHARGE-DEPENDENT TWO-BODY INTERACTIONS
DEDUCED FROM DISPLACEMENT ENERGIES
IN THE $1f_{\frac{5}{2}}$ SHELL[†]**

B. A. BROWN^{††}

Cyclotron Laboratory, Michigan State University, East Lansing, Michigan 48824

and

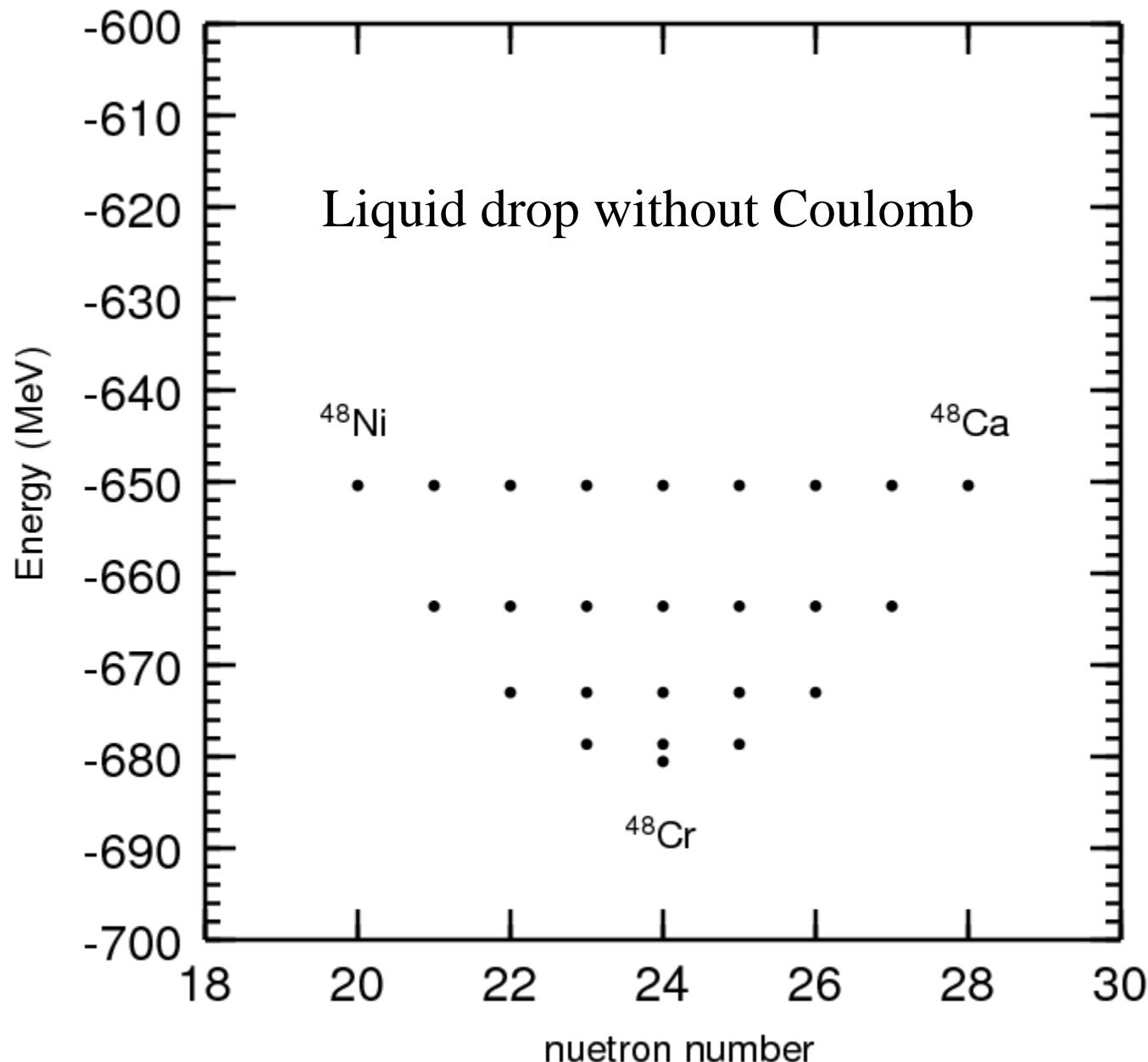
R. SHERR

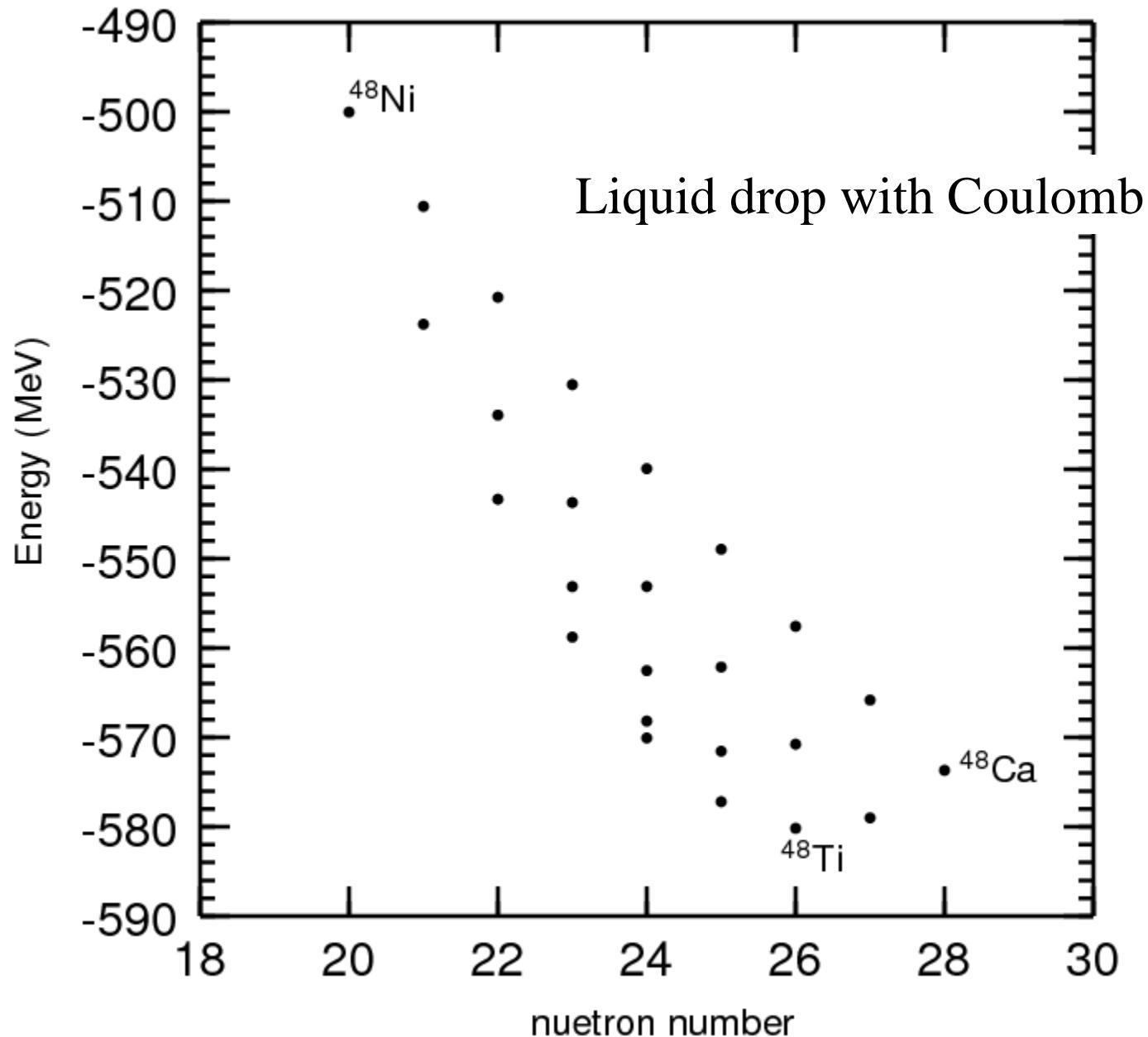
Joseph Henry Laboratories, Princeton University, Princeton, New Jersey 08540



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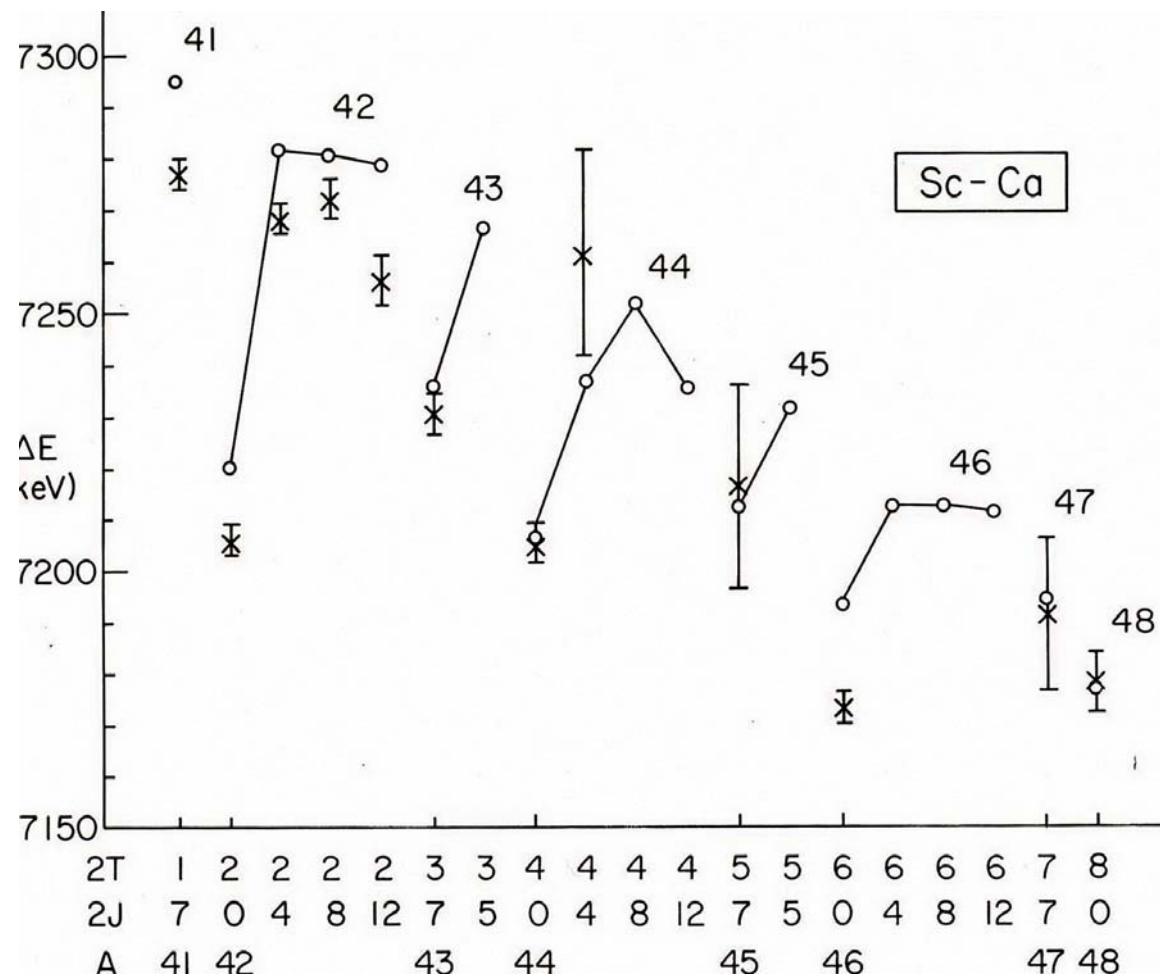


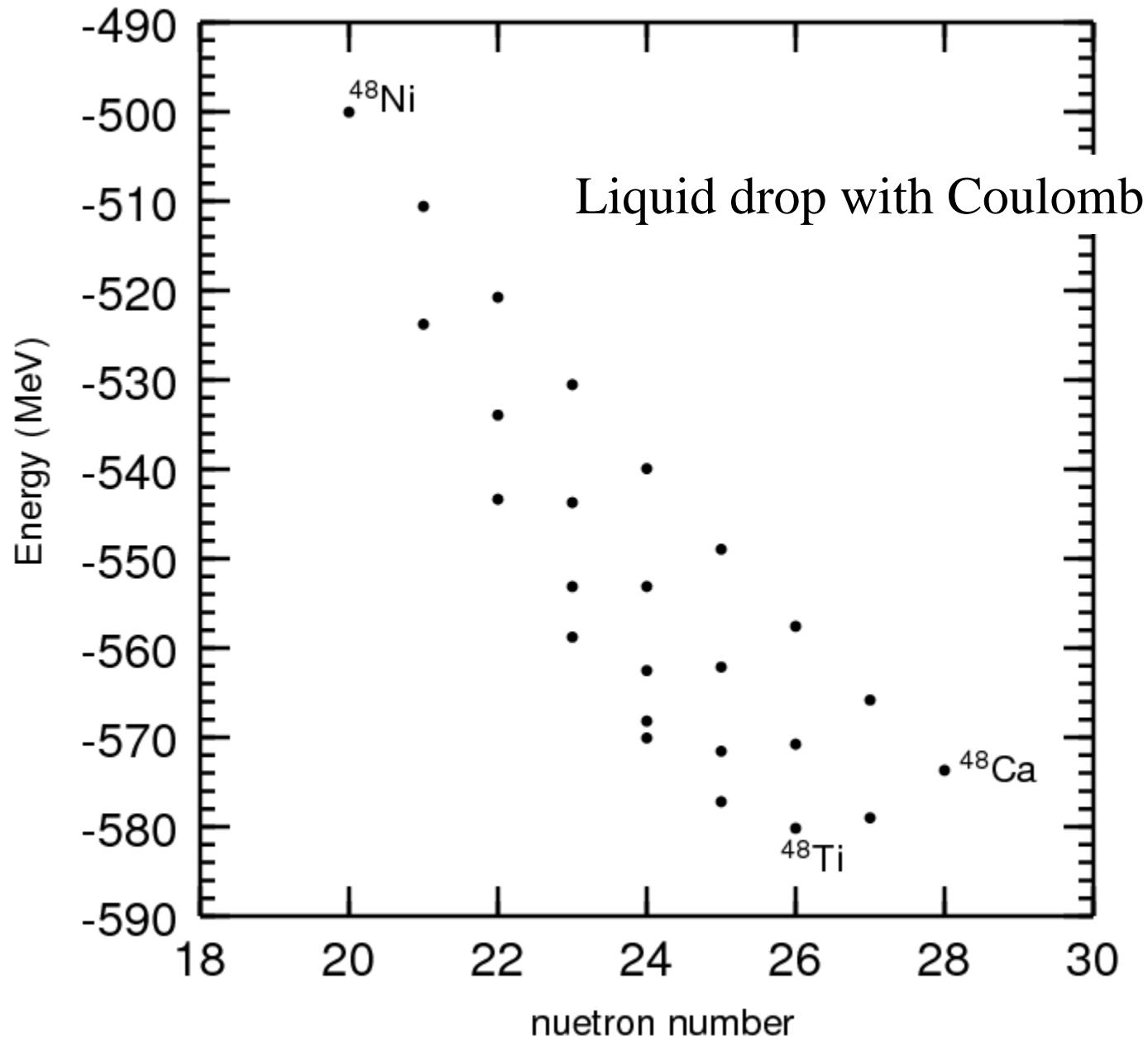




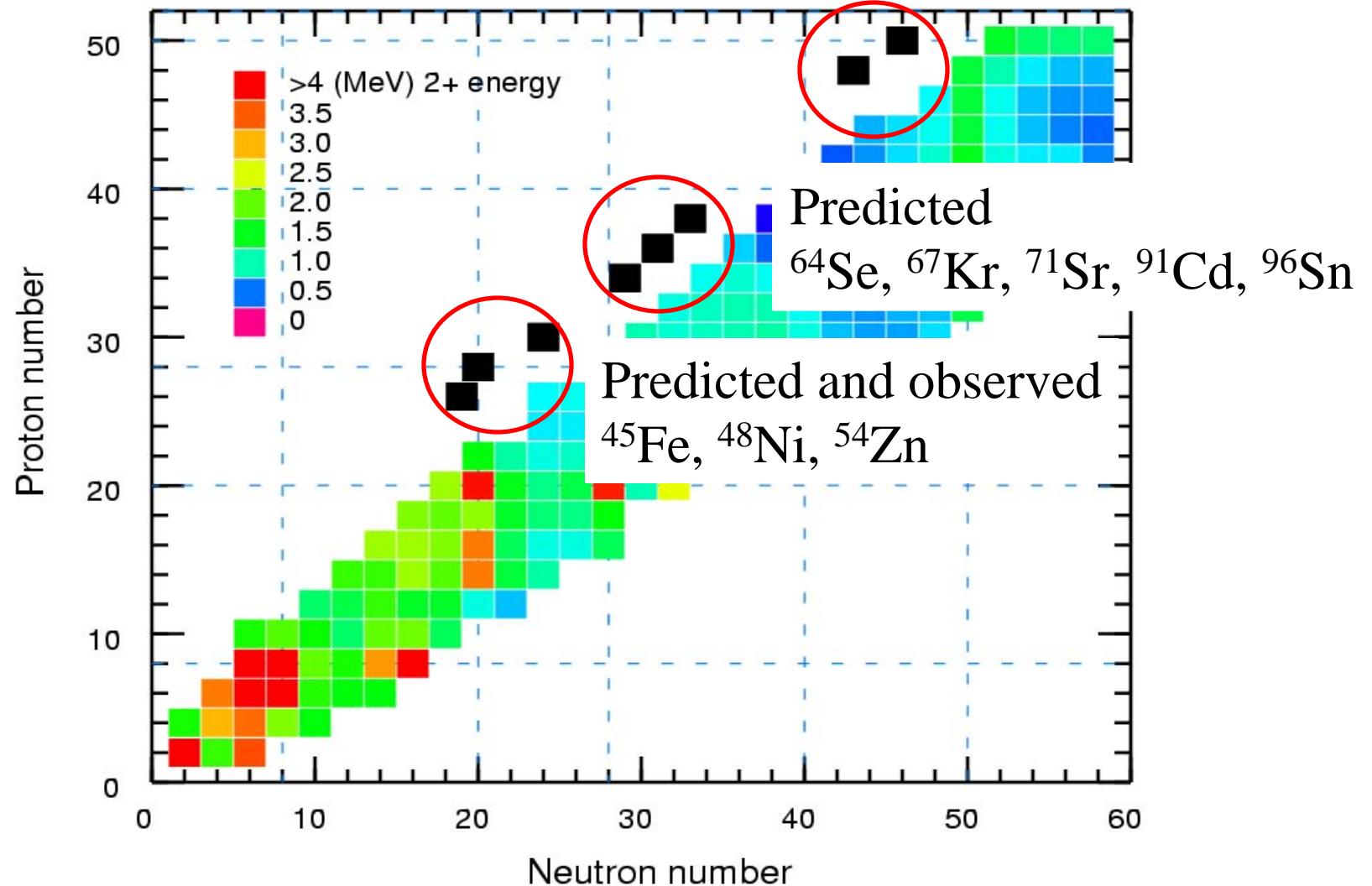
About 60 energies of isobaric analogue states for A=41-55 measured to few keV accuracy

$(f_{7/2})^n$ models with 8 parameters fit all of them to 12 keV rms





Di-proton decay



Q-value results for ^{48}Ni

$Q(\text{exp}) = 1.35 (2) \text{ MeV}$ Dossat et al. 2006 (one event)

$Q(\text{th}) = 1.36 (13)$ Brown 1991 (IMME)

3.1 (6) Audi-Wapstra extrapolation 2003

0.0-2.0 Nazarewicz et al 1996 (mean-field)



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Di-proton decay = horses to hay

What is the cluster dynamics of di-proton decay ?

^{48}Ni di-proton vs $^{48}\text{Ca}(\text{p},\text{t})^{46}\text{Ca}$?



Results for di-proton decay

Nucleus	exp Q_{2p} (MeV)	exp (a) $T_{1/2}$ (ms)	theory (b) $T_{1/2}$ (ms)	S (c)
^{45}Fe	1.151(15)	2.4 - 3.9	14 - 22 (d)	0.272
^{48}Ni	1.35(2)	<21	4 - 11	0.188
^{54}Zn	1.48(2)	2.7 - 5.9	3 - 8	0.313

- (a) B. Blank, J. Giovinazzo, M. Pfutzner.....
- (b) B. A. Brown and F. C. Barker, Phys. Rev. C67, 041304(R) (2003).
includes correlations (pairing) – three-body Coulomb asymptotics
in R matrix with pp resonance as an intermediate state

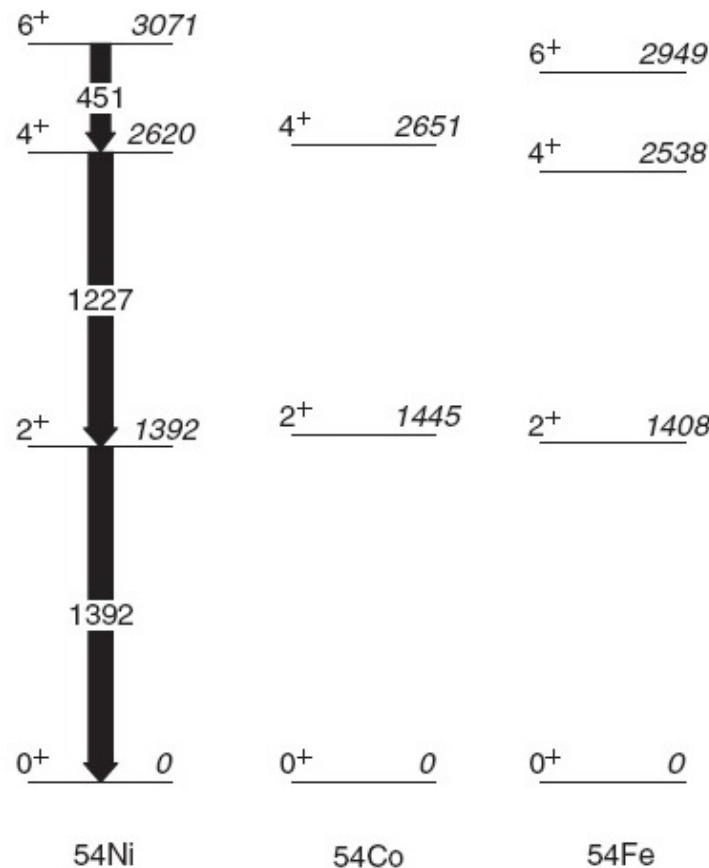
(c) Two-particle spectroscopic factor

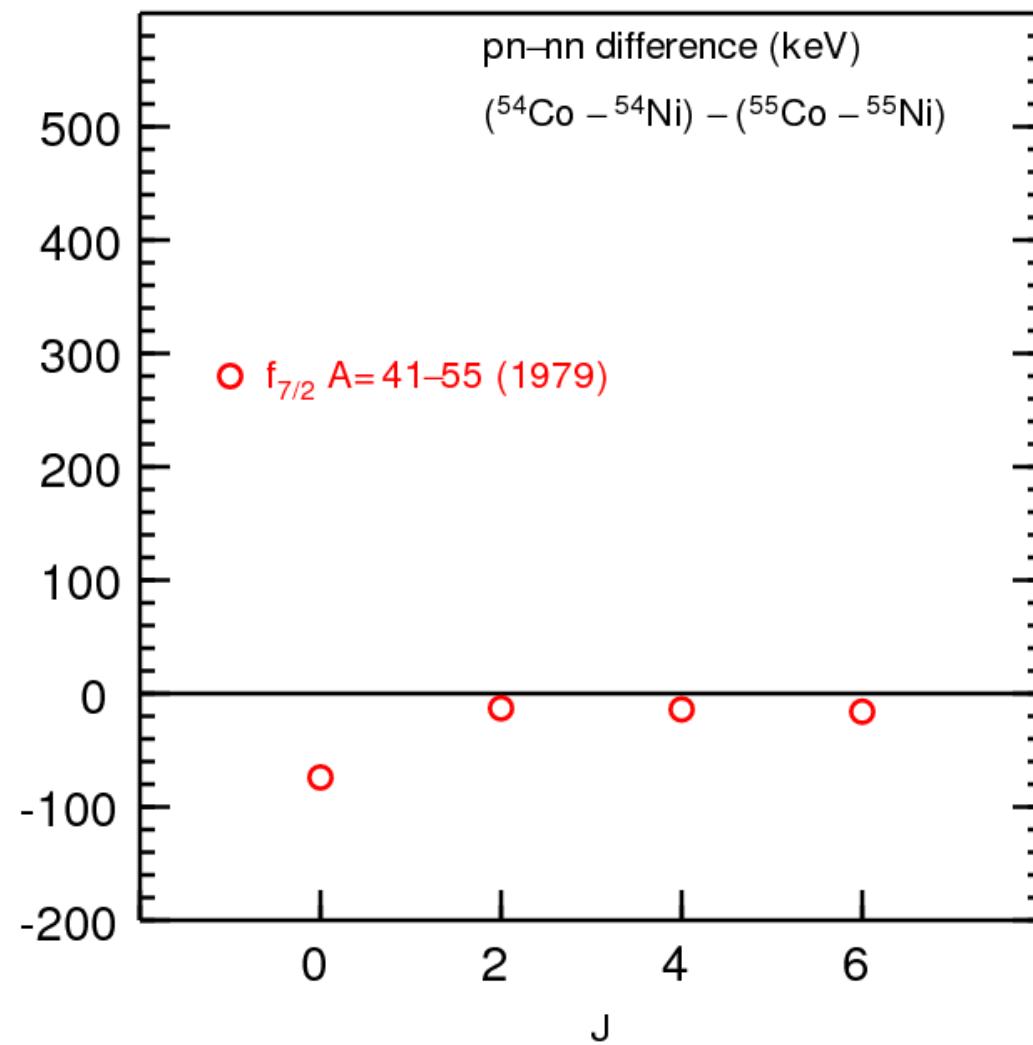
Grigorenko and Zukov, Phys. Rev. C, 68, 054005 (2003).
single-particle model (no correlations)
but includes full three-body decay with Coulomb



Observation of ^{54}Ni : Cross-Conjugate Symmetry in $f_{7/2}$ Mirror Energy Differences

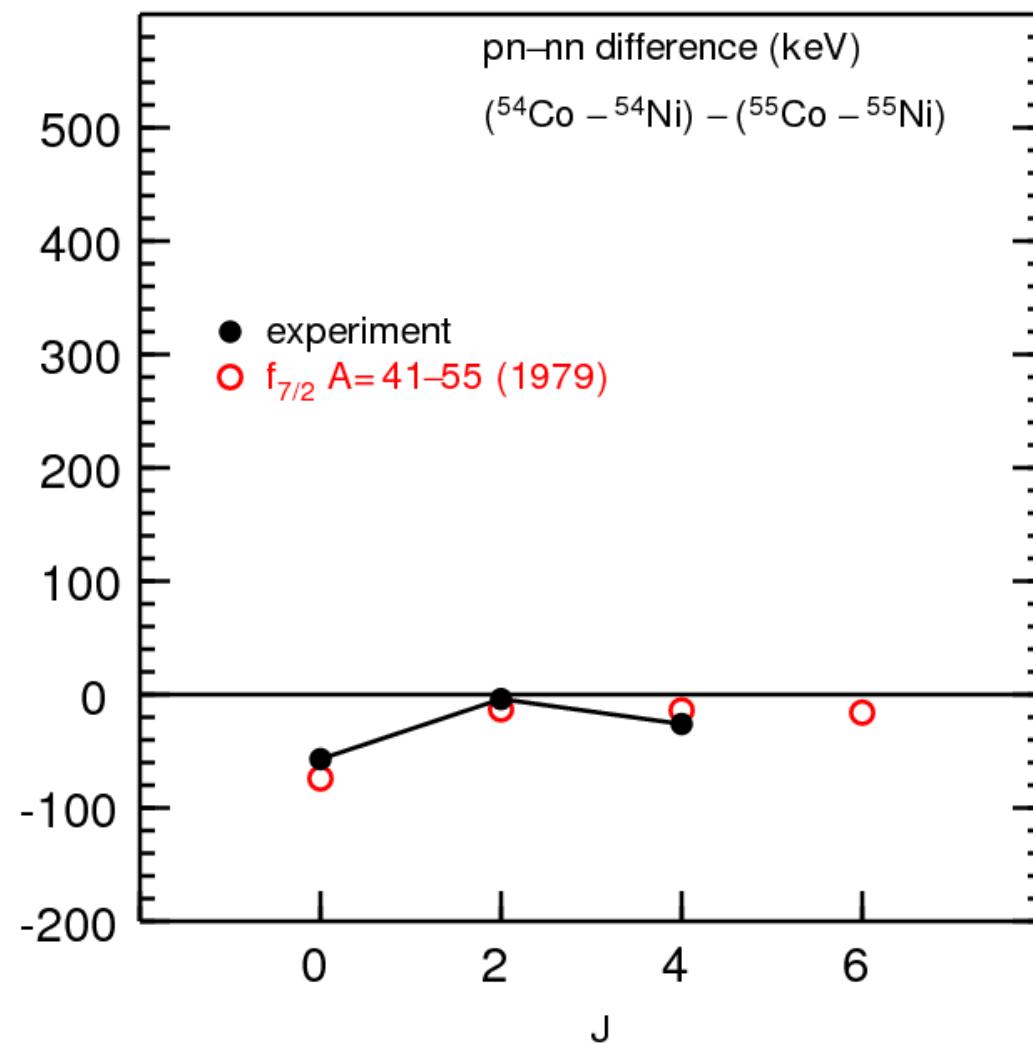
A. Gadea,¹ S. M. Lenzi,² S. Lunardi,² N. Mărginean,^{1,3} A. P. Zuker,⁴ G. de Angelis,¹ M. Axiotis,¹ T. Martínez,¹ D. R. Napoli,¹ E. Farnea,² R. Menegazzo,² P. Pavan,² C. A. Ur,^{2,3} D. Bazzacco,² R. Venturelli,² P. Kleinheinz,⁵ P. Bednarczyk,^{4,6} D. Curien,⁴ O. Dorvaux,⁴ J. Nyberg,⁷ H. Grawe,⁸ M. Górska,⁸ M. Palacz,⁹ K. Lagergren,¹⁰ L. Milechina,¹⁰ J. Ekman,¹¹ D. Rudolph,¹² C. Andreoiu,¹² M. A. Bentley,¹³ W. Gelletly,¹⁴ B. Rubio,¹⁵ A. Algora,¹⁵ E. Nacher,¹⁵ L. Caballero,¹⁵ M. Trotta,¹⁶ and M. Moszvński¹⁷





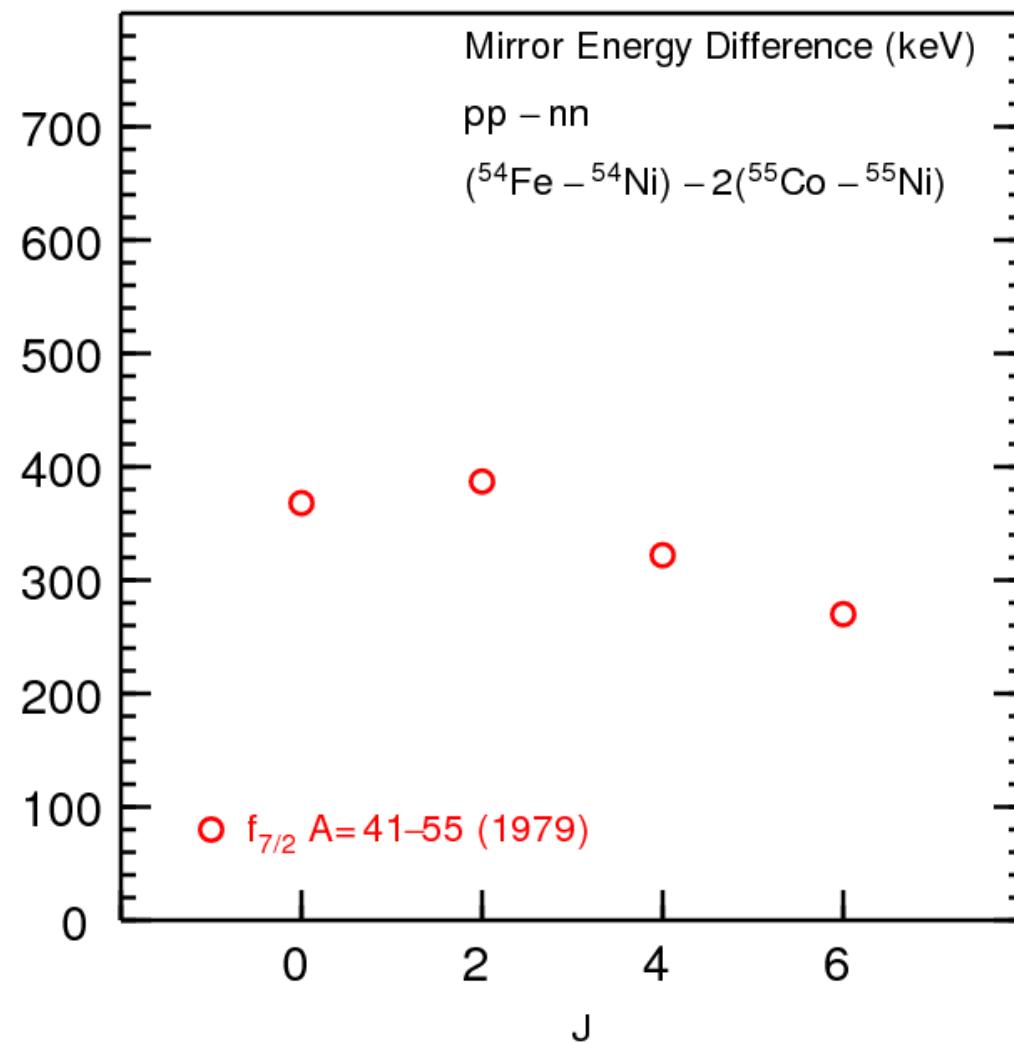
B. Alex Brown, USNDP, BNL, Nov 6, 2008





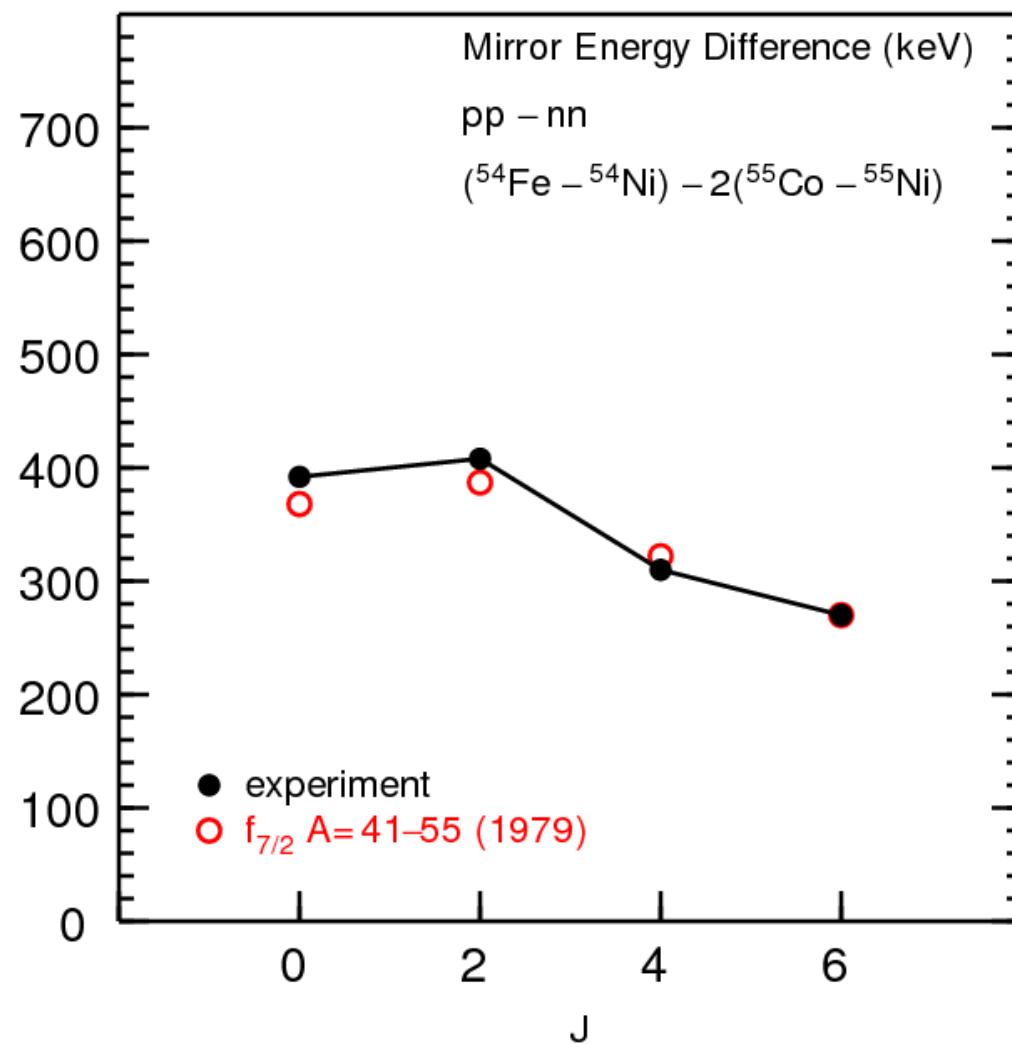
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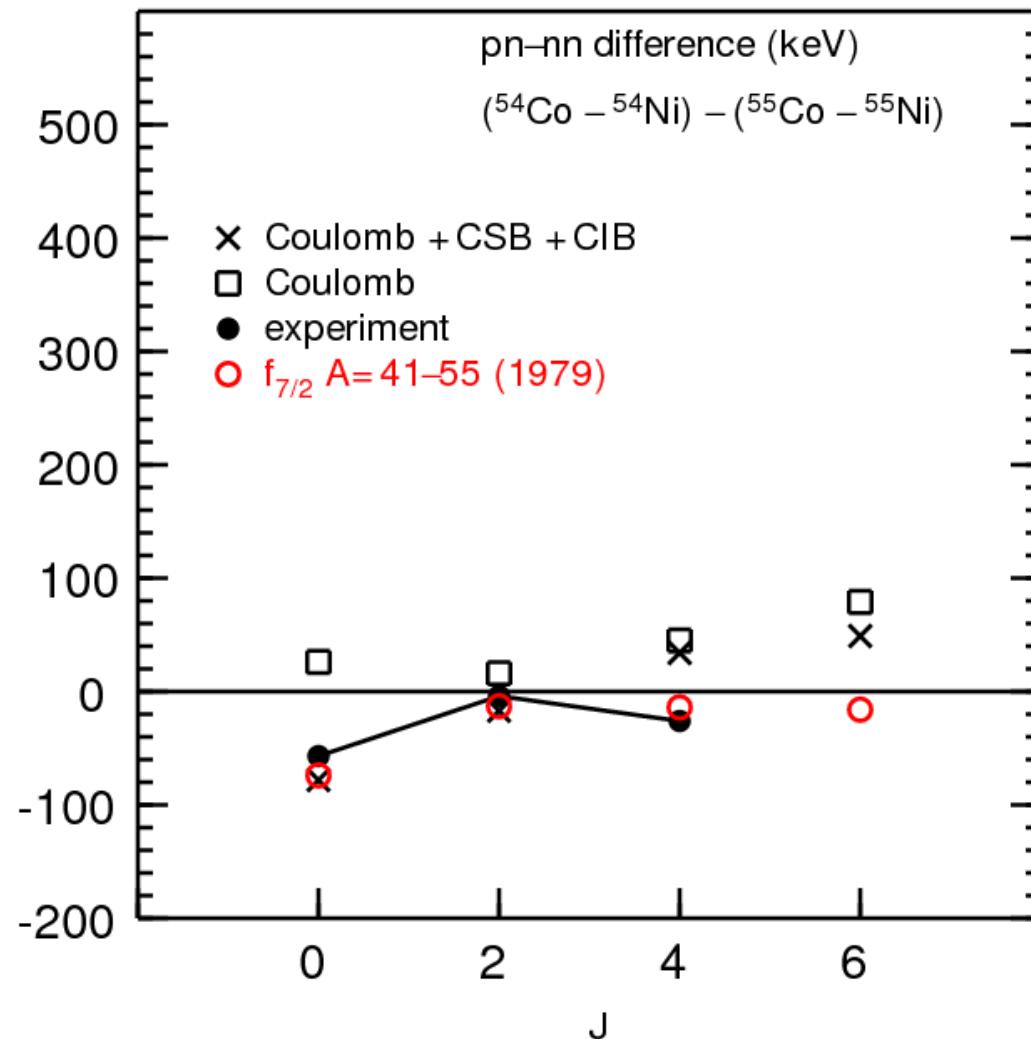


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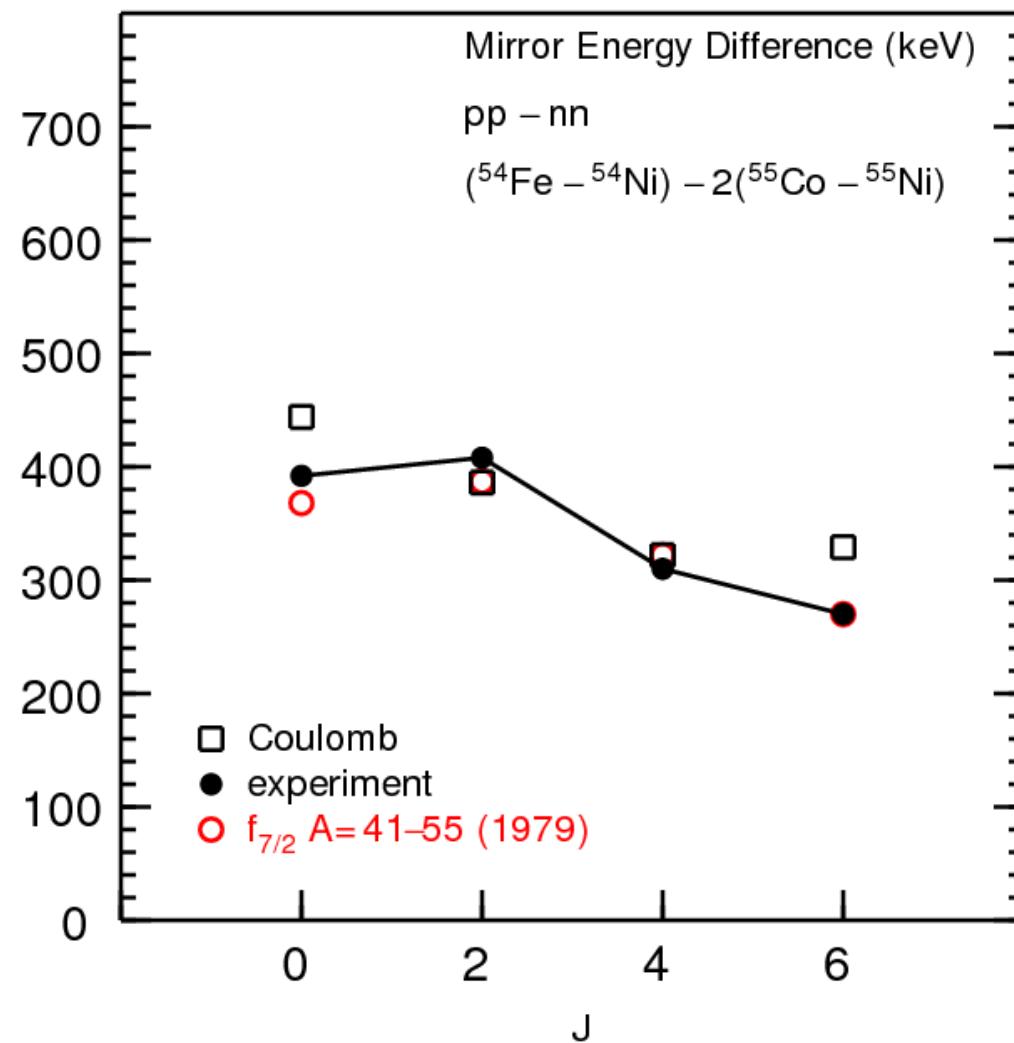




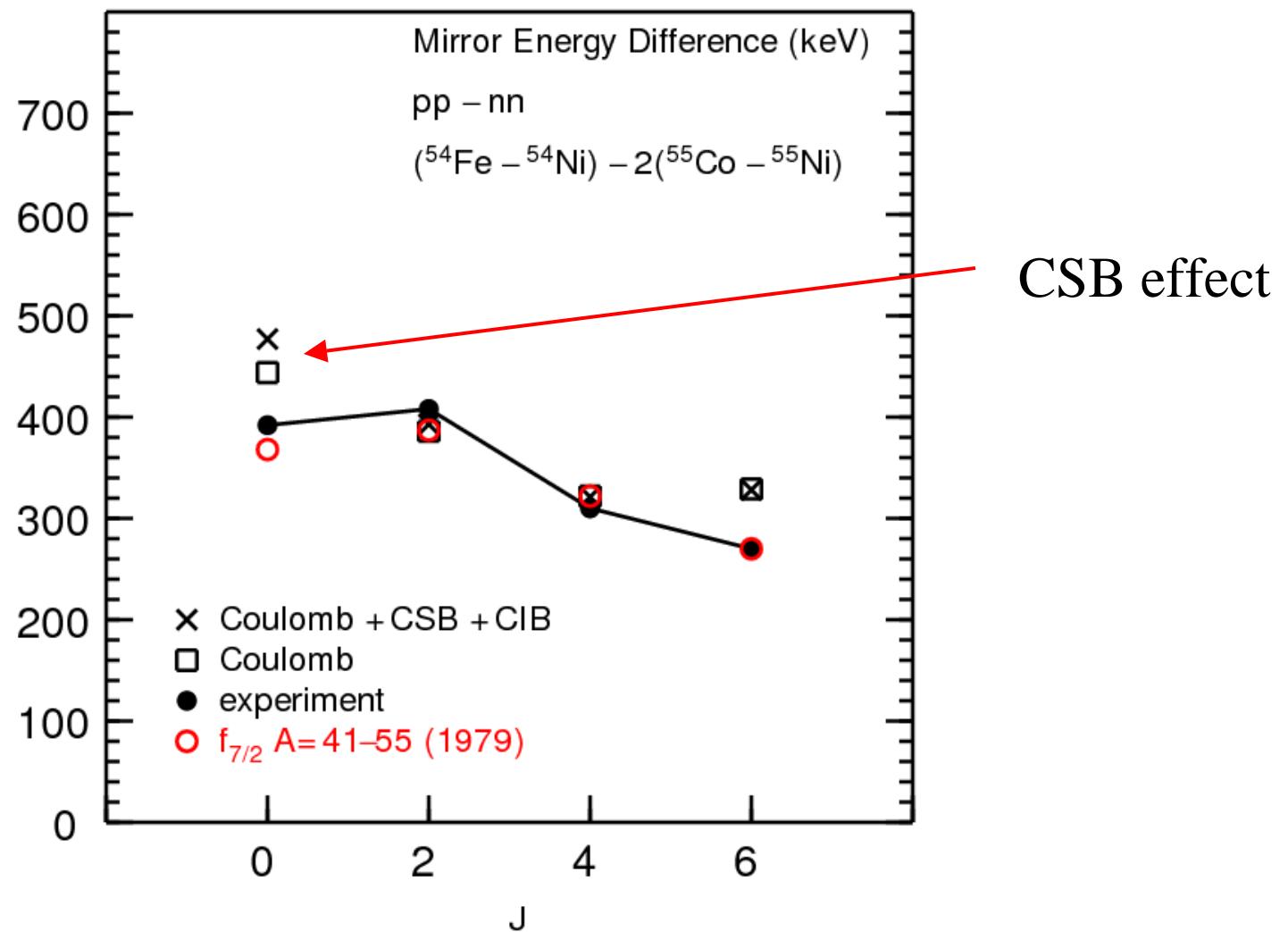
N3LO V-lowk 6hw 2nd order – “full” pf shell (Angelo Signoracci)



N3LO V-lowk 6hw 2nd order – “full” pf shell (Angelo Signoracci)



N3LO V-lowk 6hw 2nd order – “full” pf shell (Angelo Signoracci)



	N ³ LO ^a	Experiment ^b
¹ S ₀		
a_{pp}^C	-7.8188	-7.8196±0.0026
r_{pp}^C	2.795	2.790±0.014
a_{pp}^N	-17.083	
r_{pp}^N	2.876	
a_{nn}^N	-18.900	-18.9±0.4
r_{nn}^N	2.838	2.75±0.11
a_{np}	-23.732	-23.740±0.020
r_{np}	2.725	2.77±0.05
³ S ₁		
a_t	5.417	5.419±0.007
r_t	1.752	1.753±0.008

From n+d -18.7(6) PRL 83, 3788 (1999)
 -16.3(40) PRL 85, 1190 (2000)

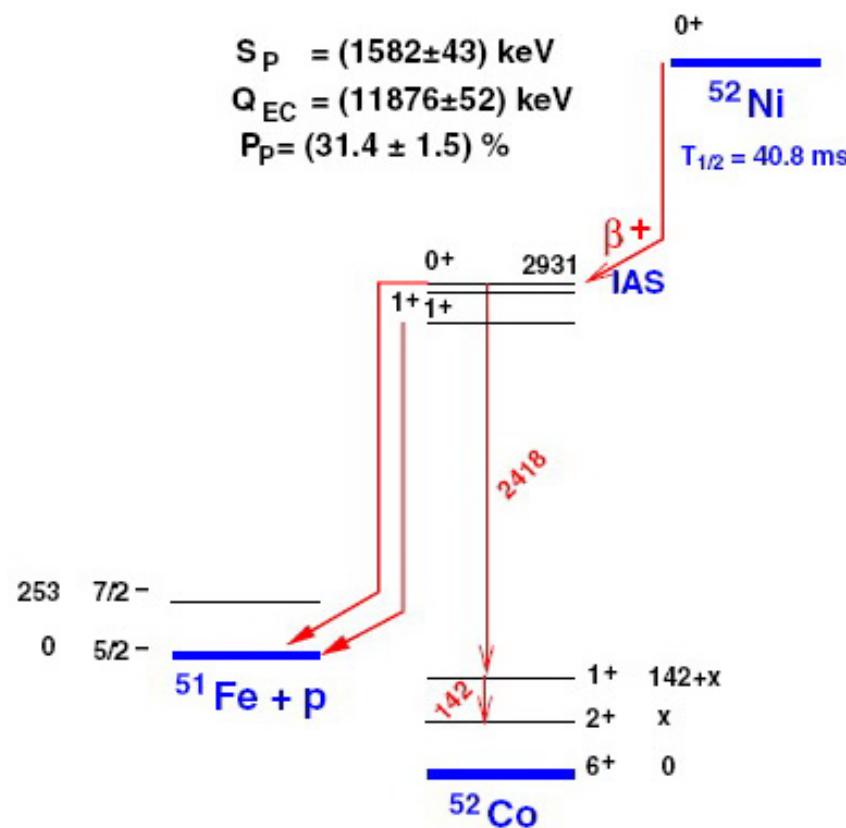


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Bertram Blank – isospin forbidden proton decay

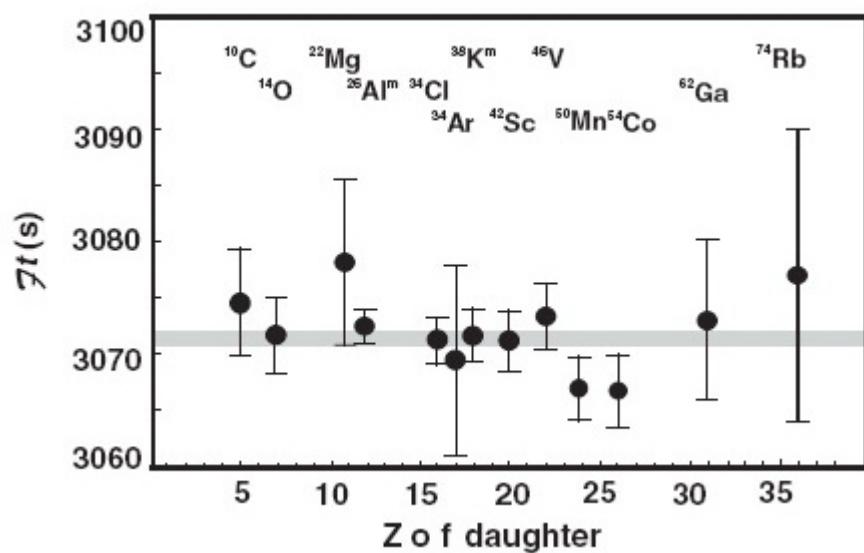
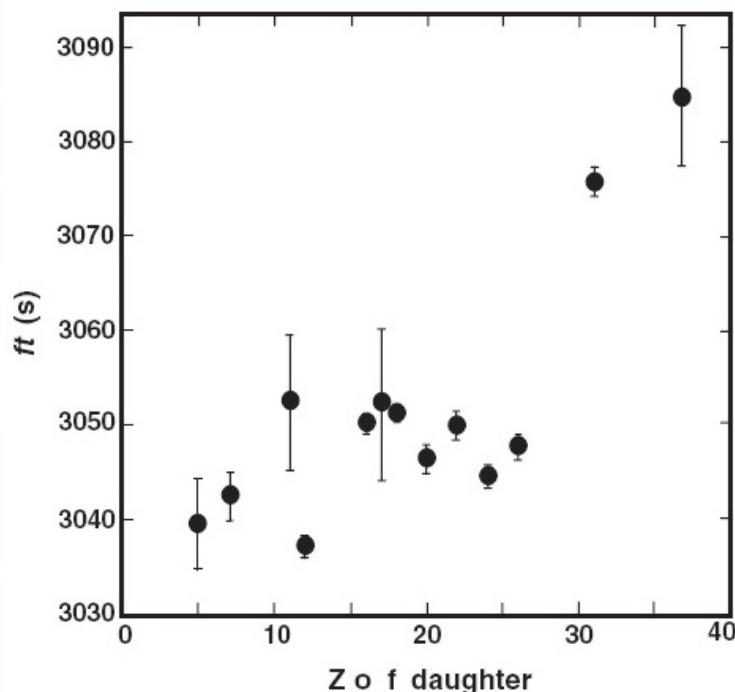
^{52}Co 0^+ T=4 to ^{51}Fe $5/2^-$ T=1/2



Improved calculation of the isospin-symmetry-breaking corrections to superallowed Fermi β decay

I. S. Towner^{*} and J. C. Hardy

Cyclotron Institute, Texas A&M University, College Station, Texas 77843, USA

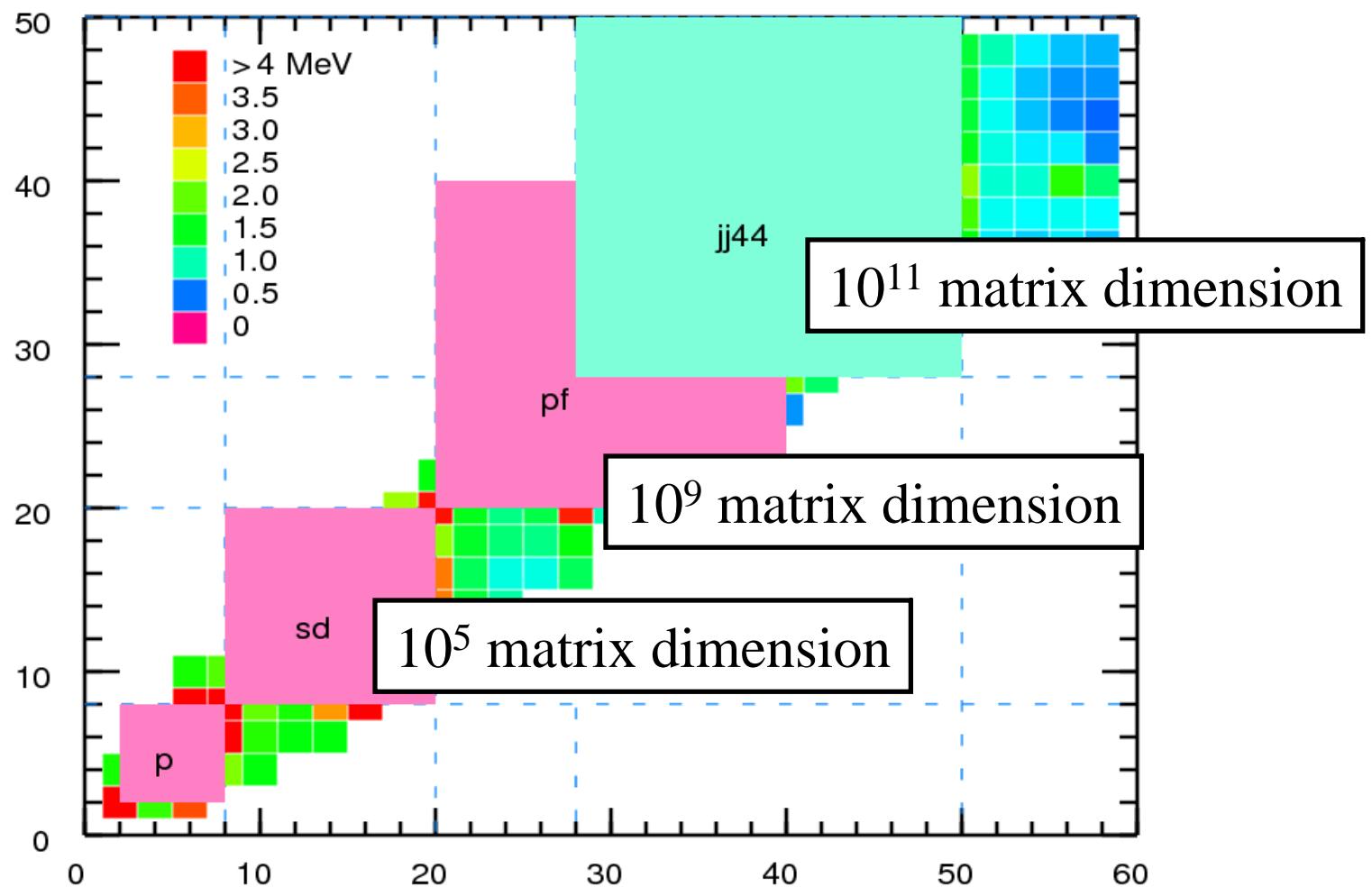


$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1.0000 \pm 0.0011.$$



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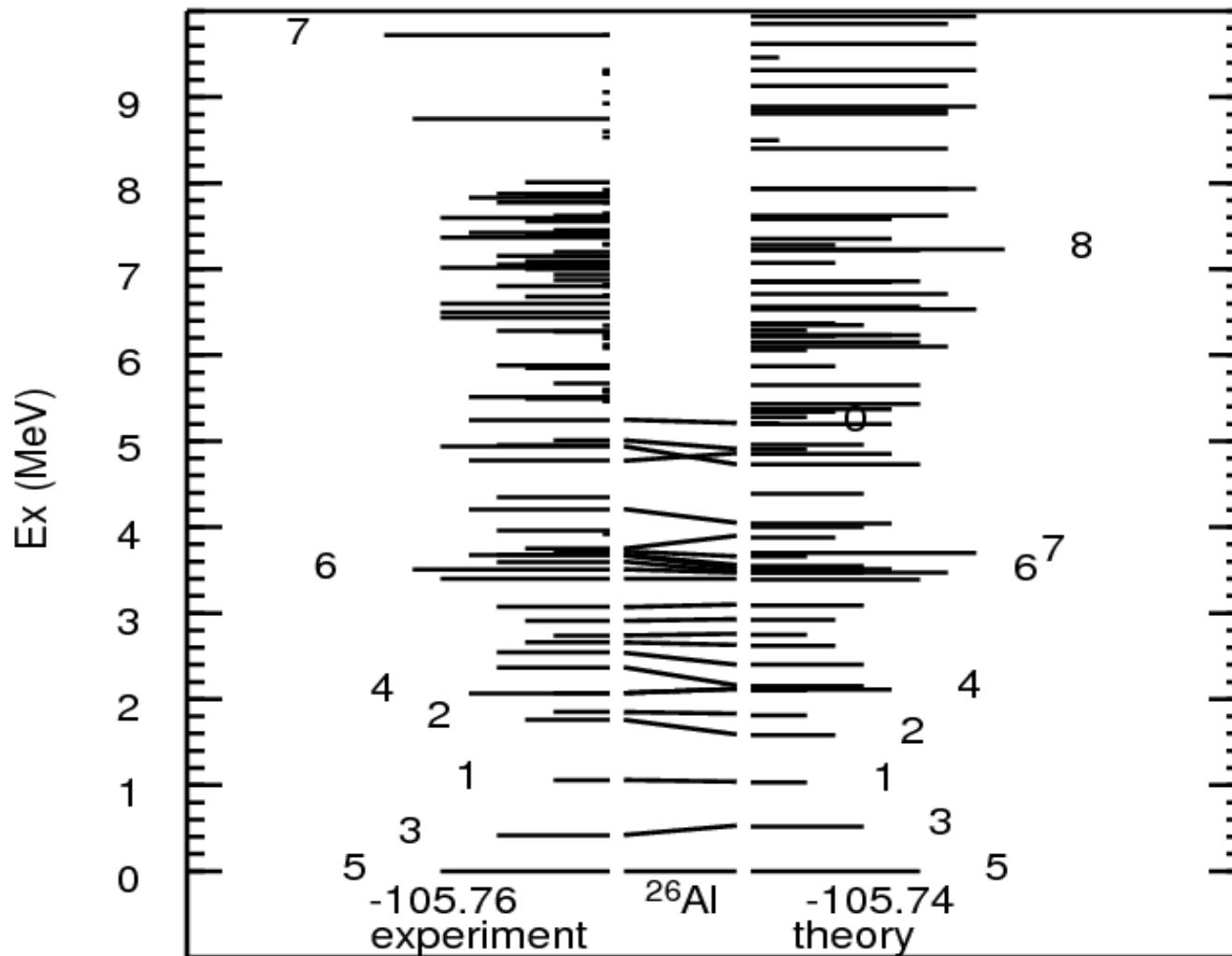
jj44 means $f_{5/2}$, $p_{3/2}$, $p_{1/2}$, $g_{9/2}$ orbits for protons and neutrons

A tour of the sd shell on the web

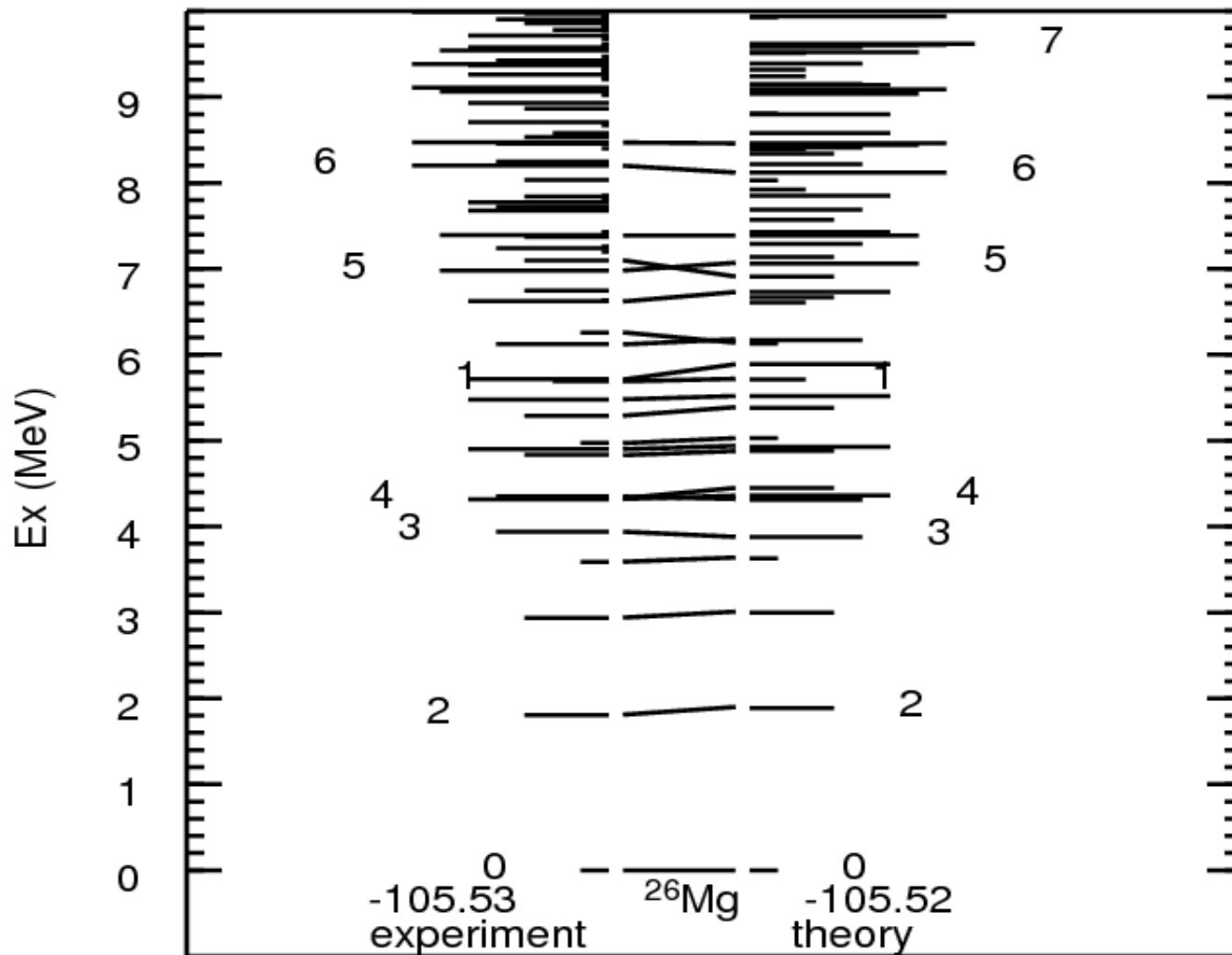


K																				38, 0	39, 1/2									
Ar																				36, 0	37, 1/2	38, 1								
Cl																				34, 0	35, 1/2	36, 1	37, 3/2							
S																				32, 0	33, 1/2	34, 1	35, 3/2	36, 2						
P																				30, 0	31, 1/2	32, 1	33, 3/2	34, 2	35, 5/2					
Si																				28, 0	29, 1/2	30, 1	31, 3/2	32, 2	33, 5/2	34, 3				
Al																				26, 0	27, 1/2	28, 1	29, 3/2	30, 2	31, 5/2	32, 3	33, 7/2			
Mg																				24, 0	25, 1/2	26, 1	27, 3/2	28, 2	29, 5/2	30, 3	31, 7/2	32, 4		
Na																				22, 0	23, 1/2	24, 1	25, 3/2	26, 2	27, 5/2	28, 3	29, 7/2	30, 4	31, 9/2	
Ne																				20, 0	21, 1/2	22, 1	23, 3/2	24, 2	25, 5/2	26, 3	27, 7/2	28, 4	29, 9/2	30, 5
F	18, 0	19, 1/2	20, 1	21, 3/2	22, 2	23, 5/2	24, 3	25, 7/2	26, 4	27, 9/2	28, 5	29, 11/2																		
O	17, 1/2	18, 1	19, 3/2	20, 2	21, 5/2	22, 3	23, 7/2	24, 4	25, 9/2	26, 5	27, 11/2	28, 6																		
	9	10	11	12	13	14	15	16	17	18	19	20																		

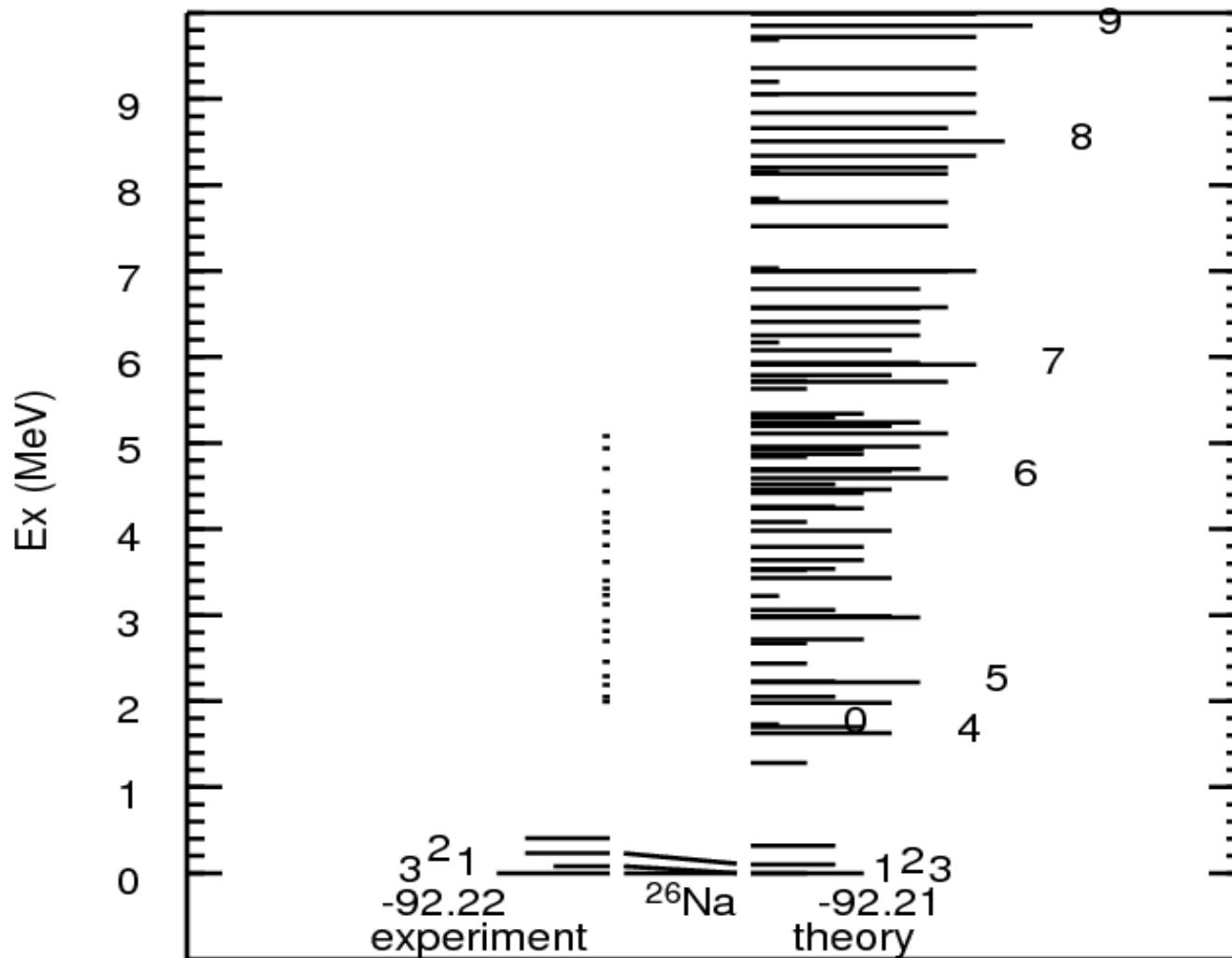
Positive parity states for ^{26}Al



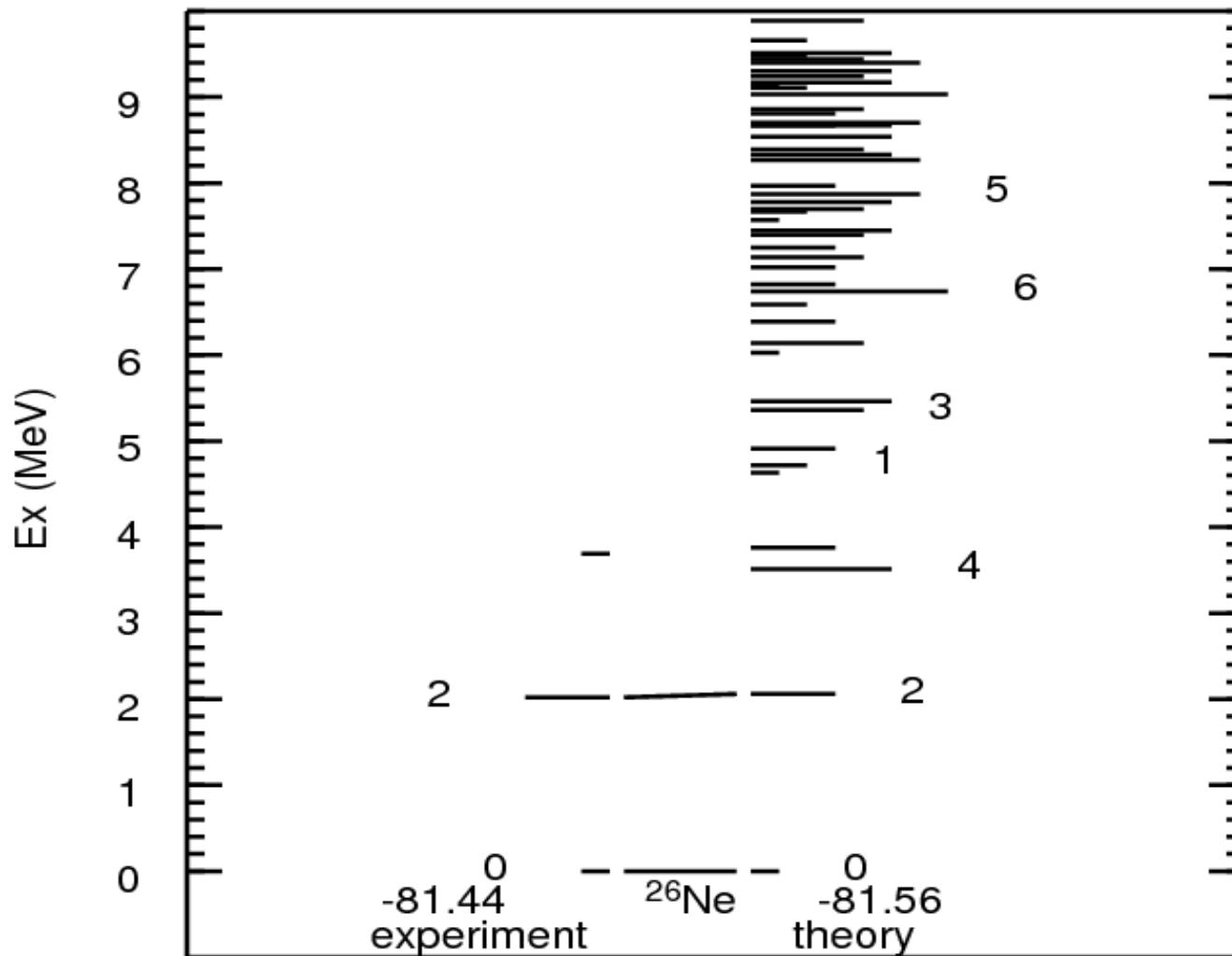
Positive parity states for ^{26}Mg



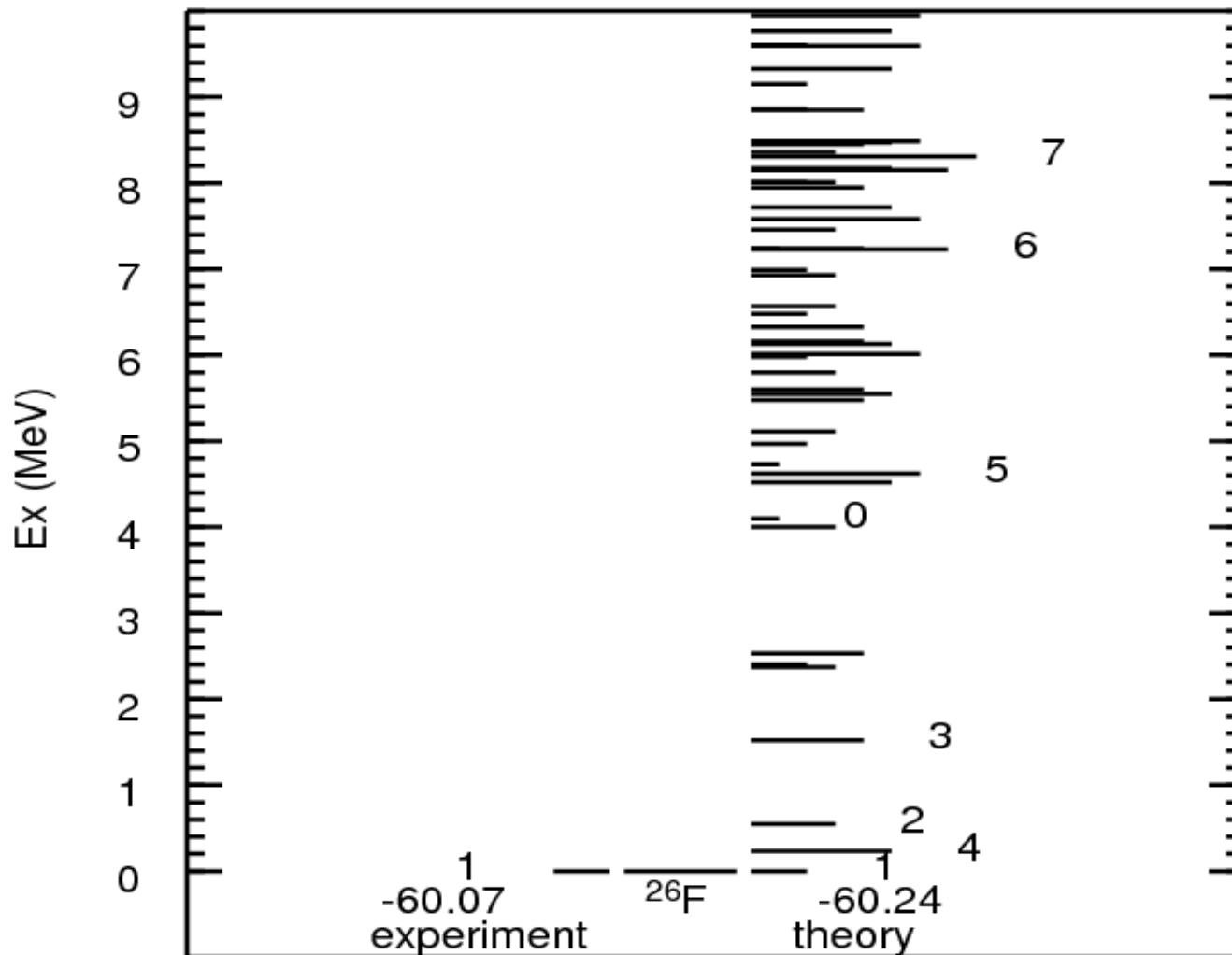
Positive parity states for ^{26}Na



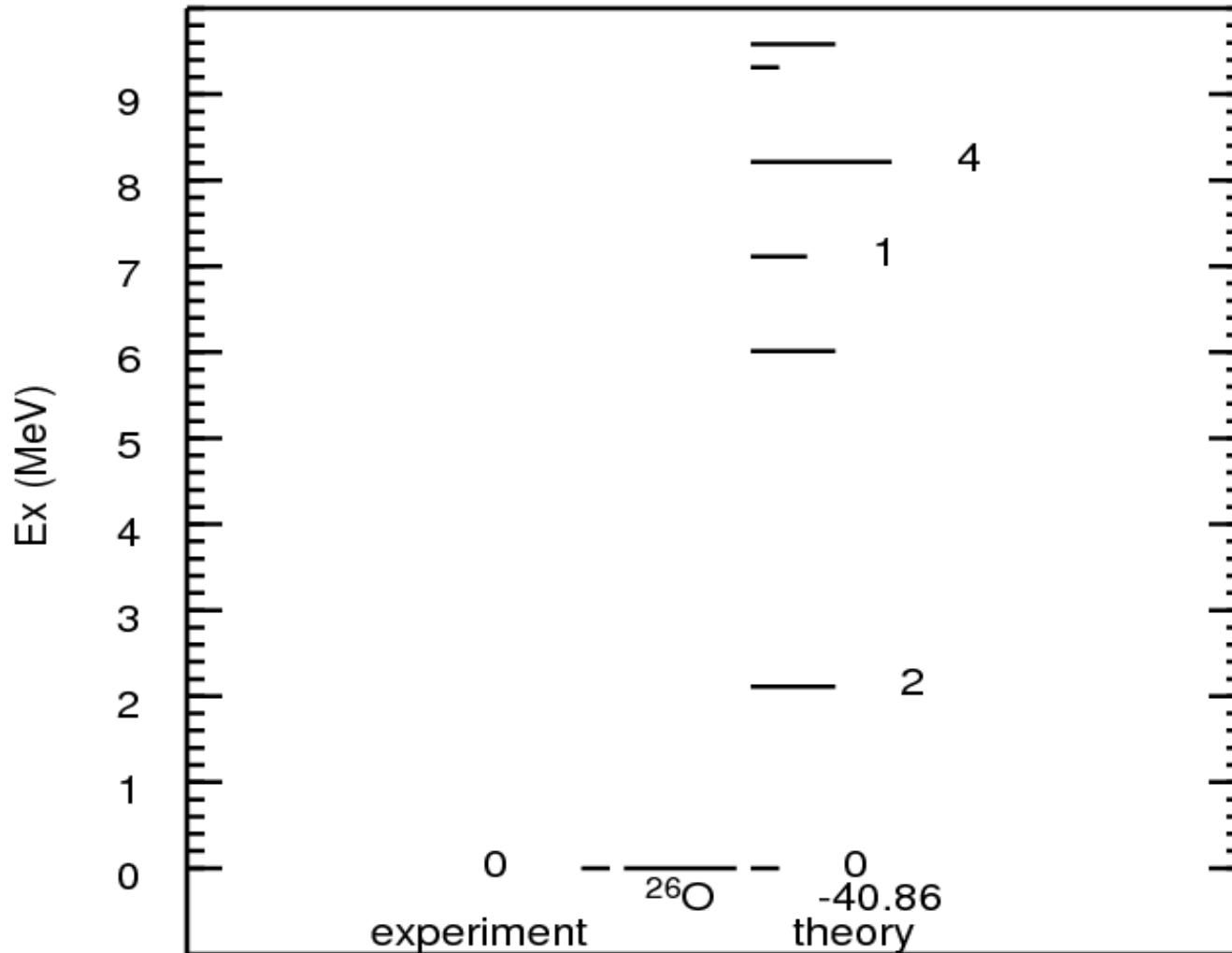
Positive parity states for ^{26}Ne



Positive parity states for ^{26}F



Positive parity states for ^{26}O

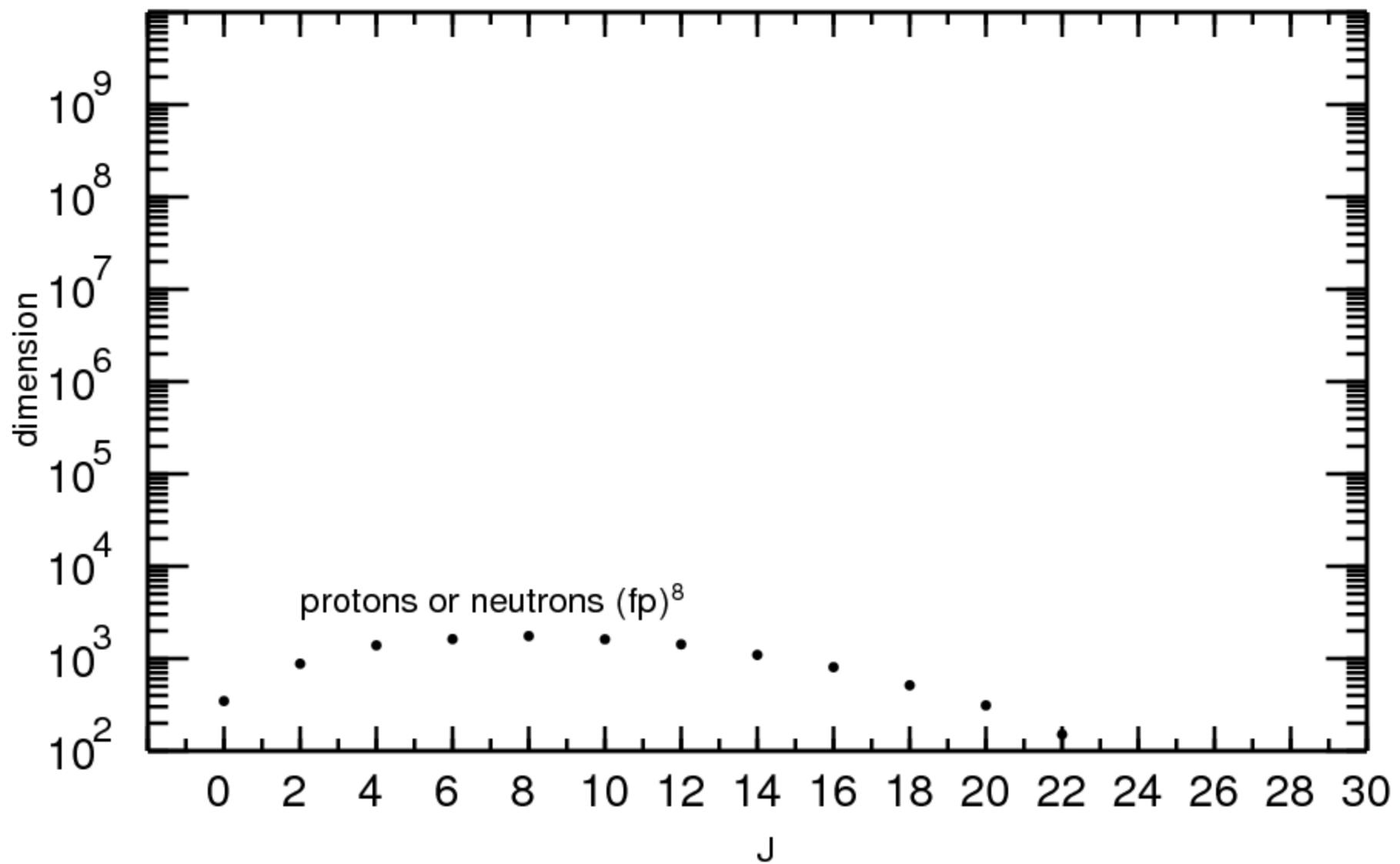


How to count basis dimensions

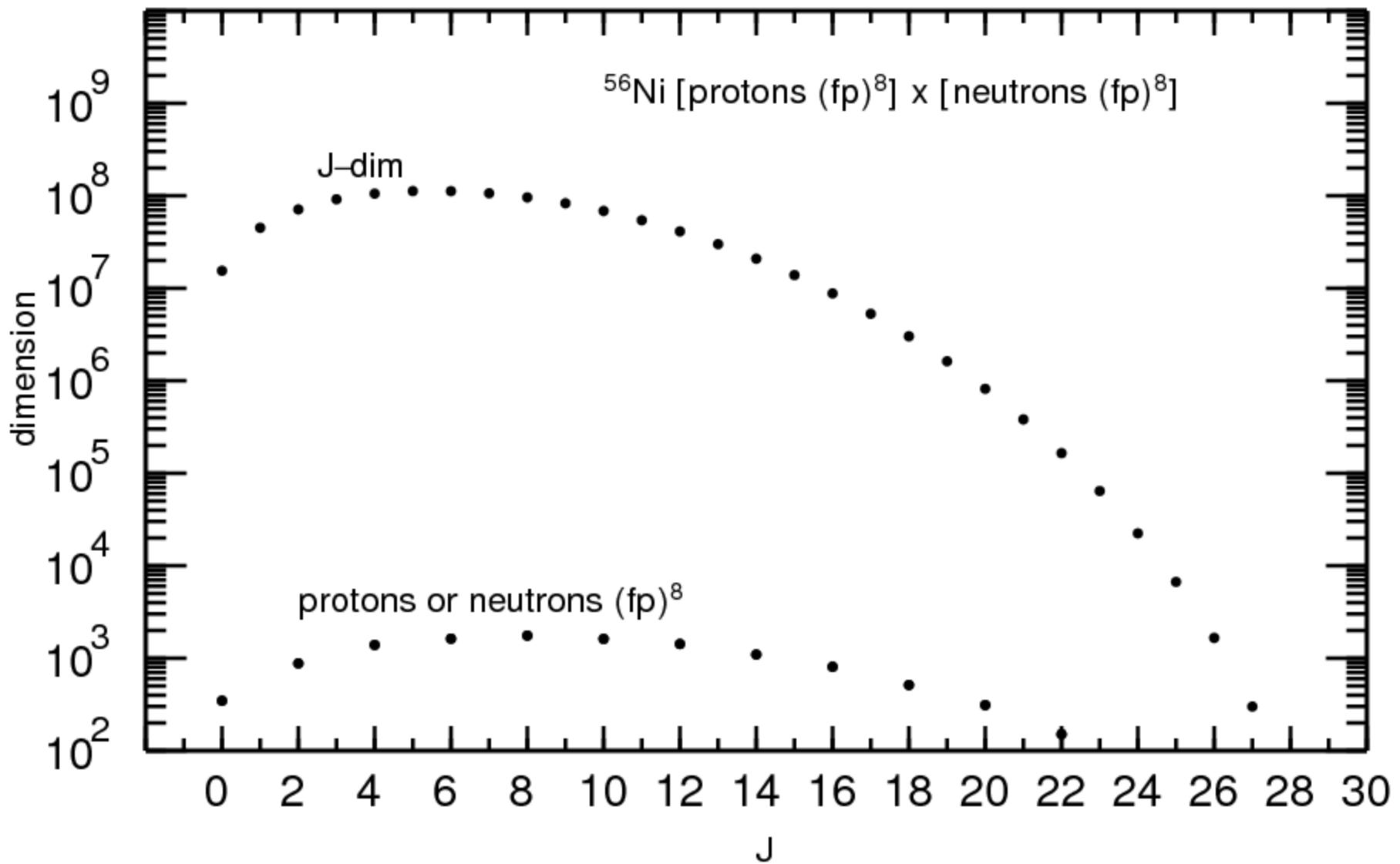
- Protons and neutrons – all of those allowed by the triangle conditions $[(J_p)] \times [(J_n)] J_{pn} D_{pn} = D_p D_n$
- Number of states for a given M-value – the sum of the J dimensions from J_{\max} down to $J = M$
- J-scheme – basis has good J (or JT)
- M-scheme – basis does not have good J – only M is fixed but the eigenstates will have good J since H is rotationally invariant.



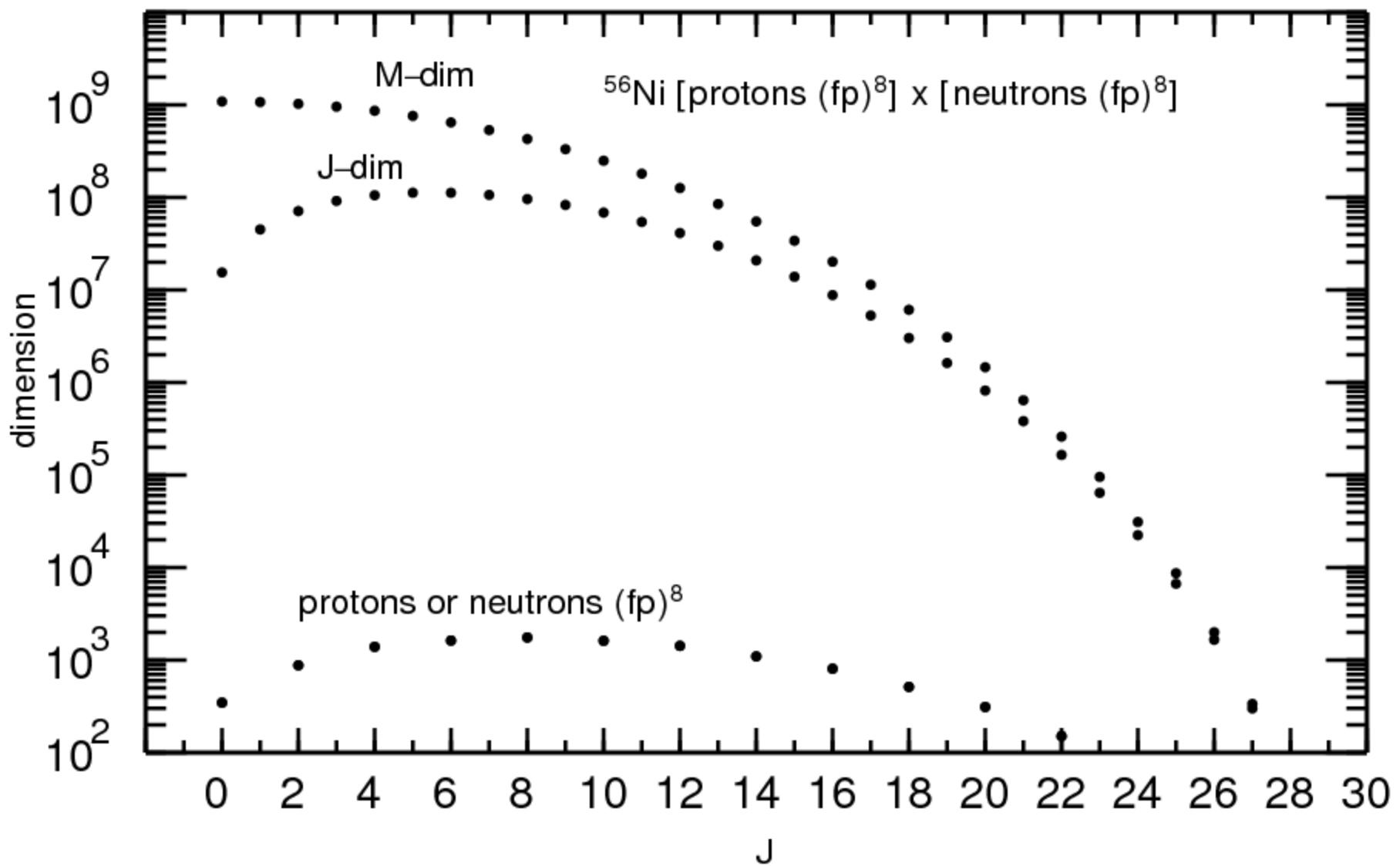
Example for ^{48}Ca in the pf shell



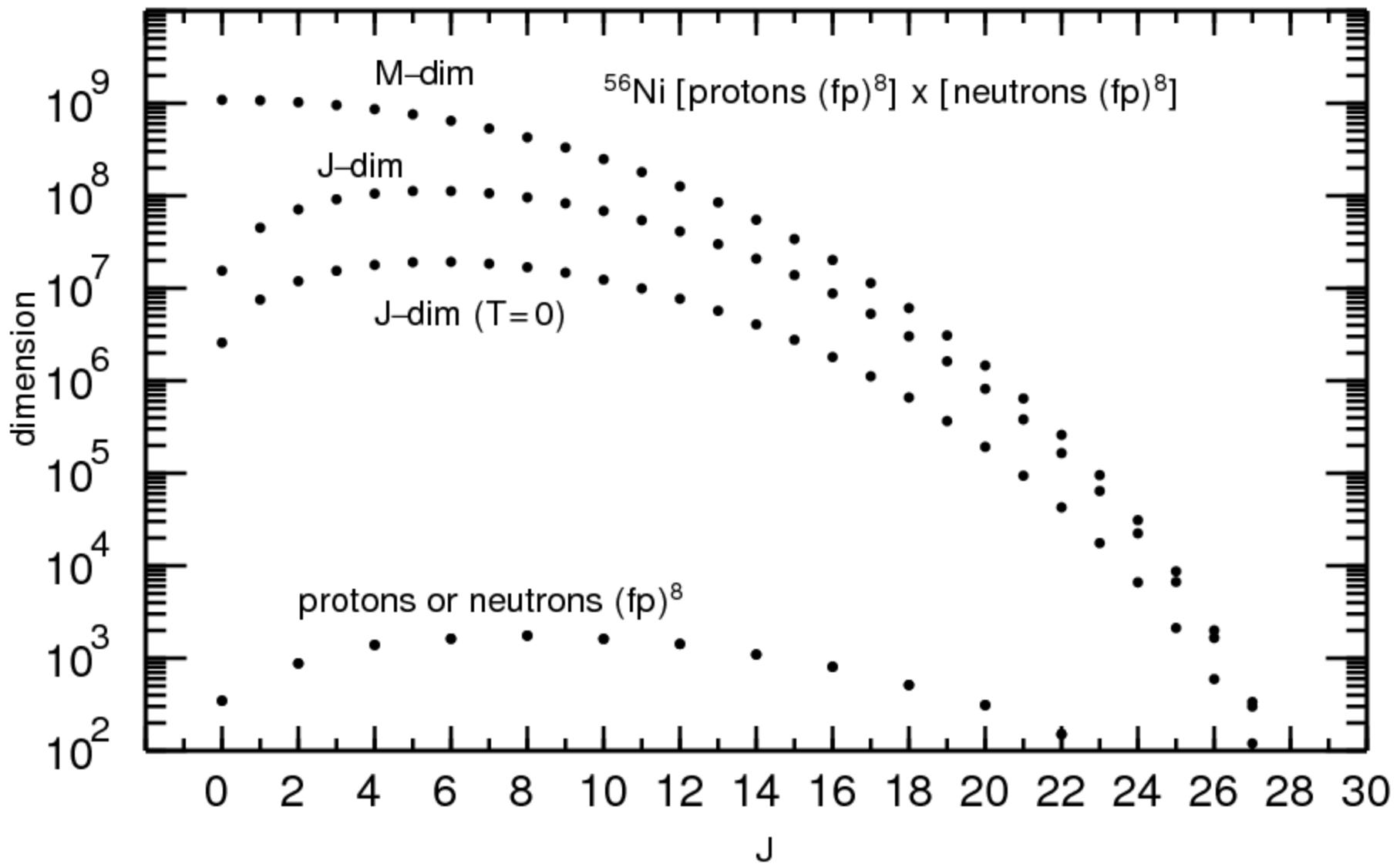
Example for ^{56}Ni in the pf shell



Example for ^{56}Ni in the pf shell



Example for ^{56}Ni in the pf shell



Codes

- M-scheme (matrix not stored) ($\sim 10^{10}$ M-states)
 - Antoine (Caurier)
 - Redstick (Ormand and Johnson)
 - CMUShell (Horoi)
 - Mshell (Mizuzaki)
 - MFDn (Vary et al)
- JT-projected M-scheme (matrix stored) ($\sim 10^5$ JT-states)
 - Oxbash (Brown and Rae) (now replaced by NuShell@MSU)
 - NuShell (Rae)
 - NuShell@MSU (Brown and Rae) (NuShell with Oxbash style input and output)
- J-scheme (matrix not stored) ($\sim 10^8$ J-states)
 - Nathan (Caurier)
 - EICODE (Toivanen)
 - NuShellx (Rae)
 - NuShellx@MSU (Brown and Rae) (NuShellx with Oxbash style input and output)

available on the web



Bill Rae (Garsington) has made big advances
Oxbash -> Nushell -> Nushellx

Nushellx uses the [Jp Jn] J coupling to eliminate storage of the matrix.

Similar to Nathan (Caurier et al) and Eicode (Toivanen) but faster.

NuShellx@MSU uses these codes as a core for nuclear structure applications.

The screenshot shows the homepage of the NuShell website. The header features a blue background with white text: "Nuclear Shell Model Codes" and "Home of NuShell, NuShellX and SunShell". To the left is a circular logo containing a stylized sun or moon. To the right is a circular inset image showing a row of computer monitors in a laboratory setting. The main content area has a white background. On the left, there's a vertical navigation bar with three items: "Home" (highlighted in green), "About Us", and "Download". The main text area contains two paragraphs: "Home Page of NuShell, NuShellX and SunShell." and "NuShell is possibly one of the easiest shell model codes to use!".

NuShellX - NuShell's Big Brother

The faster, easy choice for large scale shell model calculations !



B. Alex Brown, USNDP, BNL, Nov 6, 2008



Effective interactions – what are the two-body matrix elements?

For sd shell USD, USDA, USDB interactions obtained from a fit to data
use singular-value-decomposition method to obtain values
for 20-30 of the most important linear combinations of TBME
from about 600 energies

For pf same procedure for about 600 energies

M. Honma, T. Otsuka, B. A. Brown and T. Mizusaki,
Phys. Rev. C65, 061301 (2002) - GPFX1, GPFX1A

For heavier nuclei this method becomes unfeasible – we need better
methods for understanding the nuclear medium and model space
dependence of the NN and NNN interactions
(tomorrow) talk at Stony Brook on ^{132}Sn and ^{208}Pb regions

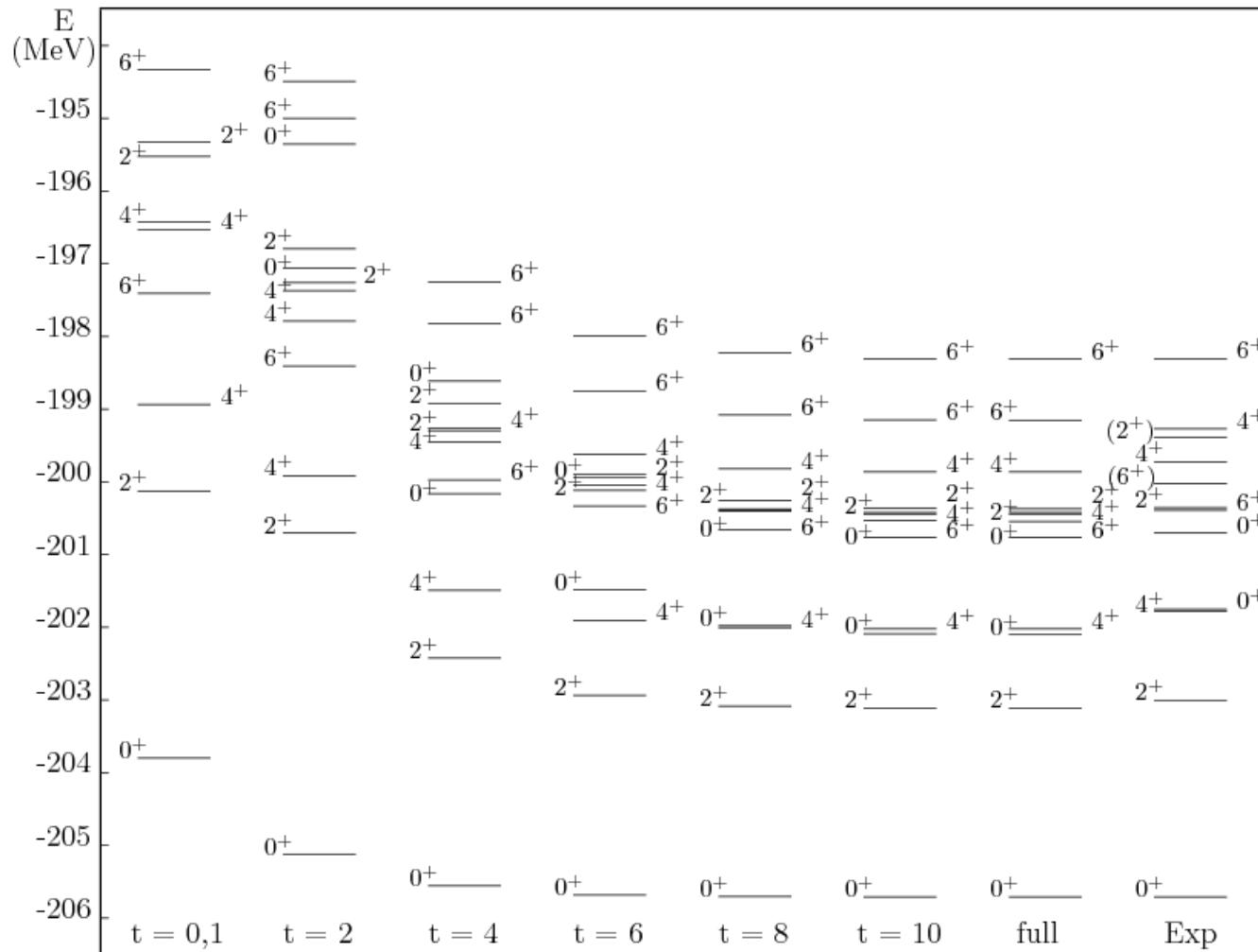


B. Alex Brown, USNDP, BNL, Nov 6, 2008



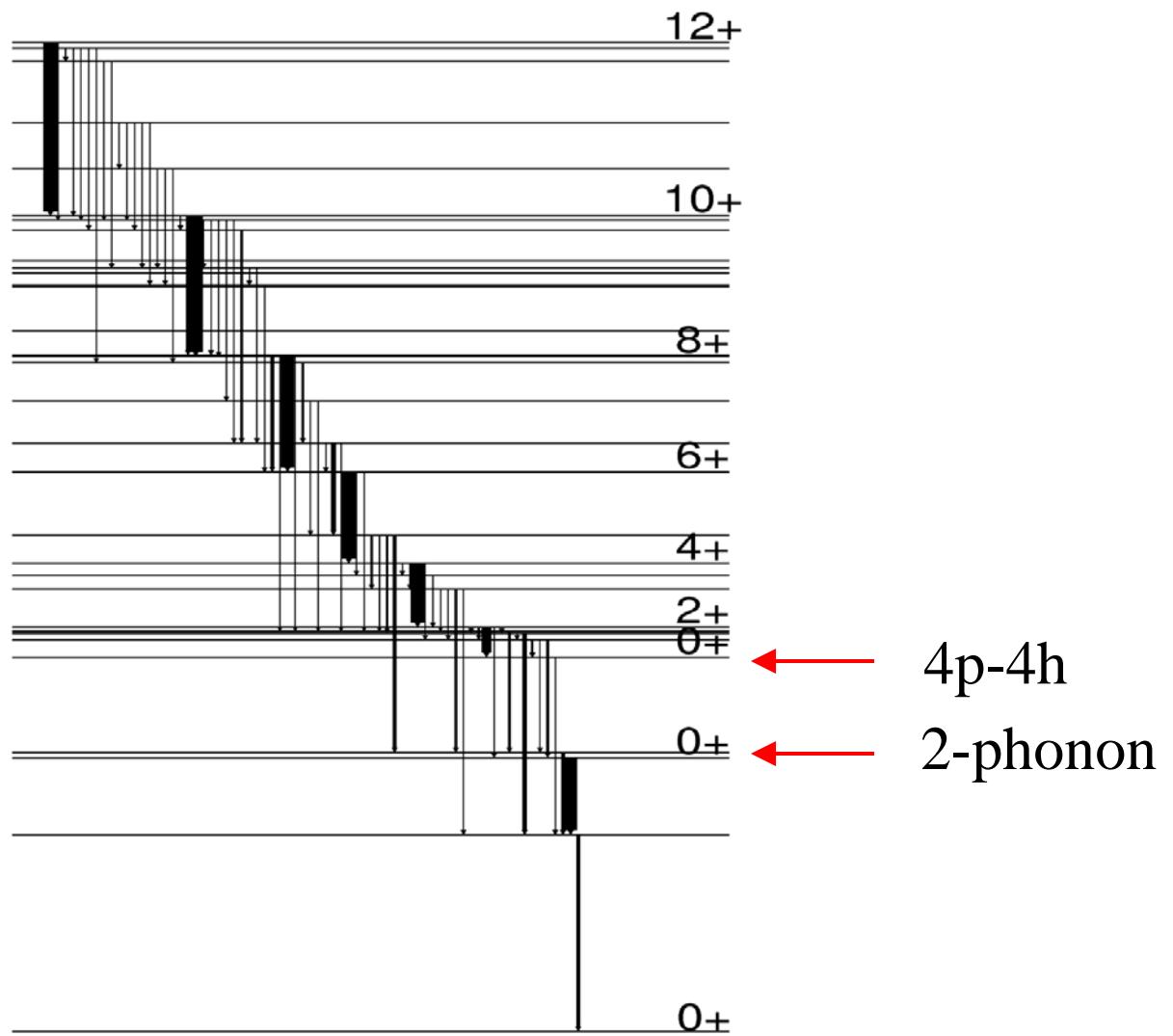
Full pf space for ^{56}Ni with GXPF1A Hamiltonian (order of one day computing time)

M. Horoi, B. A. Brown, T. Otsuka, M. Honma and T. Mizusaki, Phys. Rev. C 73, 061305(R) (2006).

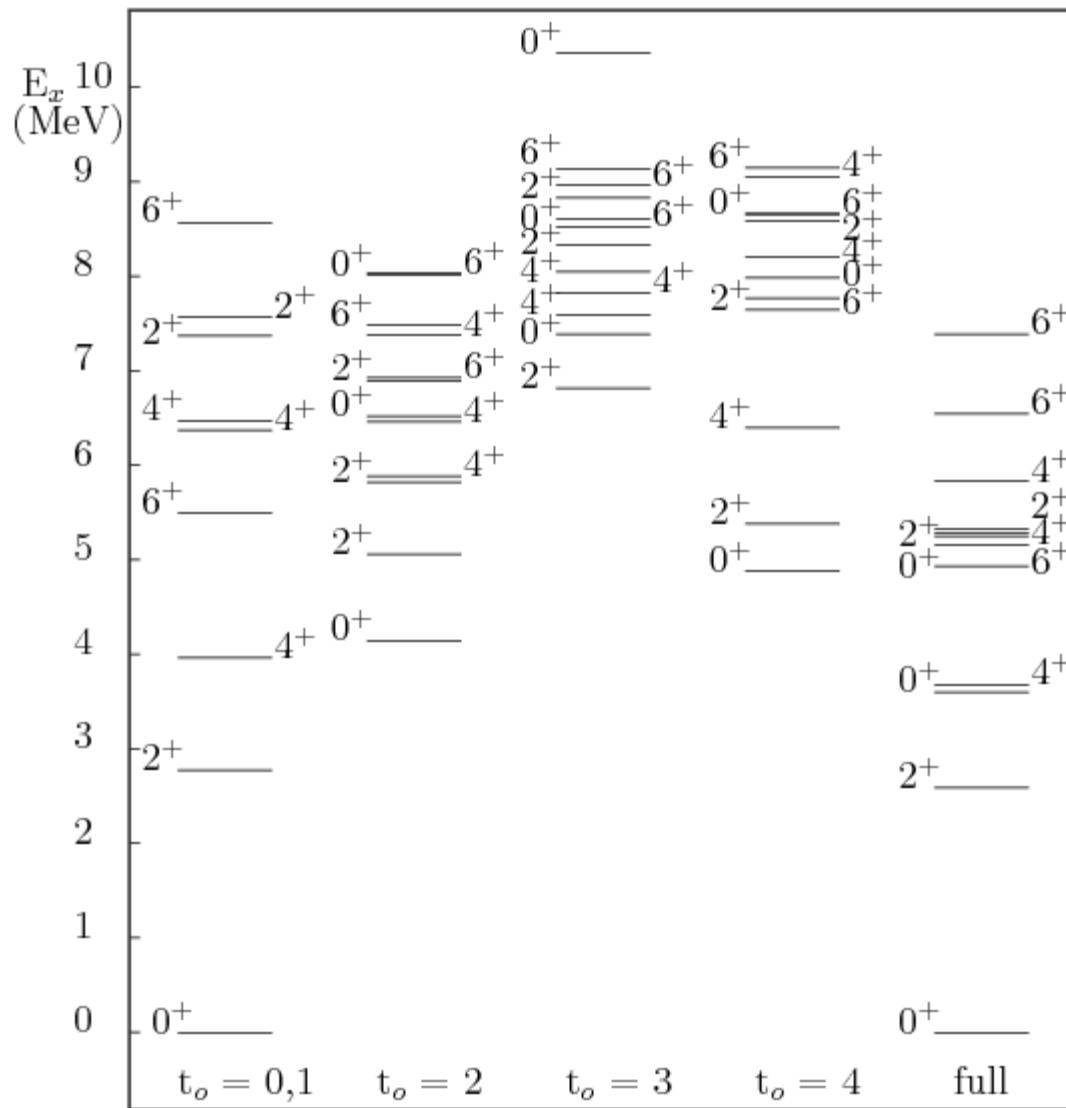


Dimension 25 1353 497805 25×10^6 255×10^6 771×10^6 1.09×10^9

B. A. BROWN, T. OTSUKA, M. HONMA, T. MIZUSAKI, 2008



Pure configurations



Requires an effective shell gap 0.9 MeV smaller than full fp

B. Alex Brown, USNDP, BNL, Nov 6, 2008





PHYSICAL REVIEW C

VOLUME 10, NUMBER 5

NOVEMBER 1974

Levels of $^{56}\text{Ni}^\dagger$

H. Nann* and W. Benenson

Cyclotron Laboratory and Department of Physics, Michigan State University, East Lansing, Michigan 48824

(Received 5 August 1974)

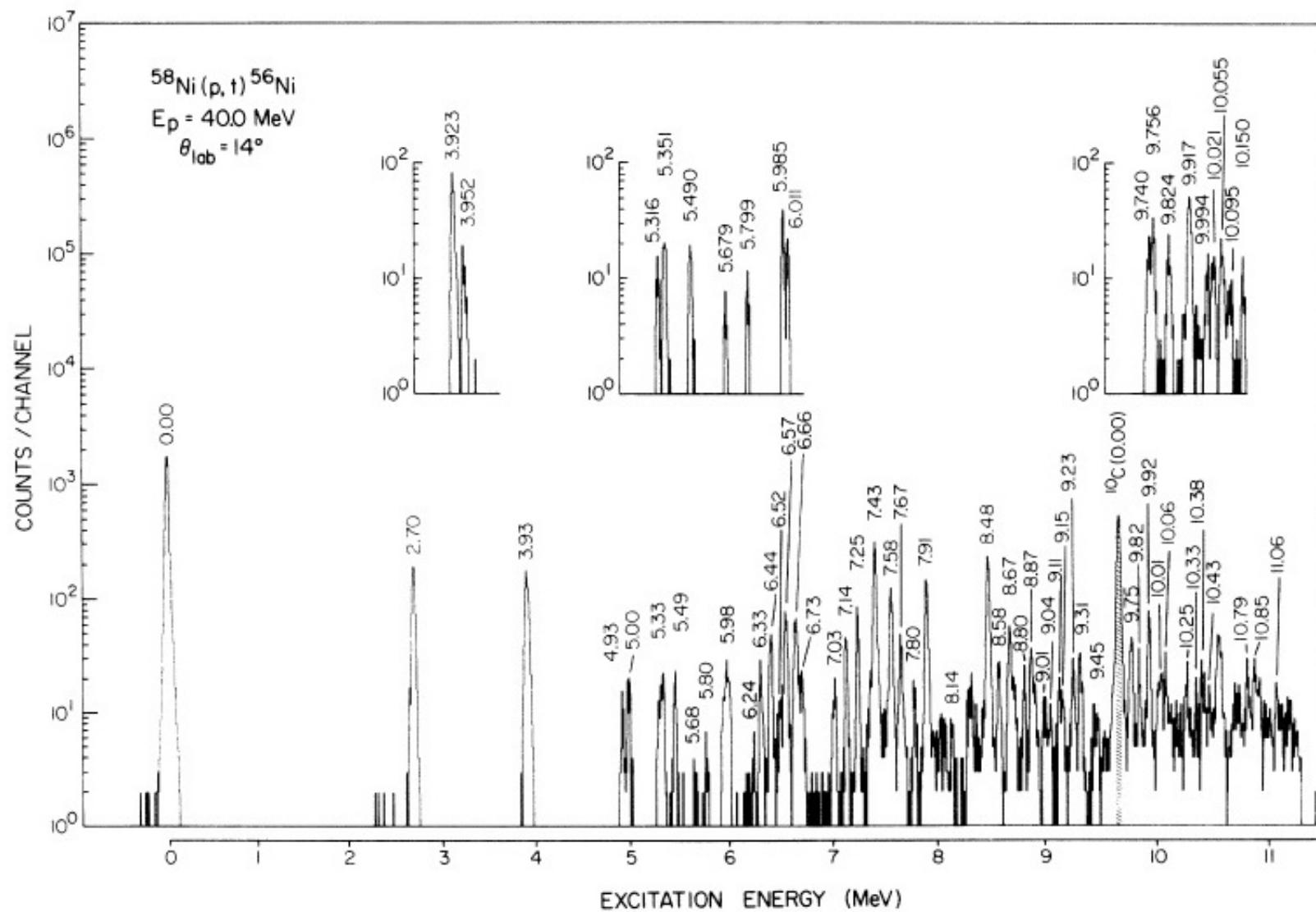
The $^{58}\text{Ni}(p, t)^{56}\text{Ni}$ reaction was studied at 40 and 45 MeV beam energy. An energy resolution of 10–25 keV permitted observation of 60 levels with excitation energy up to 10.5 MeV. Spin and parity are assigned to levels which were excited with characteristic angular distributions. These include 0^+ states at 3.95, 5.00, 6.44, 7.91, 9.92, 9.99, and 10.02 MeV.

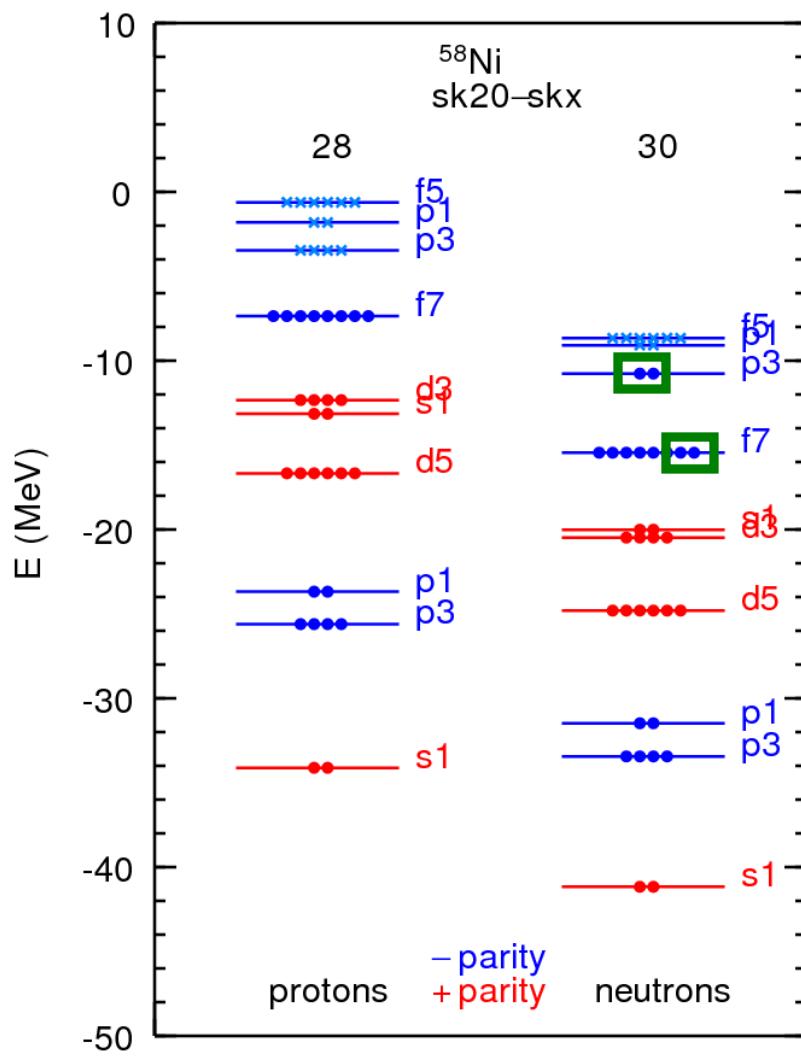


B. Alex Brown, USNDP, BNL, Nov 6, 2008



60 levels 10 keV resolution





B. Alex Brown, USNDP, BNL, Nov 6, 2008





Pairing vibrations expect three 0^+ levels with $T=0,1,2$
strength 2:3:1 and spacing that goes as $T(T+1)$

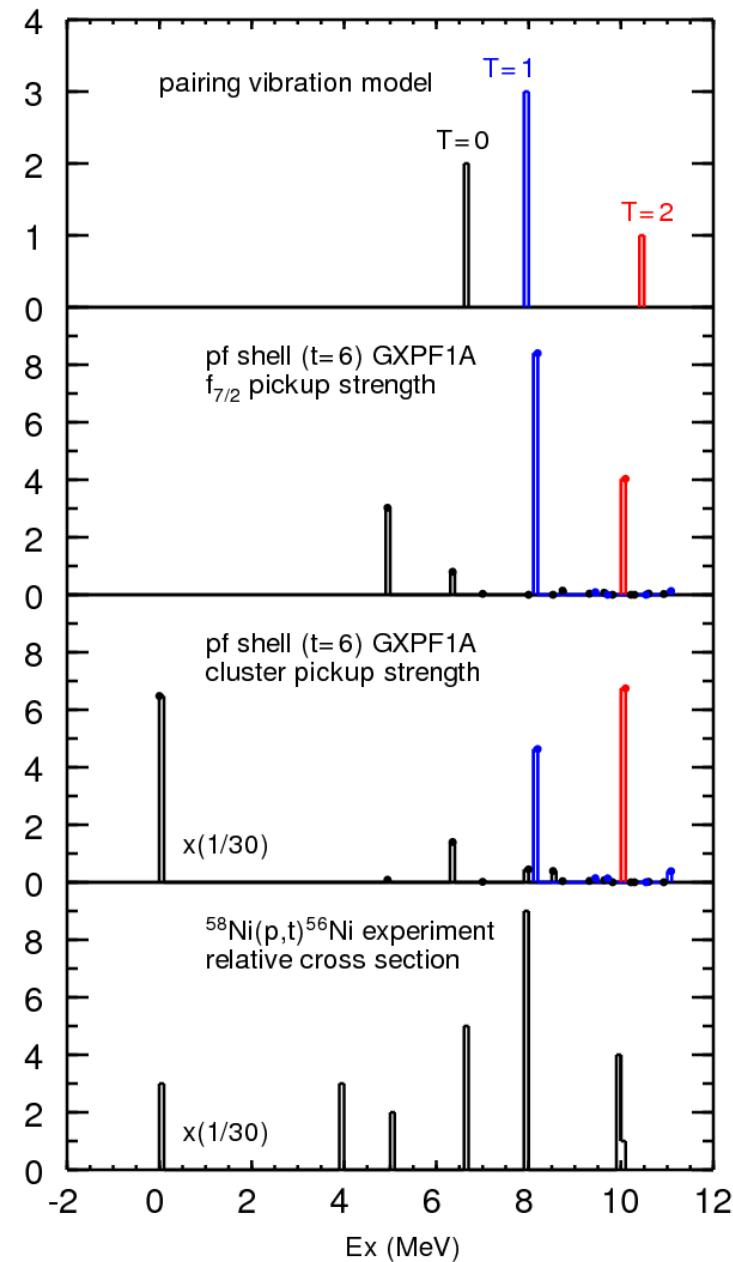
¹³A. Bohr, in *International Symposium on Nuclear Structure, Dubna, 1968* (IAEA, Vienna, 1968), p. 179.

¹⁴O. Nathan, in *International Symposium on Nuclear Structure, Dubna, 1968* (see Ref. 13), p. 191.



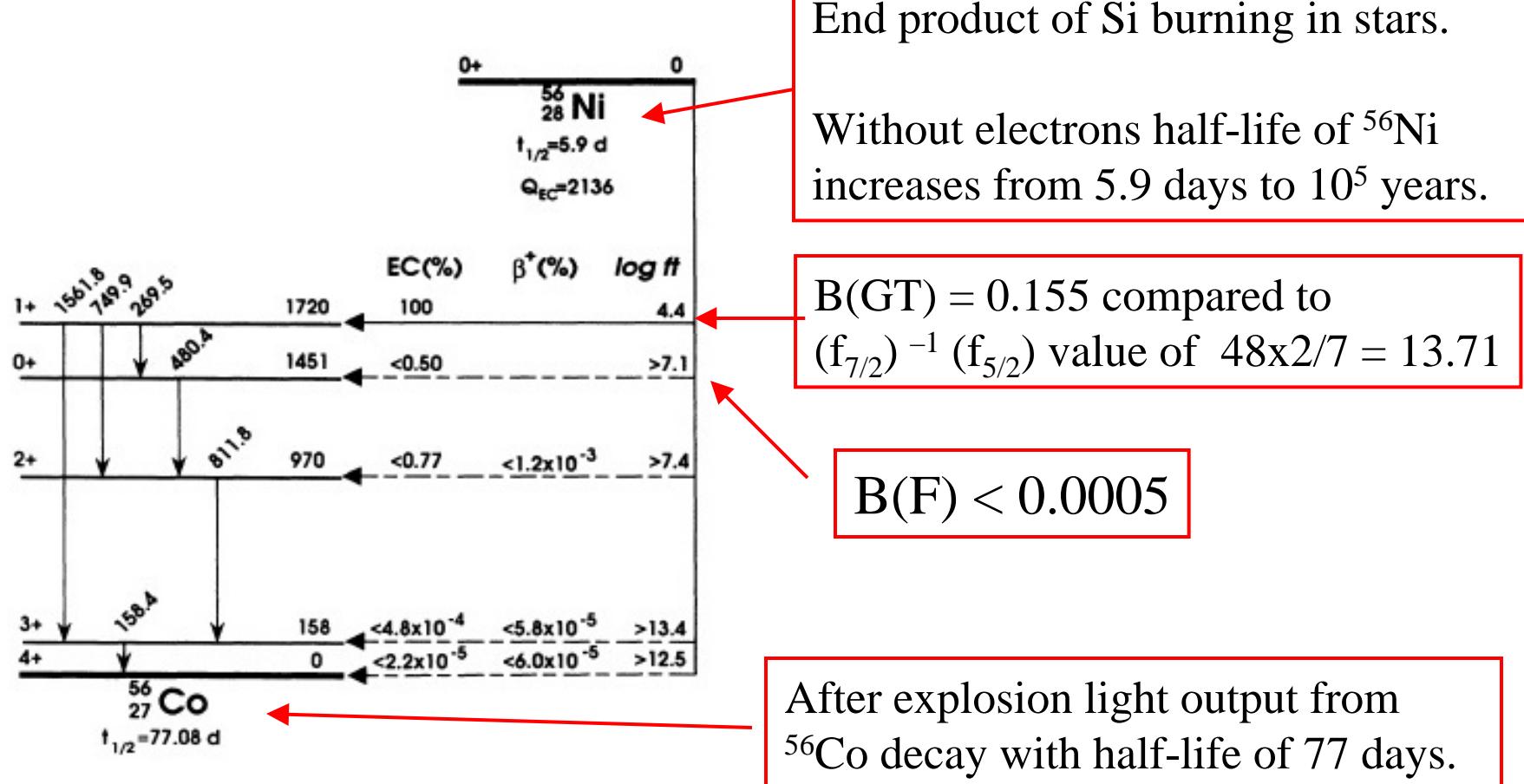
$^{58}\text{Ni}(\text{p},\text{t})^{56}\text{Ni}$

Relative strength
For 0^+ states in ^{56}Ni



Reinvestigation of ^{56}Ni decay

Bhaskar Sur, Eric B. Norman, K. T. Lesko, Edgardo Browne, and Ruth-Mary Larimer
Nuclear Science Division, Lawrence Berkeley Laboratory, 1 Cyclotron Road, Berkeley, California 94720



STELLAR WEAK INTERACTION RATES¹ FOR INTERMEDIATE-MASS NUCLEI. II. $A=21$ TO $A=60$

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W. K. Kellogg Radiation Laboratory, California Institute of Technology

AND

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Applied Theoretical Physics Division, Los Alamos National Laboratory, University of California, Los Alamos
Received 1981 June 12; accepted 1981 August 3

THE ASTROPHYSICAL JOURNAL, 252:715–740, 1982 January 15

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ELECTRON CAPTURE AND β -DECAY IN PRESUPERNOVA STARS

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Physics Department, California Institute of Technology

Received 1989 September 25; accepted 1990 April 2

THE ASTROPHYSICAL JOURNAL, 362:241–250, 1990

RATE TABLES FOR THE WEAK PROCESSES OF pf -SHELL NUCLEI
IN STELLAR ENVIRONMENTS

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Institut for Fysik og Astronomi, Århus Universitet, DK-8000 Århus C, Denmark

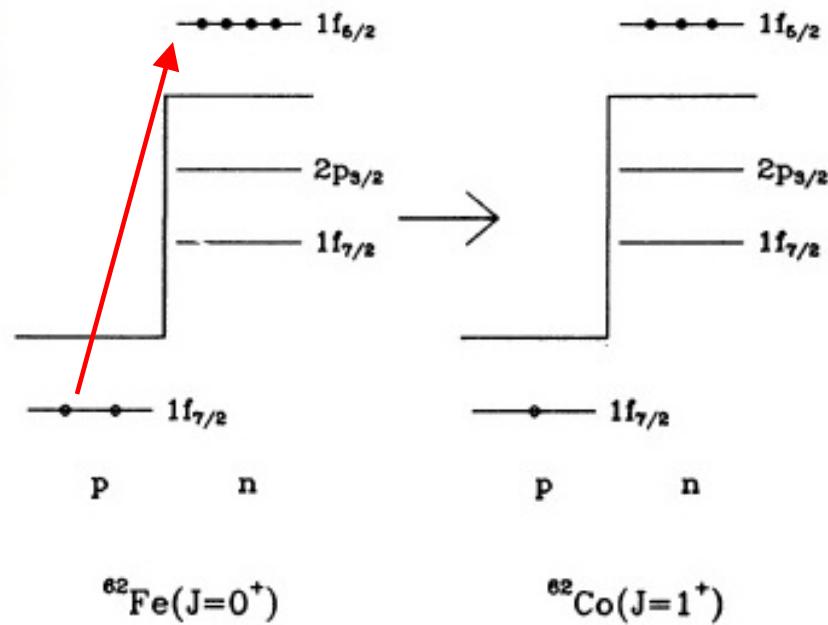
Atomic Data and Nuclear Data Tables 79, 1–46 (2001)

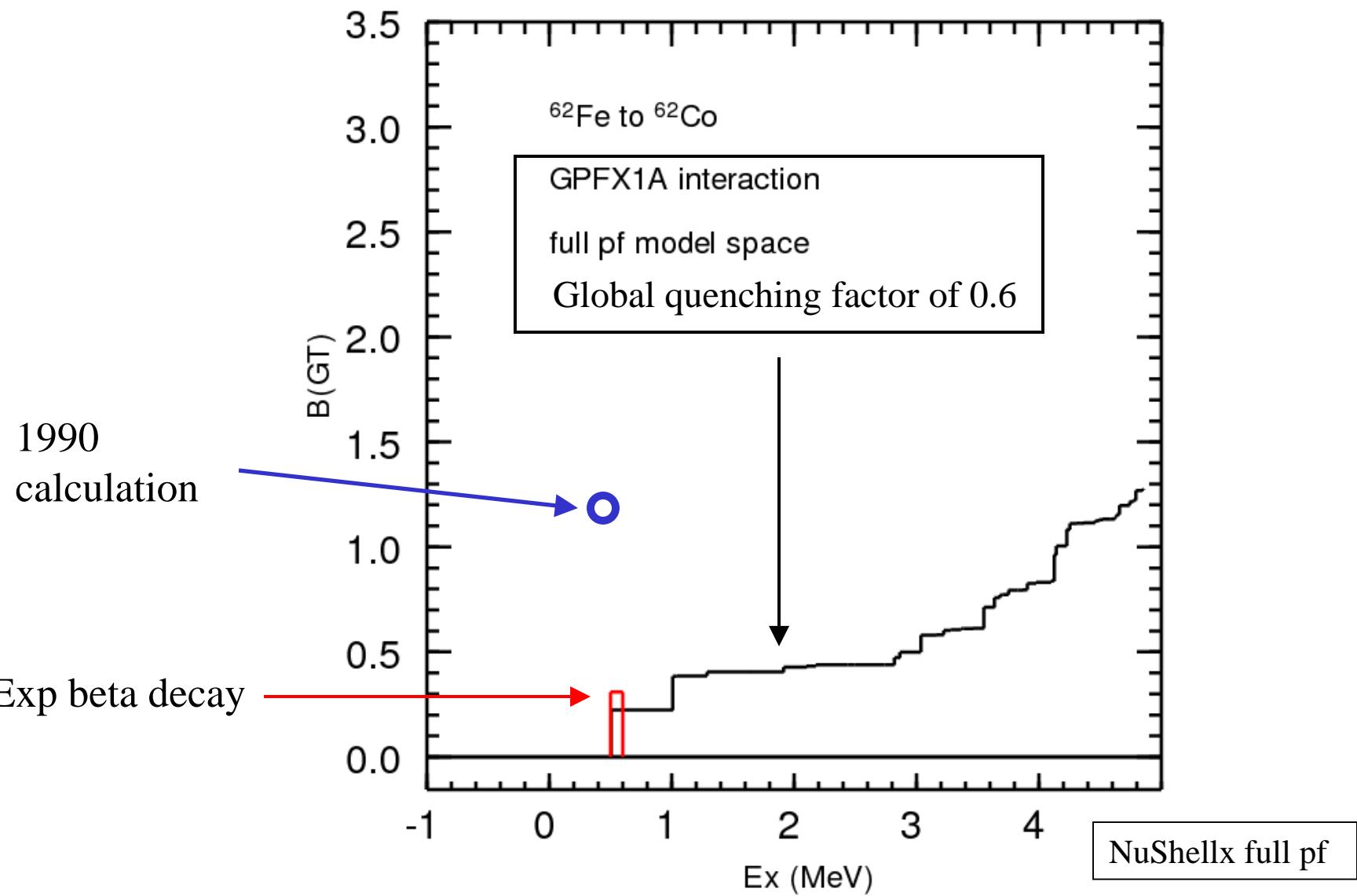


B. Alex Brown, USNDP, BNL, Nov 6, 2008



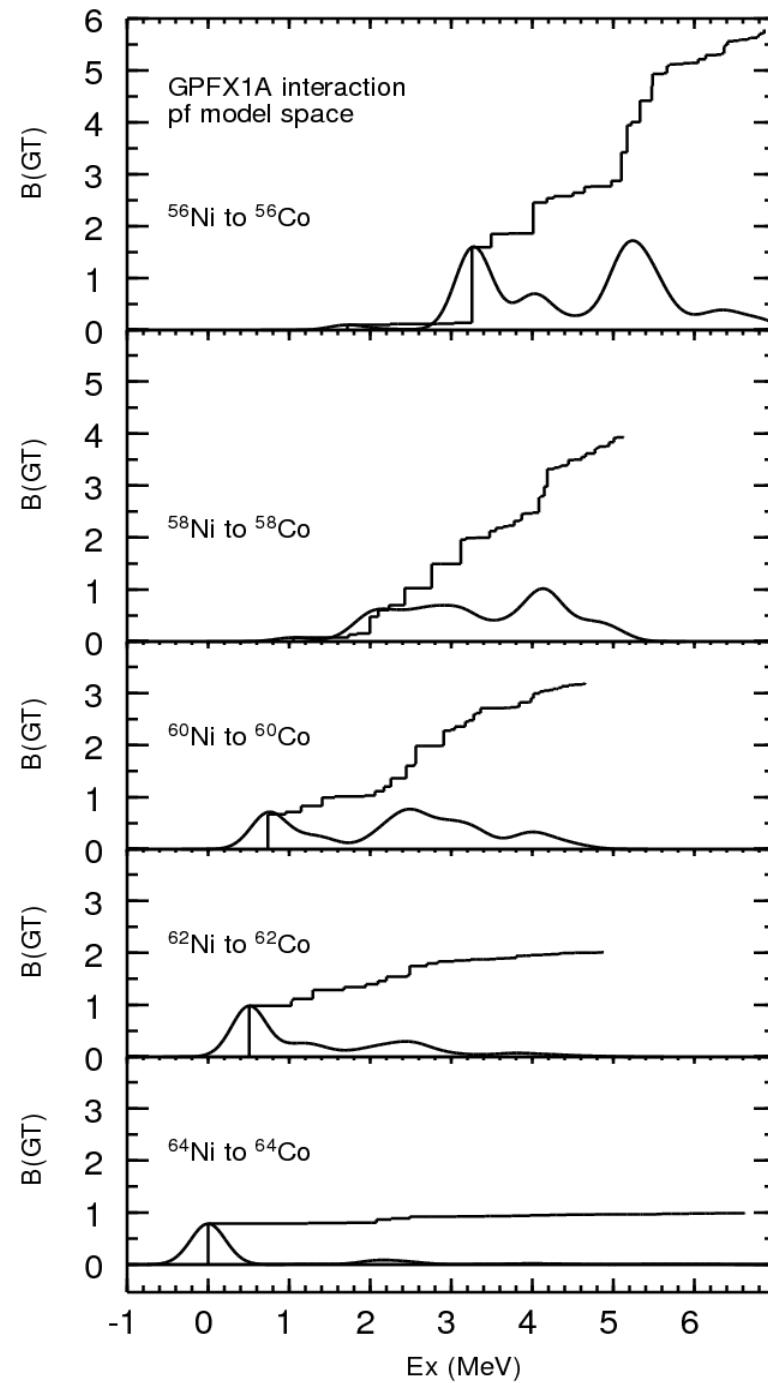
^{62}Fe to ^{62}Co model from Aufderheide et al. 1990





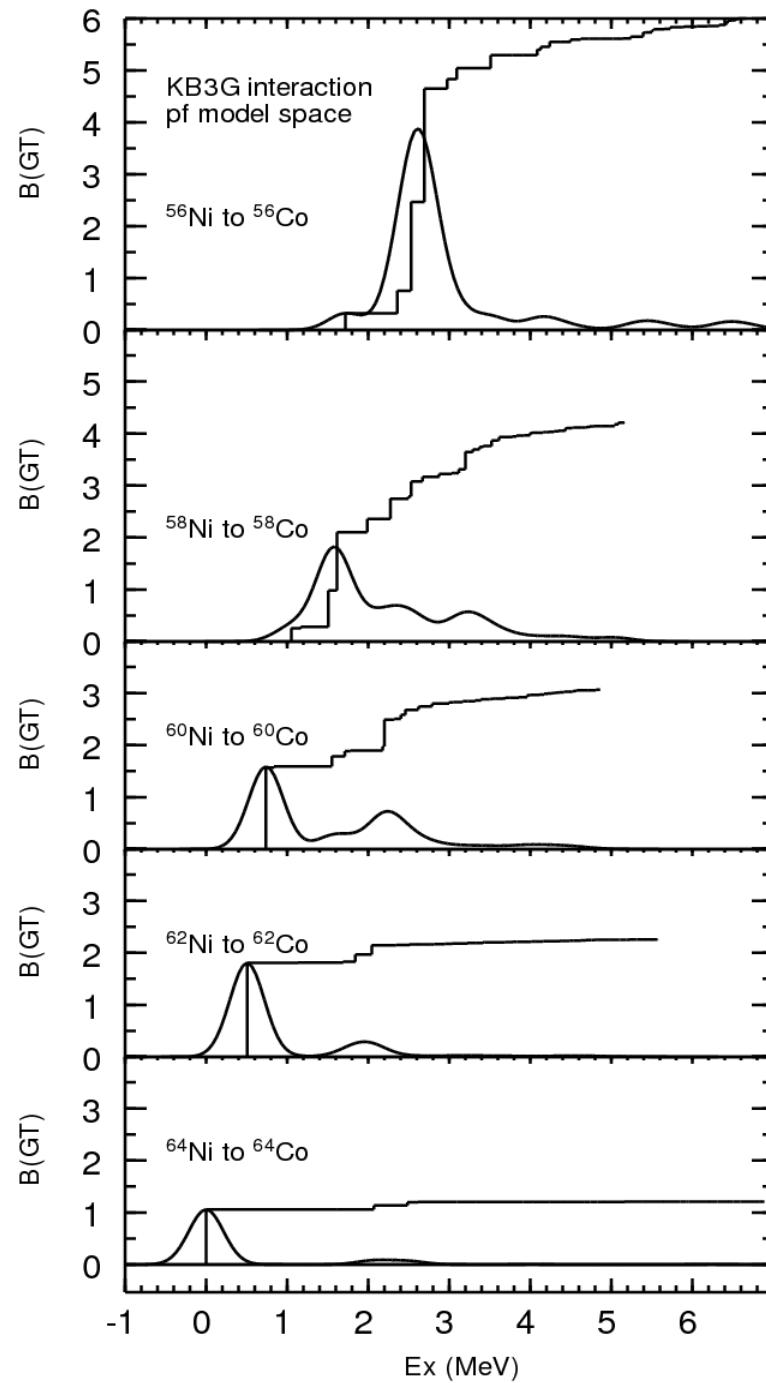
B. Alex Brown, USNDP, BNL, Nov 6, 2008





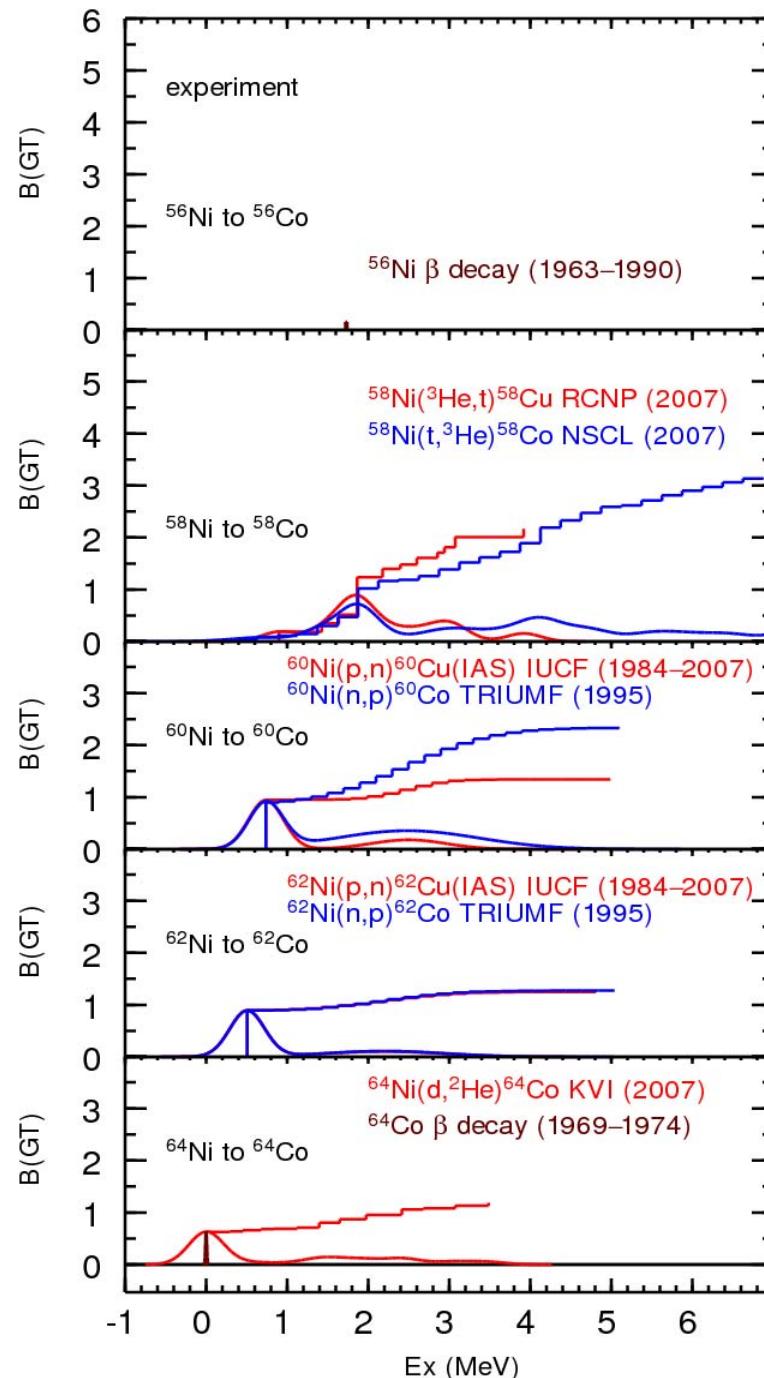
NuShellx t=6

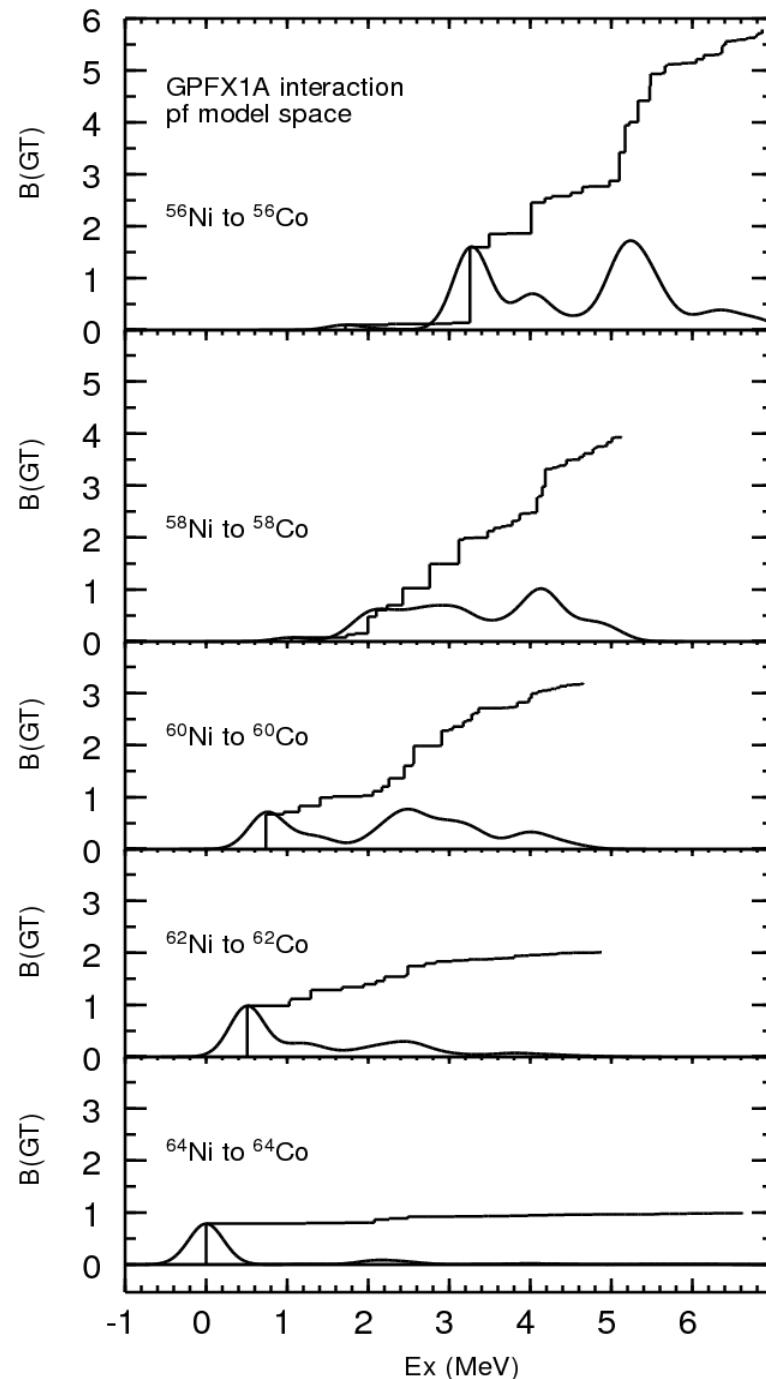
γ n, USNDP, BNL, Nov 6, 2008



NuShellx t=6

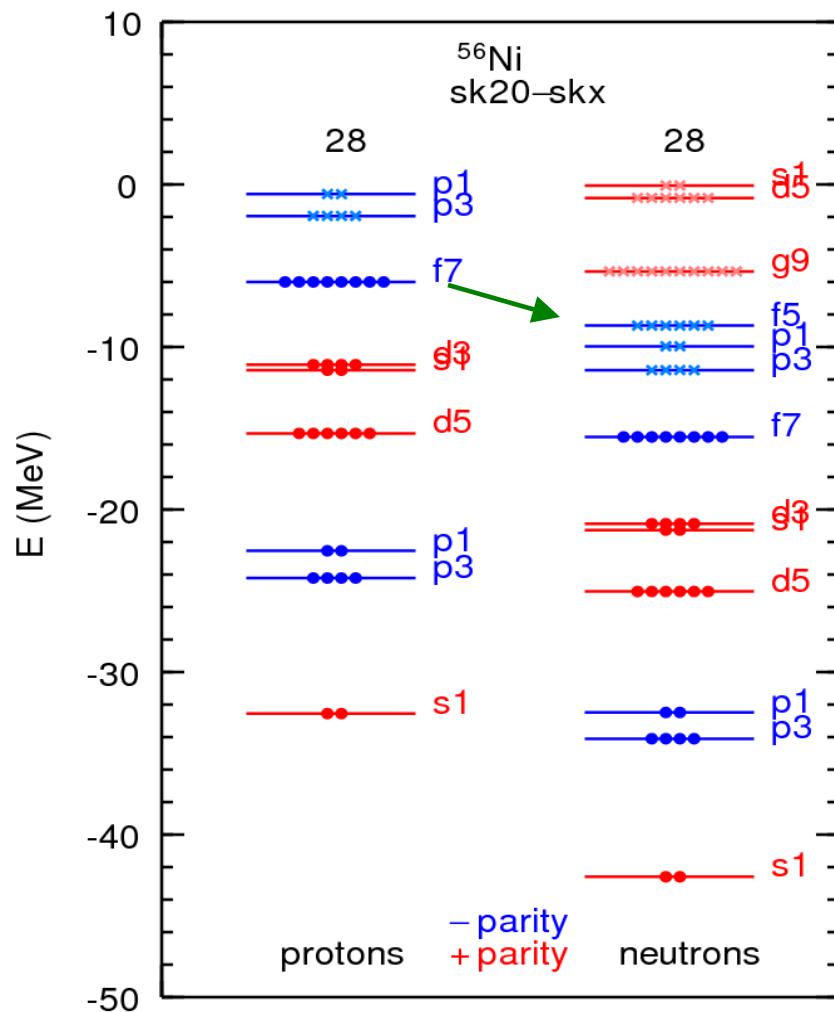
γ n, USNDP, BNL, Nov 6, 2008

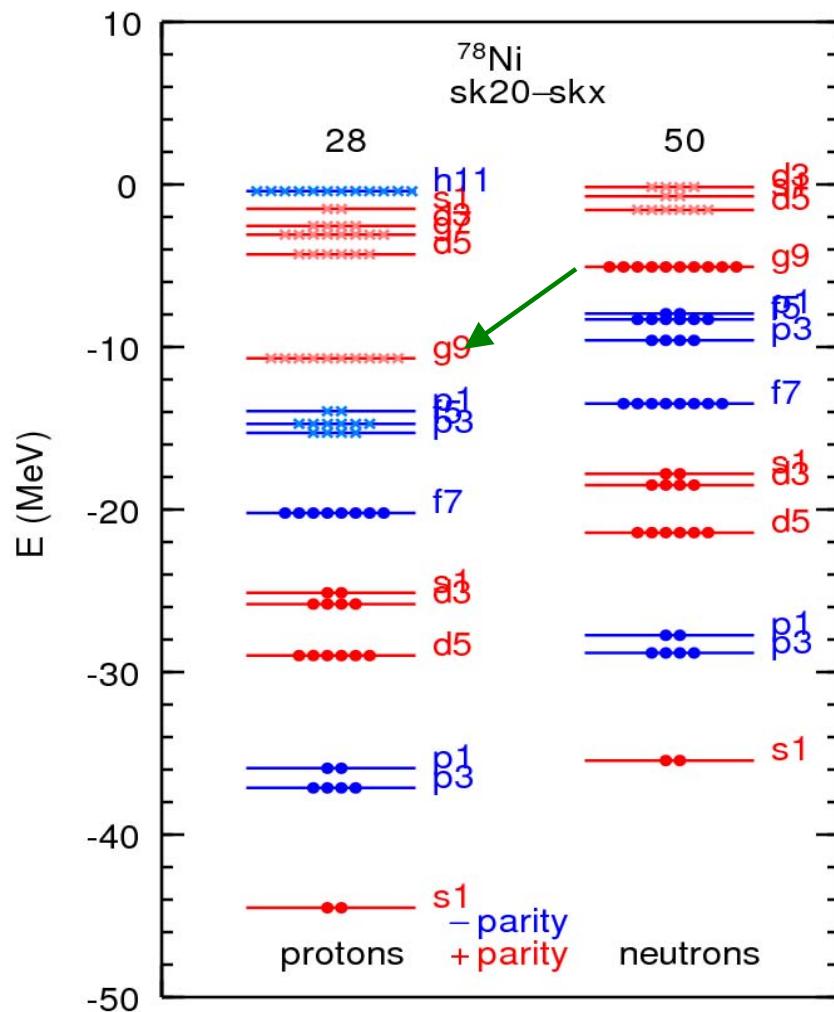




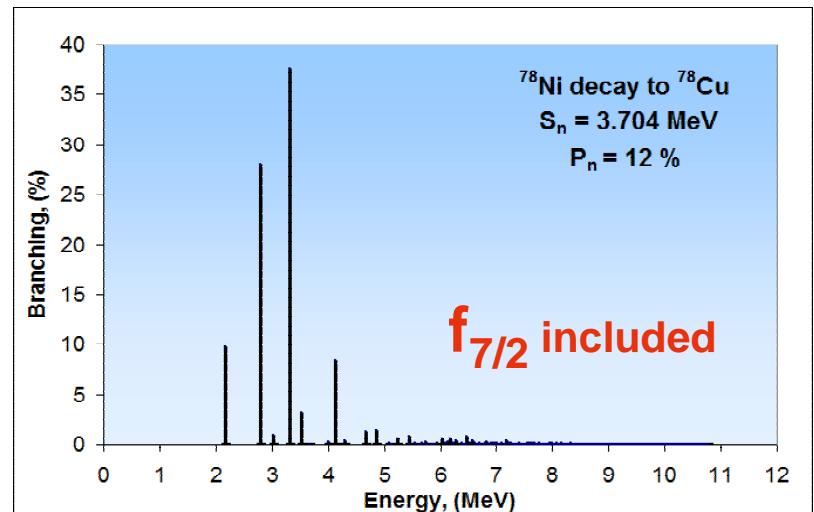
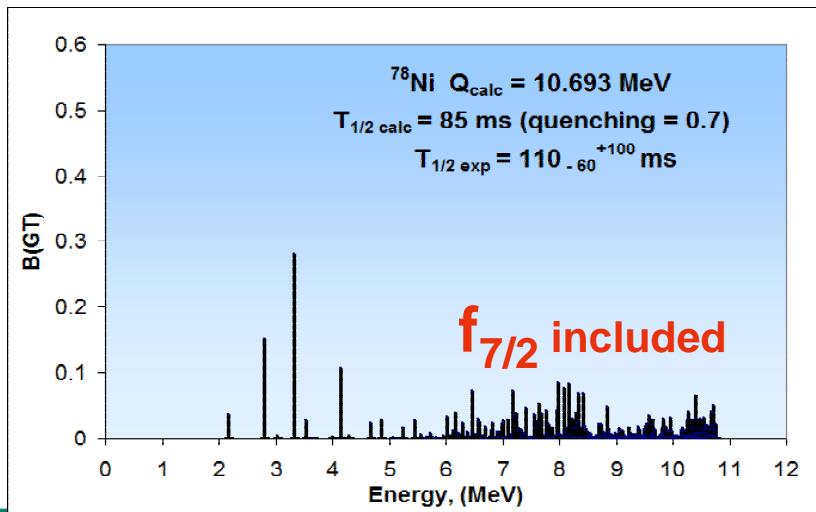
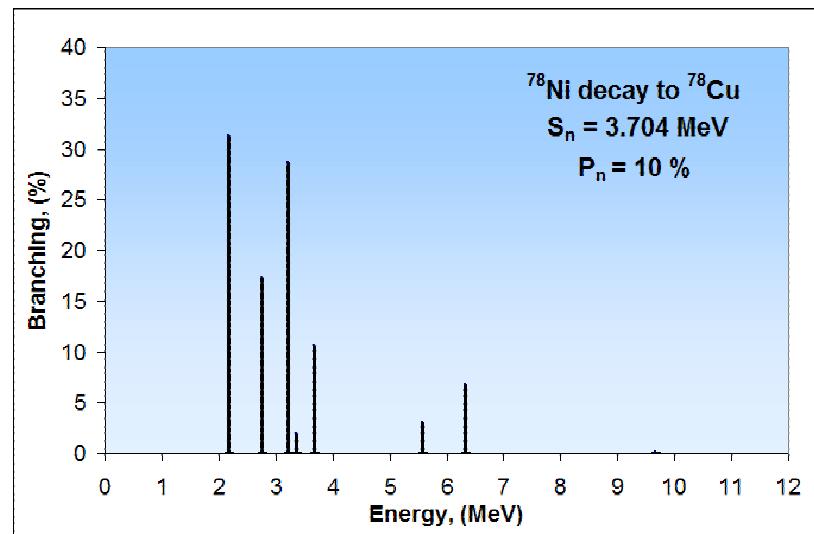
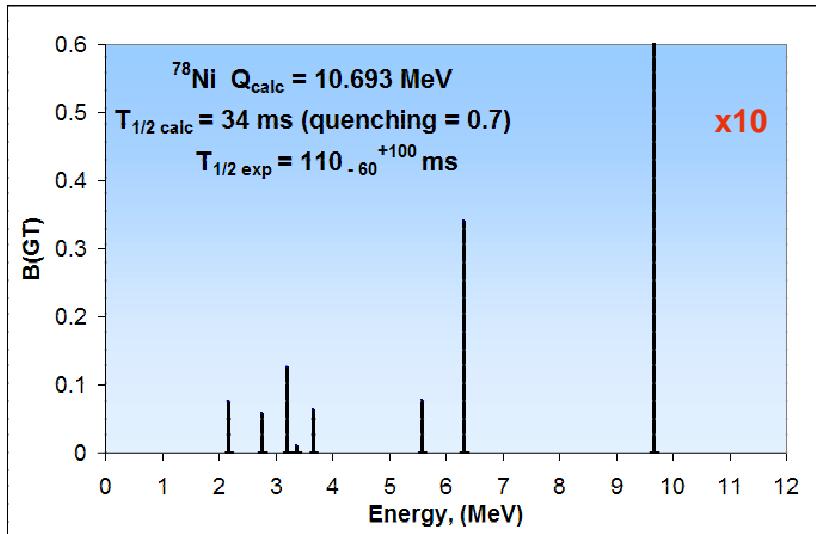
NuShellx t=6

γn , USNDP, BNL, Nov 6, 2008

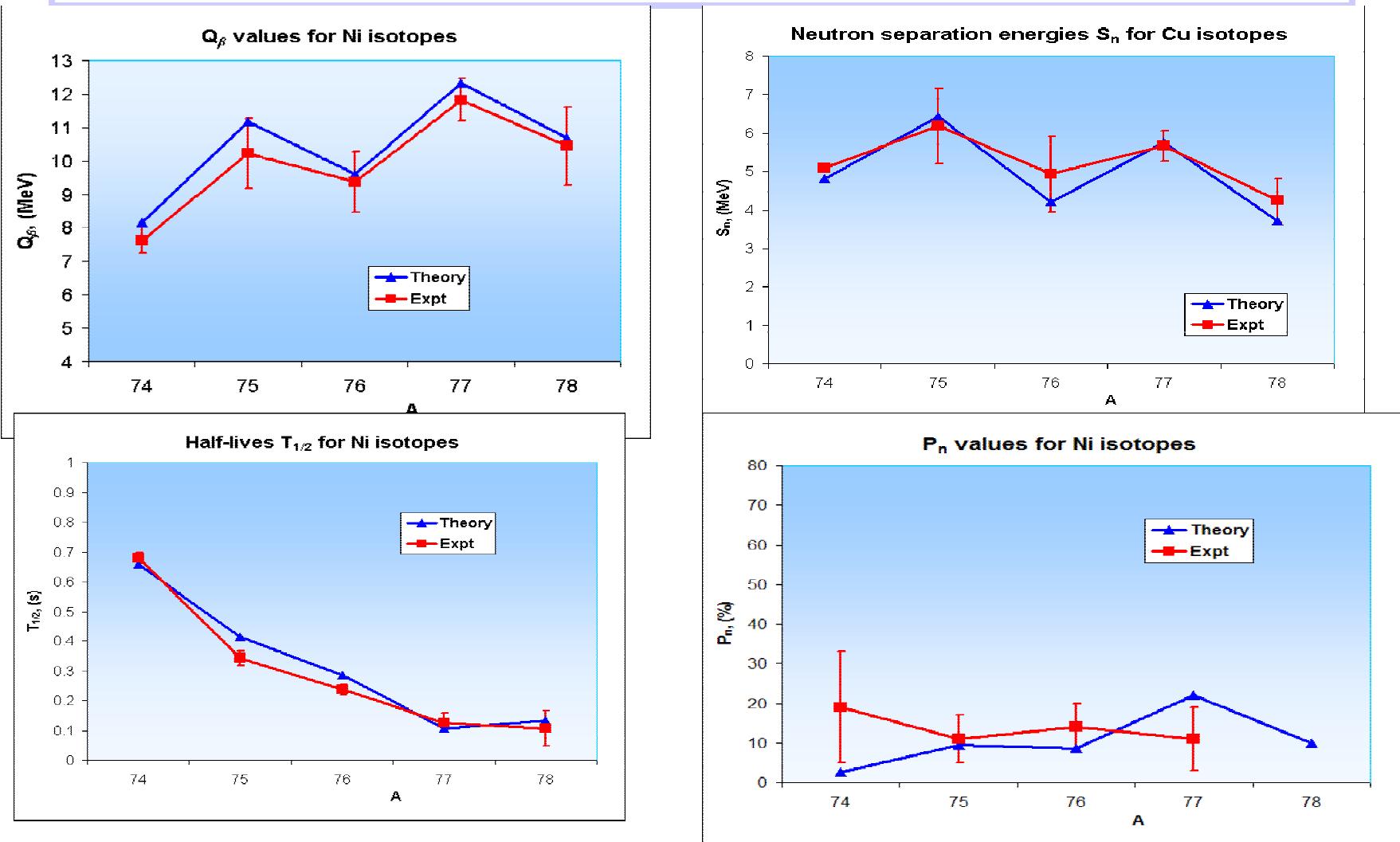




^{78}Ni : beta-decay (Lisetsky)



Ni: Beta-decay results (Lisetsky)

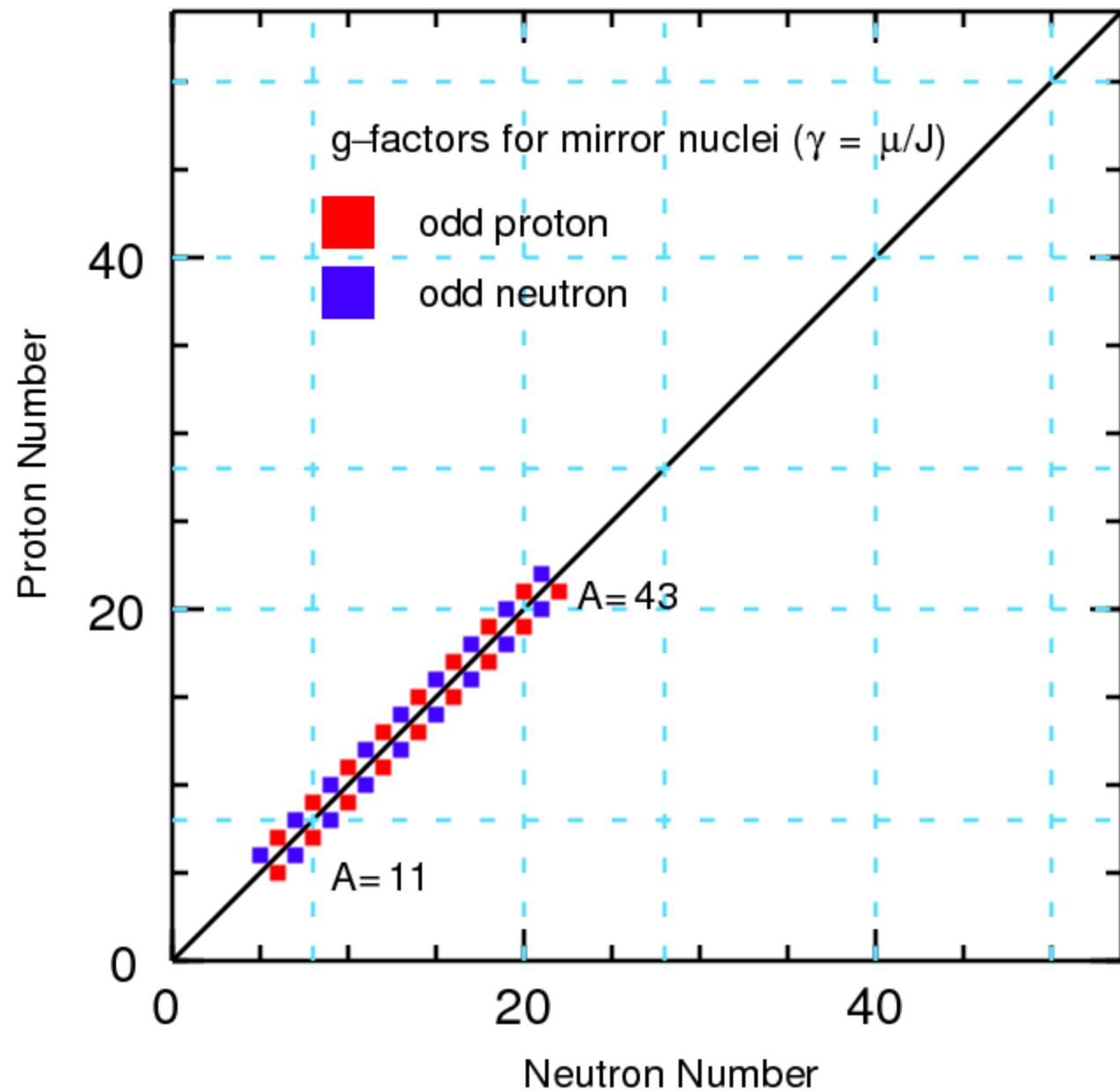


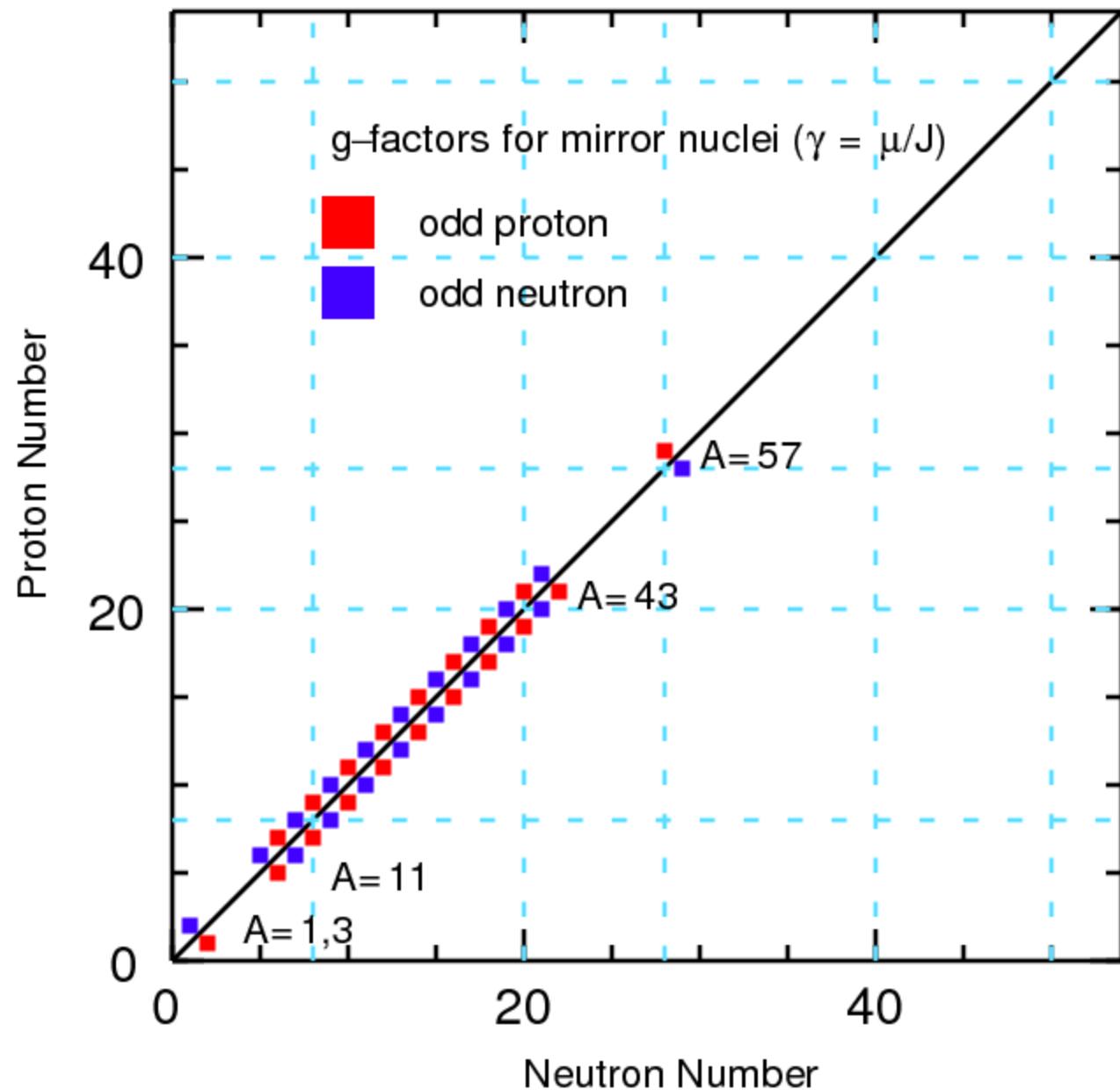
P. T. Hosmer et al., PRL 94, 112501 (2005)

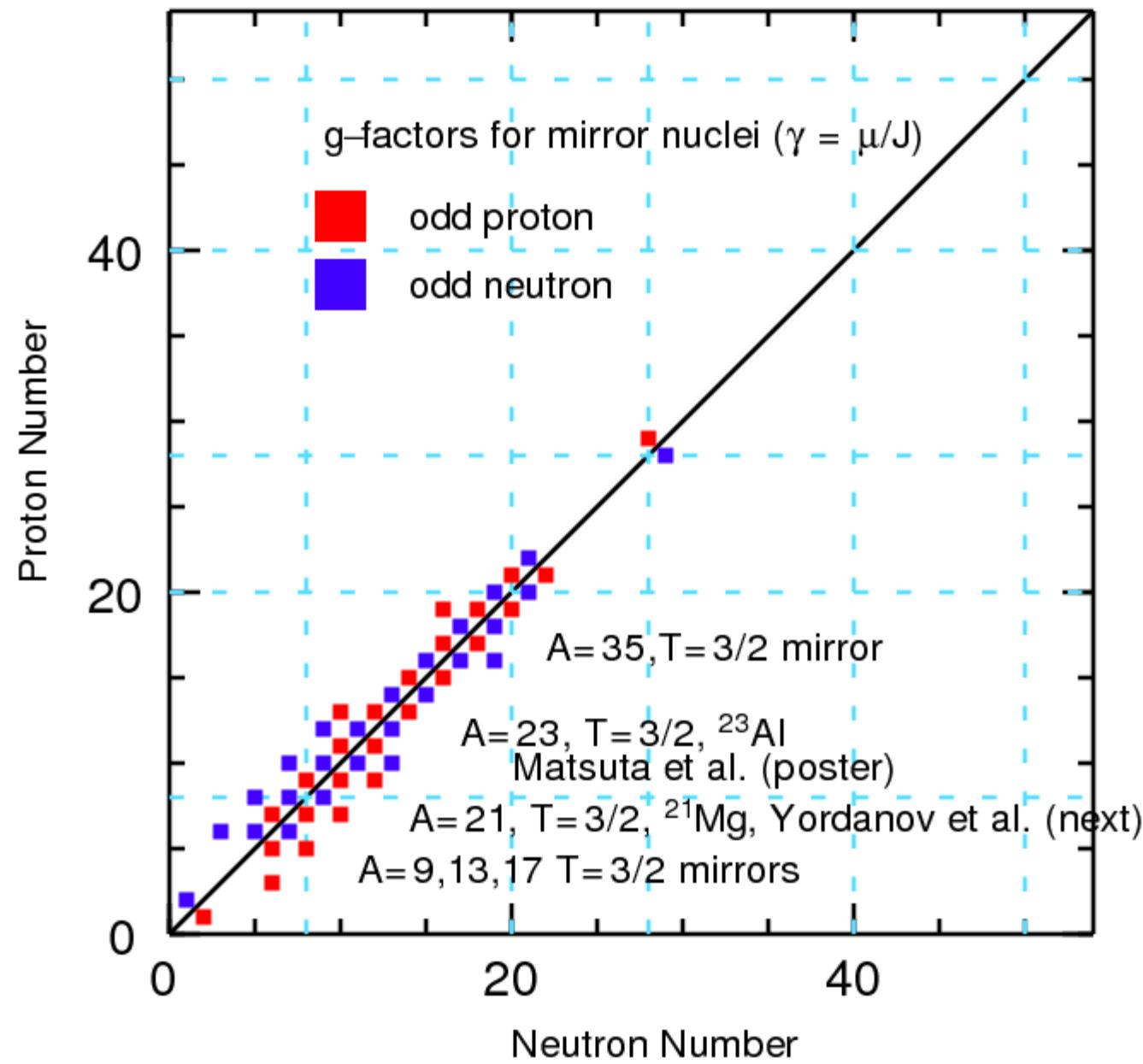


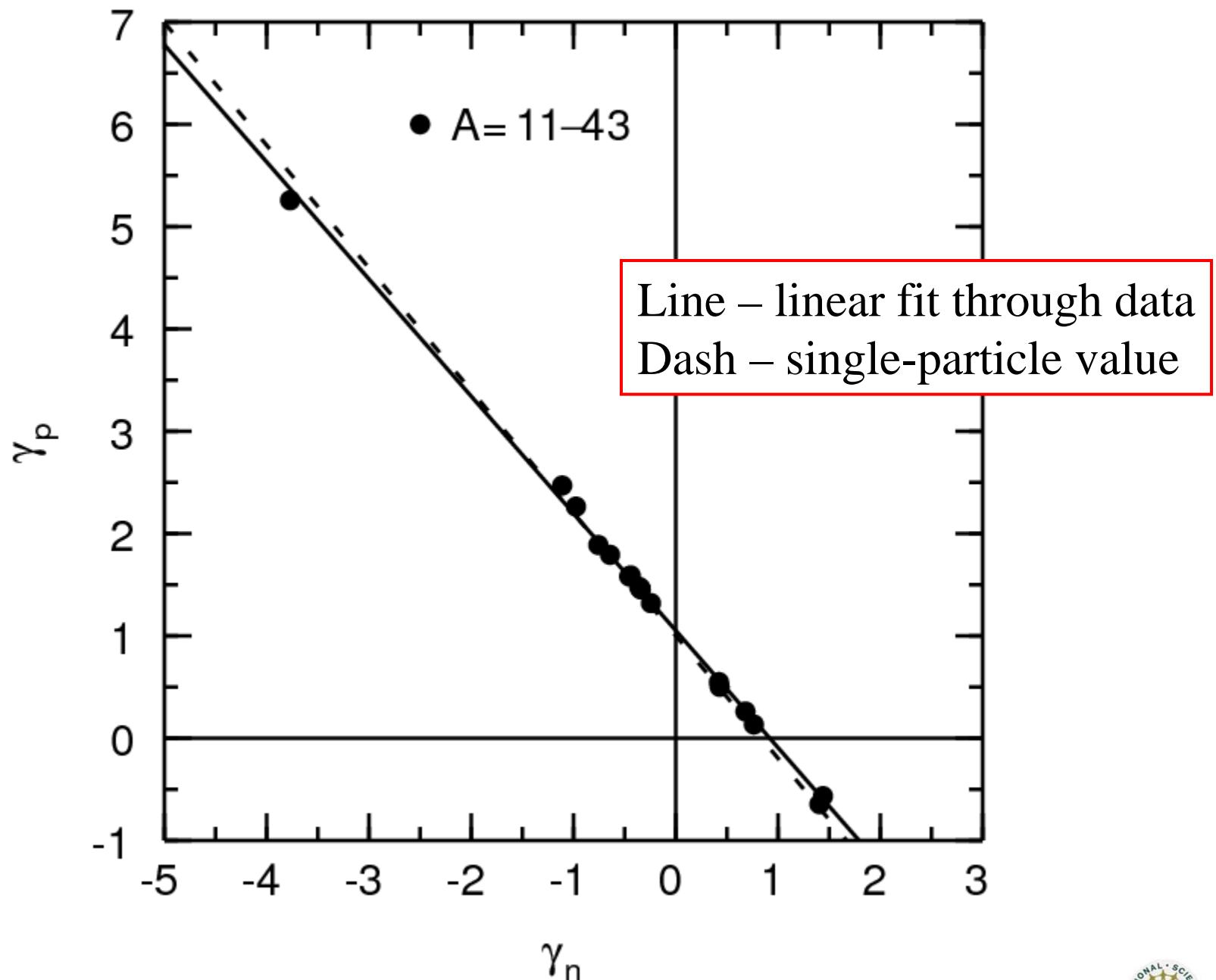
B. Alex Brown, USNDP, BNL, Nov 6, 2008

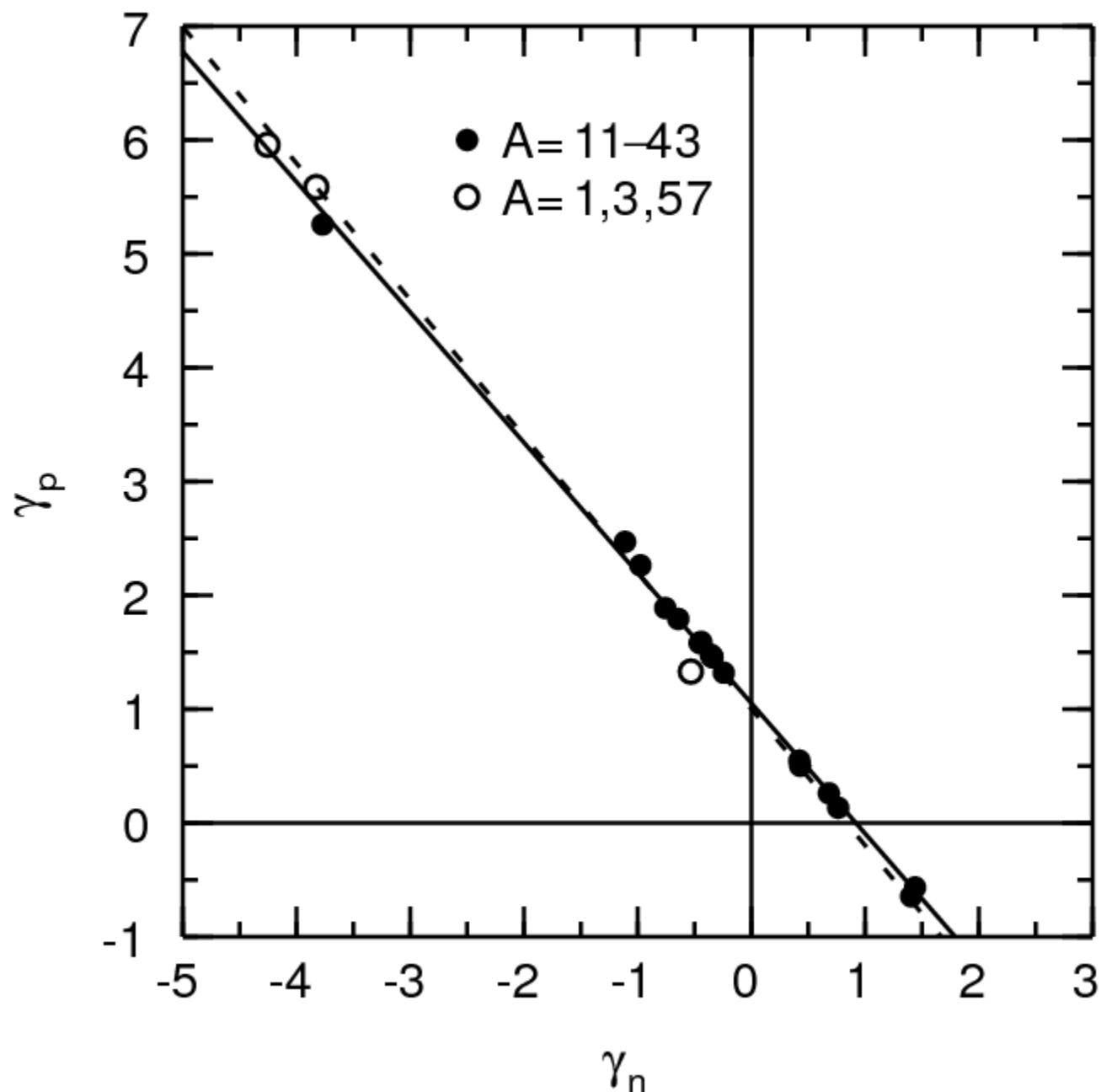


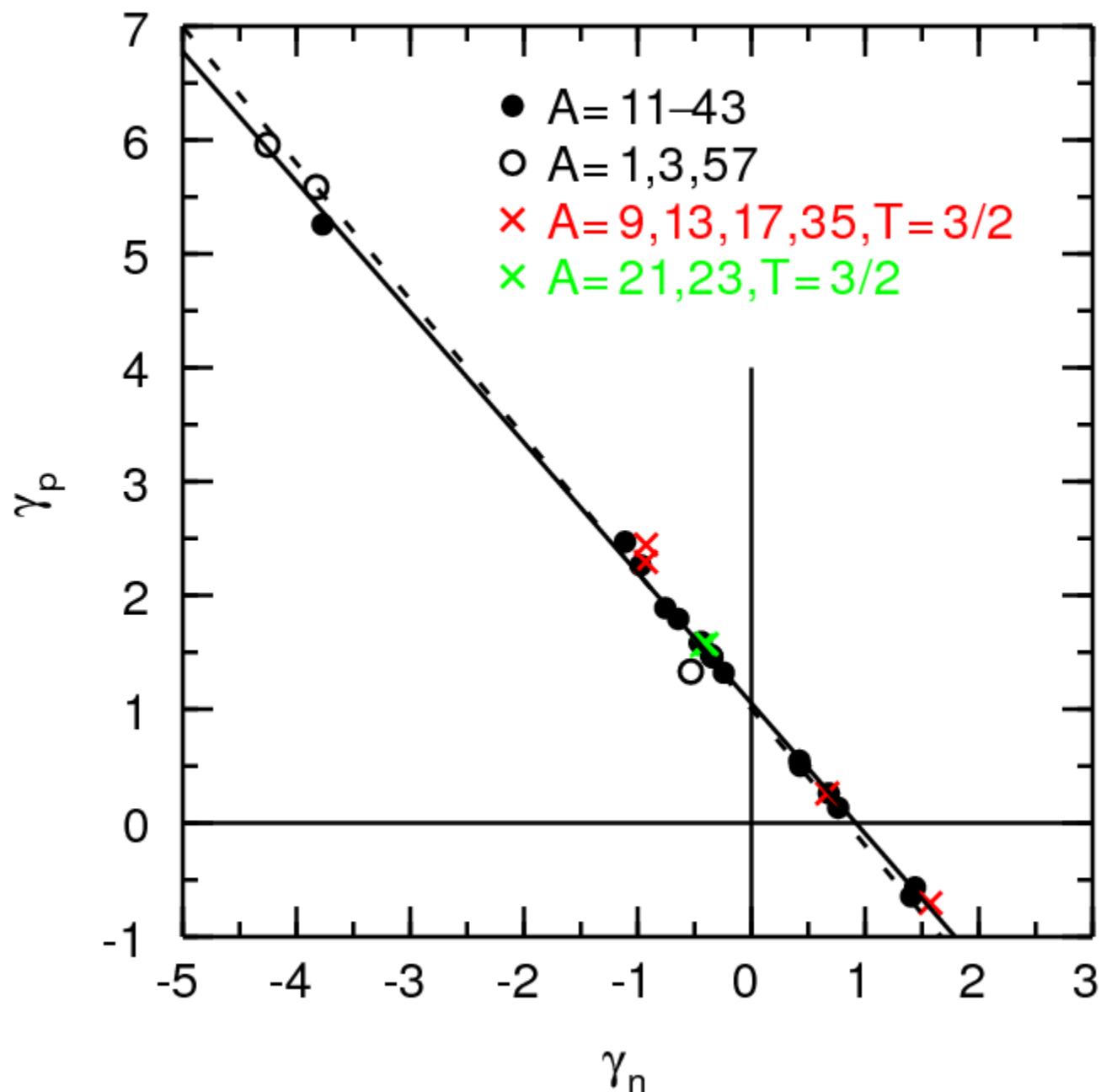












Phys. Rev. C 77, 064311 (2008)

Correlations between magnetic moments and beta decay

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VOLUME 50, NUMBER 25

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20 JUNE 1983

New Look at Magnetic Moments and Beta Decays of Mirror Nuclei

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Department of Theoretical Physics, Oxford University, Oxford OX1 3RH, United Kingdom

and

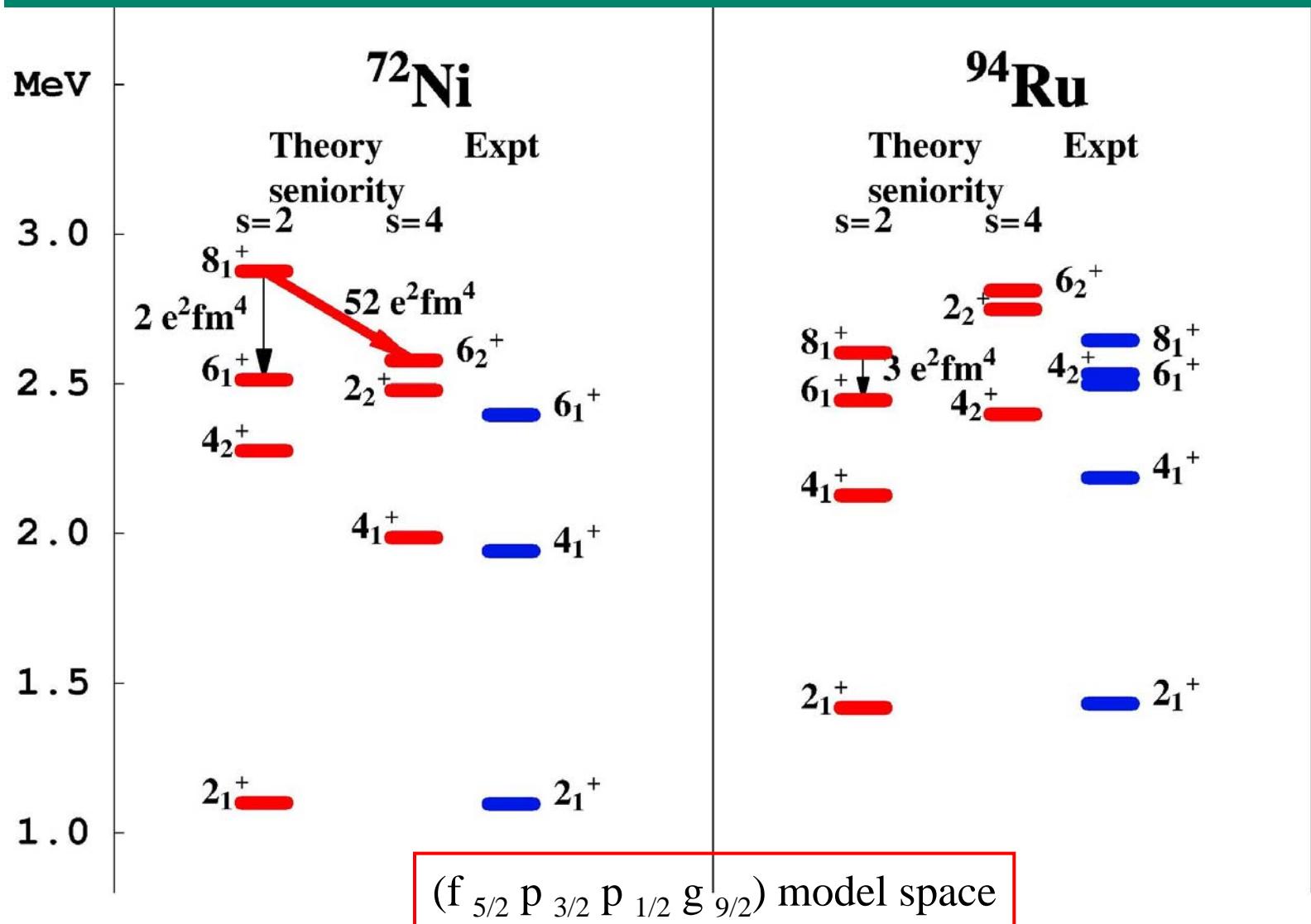
S. M. Perez



B. Alex Brown, USNDP, BNL, Nov 6, 2008

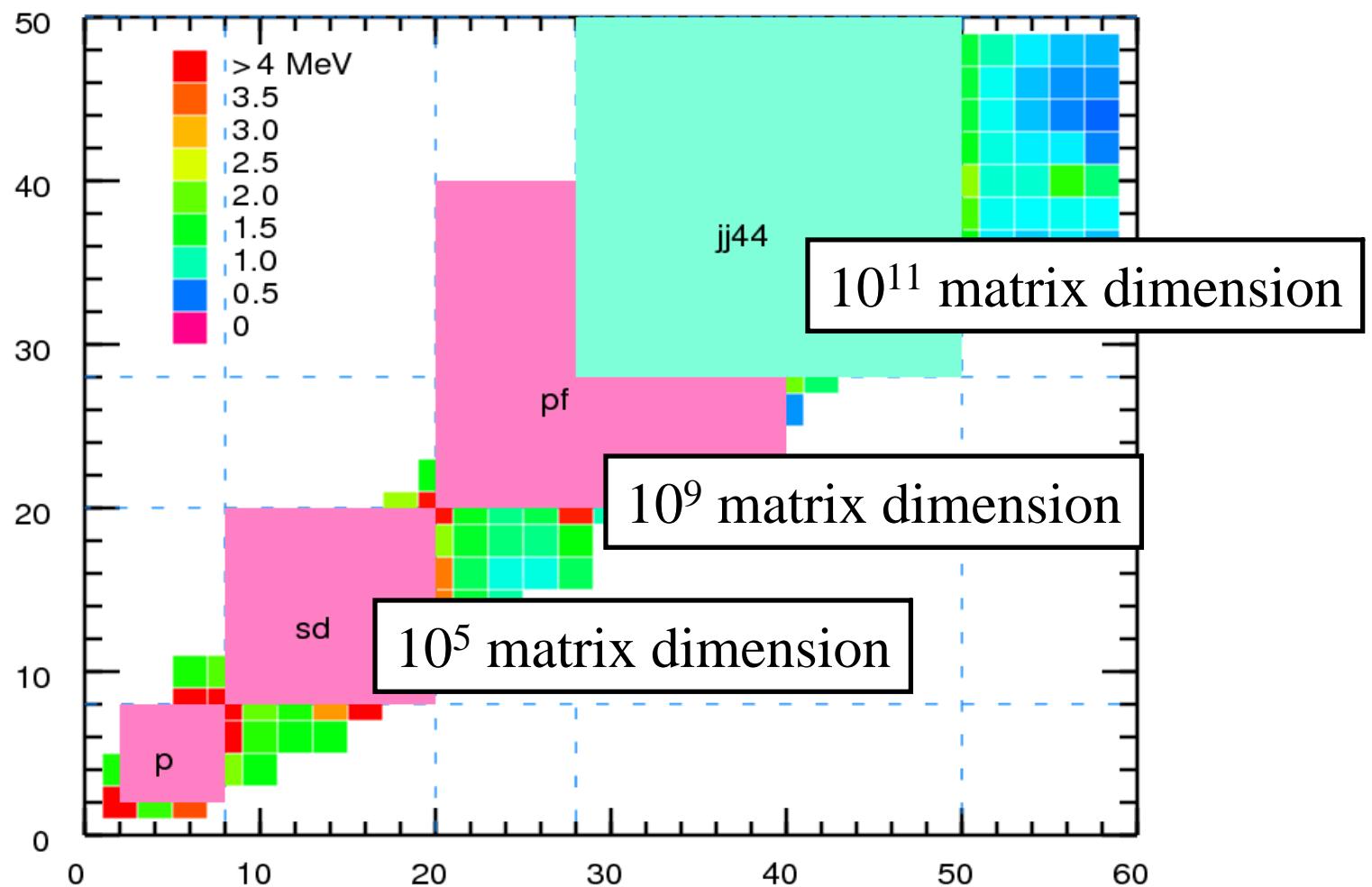


Faded seniority isomerism near ^{78}Ni



A. Lisetskiy et al., PRC 70, 044312 (2004)

B. Alex Brown, USNDP, BNL, Nov 6, 2008



jj44 means $f_{5/2}$, $p_{3/2}$, $p_{1/2}$, $g_{9/2}$ orbits for protons and neutrons

