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## *Uncertainty Analysis with the AFCI1.2 Covariance Matrix*



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### AFCI covariance matrix

- A first release of the matrix (AFCI1.0) was made in November last year. The first applications of AFCI1.0 were presented at the data adjustment meeting held at INL in December 2008 and at the Nuclear Physics Working Group meeting held in San Diego (CA) in May 2009. The matrix was used to calculate the uncertainty of the multiplication factor of all fast systems investigated in the Sg26 activity (ABTR, SFR, EFR, GFR, LFR, ADMAB).
- An updated version of the matrix, called AFCI1.1, was released by BNL and LALN in May 2009: Pu239 (only  $\nu$ ), Fe56, Cr50, Ni58, C, O, Na23, B10, Zr90 and Mn55 were reprocessed. Applications were presented at the NNDC meeting in Port Jefferson, June 2009 (see also ANS paper, Nov. 2009).
- The AFCI1.2 matrix was released in August 2009: 14 MAs were updated as guided by Maslov review and missing correlation matrices were recovered; U235 capture and Pu239  $\nu$  were updated; Structural materials (Cr, Fe, Ni, Pb, Bi) were reviewed and updated.
- The present work shows an extensive application of the recent AFCI1.2 matrix, with the determination of the uncertainty for the main integral parameters (multiplication factor, power peaking factor, Doppler reactivity coefficient, coolant void reactivity worth and burnup reactivity swing) of a series of fast reactors (ABR metal core, ABR oxide core, SFR, EFR, GFR, LFR, ADMAB).  
The obtained AFCI1.2 parameter uncertainties are also compared with the results presented in previous studies with the BOLNA correlation matrix.

## AFCI1.2 Covariance Matrix at a Glance

- Processed/used isotopes:  
U234, U235, U236, U238, Np237, Pu238, Pu239, Pu240, Pu241, Pu242, Am241, Am242m, Am243, Cm242, Cm243, Cm244, Cm245, Cm246, Fe56, Fe57, Cr50, Cr52, Ni58, Ni60, Zr90, Zr91, Zr92, Zr94, Na23, O, He4, Si28, C, N15, B10, B11, P204, Pb206, Pb207, Pb208, Bi209, Mn55, Mo92, Mo94, Mo95, Mo96, Mo97, Mo98, Mo100.
- Processed/used reactions:  
**v, fission, capture, elastic, inelastic and n2n** for fissile isotopes and **capture, elastic, inelastic and n2n** for structural isotopes.
- For most of the isotopes AFCI1.2 contains covariance data for the reaction itself, only for **U235, U238, Pu239, Cm246, Fe56, Cr52, Ni58, O, Zr90, C, B10, B11, Mn55, N15** some cross-correlations have been also provided.
- In the AFCI1.2 matrix there are no “cross-material” correlations.

## Features of the Investigated Systems

| <b>System</b>         | <b>Coolant</b> | <b>Fuel Type</b> | <b>%TRU in (U+TRU)</b>     | <b>% MA<sup>(a)</sup> in (U+TRU)</b> | <b>Power [MW<sub>th</sub>]</b> |
|-----------------------|----------------|------------------|----------------------------|--------------------------------------|--------------------------------|
| <b>ABR Metal Core</b> | Na             | Metal            | 18.5 – 24.2 <sup>(b)</sup> | 1.5 – 2.2 <sup>(b)</sup>             | 1000                           |
| <b>ABR Oxide Core</b> | Na             | MOX              | 23.2 – 37.1 <sup>(b)</sup> | 2.2 – 4.1 <sup>(b)</sup>             | 1000                           |
| <b>SFR</b>            | Na             | Metal            | 60.5                       | 10.6                                 | 840                            |
| <b>EFR</b>            | Na             | MOX              | 23.7                       | 1.2                                  | 3600                           |
| <b>GFR</b>            | He             | Carbide          | 21.7                       | 5.0                                  | 2400                           |
| <b>LFR</b>            | Pb             | Metal            | 23.3                       | 2.4                                  | 900                            |
| <b>ADMAB</b>          | LBE            | Nitride          | 100                        | 68.0                                 | 380                            |

<sup>(a)</sup> MA: Minor Actinides;

<sup>(b)</sup> Inner Core – Outer Core.

In the AFCI1.1 matrix, the correlation matrices for several reactions of the isotopes from the Maslov evaluation (all actinides except U235, U238 and Pu239) had no correlations in energy and, as consequence, contain diagonal values only (i.e. no “off-diagonal” energy correlation terms were provided).

**SFR  $k_{\text{eff}}$  Uncertainties (%) by Isotope and Reaction**

|                             | <b>Diagonal<br/>BOLNA</b> | <b>Diagonal<br/>AFCI1.1</b> | <b>Full<br/>BOLNA</b> | <b>Full<br/>AFCI1.1</b> |
|-----------------------------|---------------------------|-----------------------------|-----------------------|-------------------------|
| <b>Pu238 fission</b>        | 0.32                      | 0.61                        | 0.56                  | 0.61                    |
| <b>Pu240 fission</b>        | 0.27                      | 0.20                        | 0.35                  | 0.20                    |
| <b>Pu241 fission</b>        | 0.54                      | 0.37                        | 1.01                  | 0.37                    |
| <b>Pu242 fission</b>        | 0.25                      | 0.20                        | 0.38                  | 0.20                    |
| <b>Am242m fission</b>       | 0.38                      | 0.27                        | 0.77                  | 0.27                    |
| <b>Cm244 fission</b>        | 0.27                      | 0.06                        | 0.41                  | 0.06                    |
| <b>Cm245 fission</b>        | 0.20                      | 0.14                        | 0.41                  | 0.14                    |
| <b>Total <sup>(a)</sup></b> | <b>1.10</b>               | <b>0.92</b>                 | <b>1.86</b>           | <b>1.09</b>             |

<sup>(a)</sup> Total of all isotopes (not listed too)

AFCI1.1 correlation matrices with diagonal values only:

U234 (inelastic, fission,  $\nu$ )

U236 (elastic, fission, capture,  $\nu$ )

Np237 (elastic, fission,  $\nu$ )

Pu238 (fission,  $\nu$ )

Pu240 (fission,  $\nu$ )

Pu241 (elastic, fission, capture,  $\nu$ )

Pu242 (fission,  $\nu$ )

Am241 (elastic, fission, capture,  $\nu$ )

Am242m (fission, capture,  $\nu$ )

Am243 (fission, capture,  $\nu$ )

Cm242 (fission,  $\nu$ )

Cm243 (elastic, fission,  $\nu$ )

Cm244 (fission,  $\nu$ )

Cm245 (elastic, fission, capture,  $\nu$ )

All the correlation matrices missing in AFCI1.1 have been added in AFCI1.2.

**SFR  $k_{\text{eff}}$  Uncertainties (%) by Isotope and Reaction**

|                             | <b>Diagonal<br/>BOLNA</b> | <b>Diagonal<br/>AFCI1.1</b> | <b>Diagonal<br/>AFCI1.2</b> | <b>Full<br/>BOLNA</b> | <b>Full<br/>AFCI1.1</b> | <b>Full<br/>AFCI1.2</b> |
|-----------------------------|---------------------------|-----------------------------|-----------------------------|-----------------------|-------------------------|-------------------------|
| <b>Pu238 fission</b>        | 0.32                      | 0.61                        | 0.61                        | 0.56                  | 0.61                    | 1.36                    |
| <b>Pu240 fission</b>        | 0.27                      | 0.20                        | 0.20                        | 0.35                  | 0.20                    | 0.38                    |
| <b>Pu241 fission</b>        | 0.54                      | 0.37                        | 0.40                        | 1.01                  | 0.37                    | 1.02                    |
| <b>Pu242 fission</b>        | 0.25                      | 0.20                        | 0.21                        | 0.38                  | 0.20                    | 0.40                    |
| <b>Am242m fission</b>       | 0.38                      | 0.27                        | 0.25                        | 0.77                  | 0.27                    | 0.69                    |
| <b>Cm244 fission</b>        | 0.27                      | 0.06                        | 0.07                        | 0.41                  | 0.06                    | 0.15                    |
| <b>Cm245 fission</b>        | 0.20                      | 0.14                        | 0.16                        | 0.41                  | 0.14                    | 0.43                    |
| <b>Total <sup>(a)</sup></b> | <b>1.10</b>               | <b>0.92</b>                 | <b>0.94</b>                 | <b>1.86</b>           | <b>1.09</b>             | <b>2.16</b>             |

<sup>(a)</sup> Total of all isotopes (not listed too)

Improvements of AFCI1.2 based on  
the Results of AFCI1.1 Applications

In AFCI1.1, U235 Capture  
standard deviations were  
considered suspicious!

| U235 Standard Deviations (%) |          |                  |                 |                 |               |                 |                    |                 |                 |               |                 |
|------------------------------|----------|------------------|-----------------|-----------------|---------------|-----------------|--------------------|-----------------|-----------------|---------------|-----------------|
|                              |          | U235: BOLNA 15Gr |                 |                 |               |                 | U235: AFCI1.1 33Gr |                 |                 |               |                 |
| Gr.                          | [MeV]    | $\nu$            | $\sigma_{fiss}$ | $\sigma_{inel}$ | $\sigma_{el}$ | $\sigma_{capt}$ | $\nu$              | $\sigma_{fiss}$ | $\sigma_{inel}$ | $\sigma_{el}$ | $\sigma_{capt}$ |
| 1                            | 1.964E+1 | 0.9              | 0.5             | 21.7            | 9.6           | 61.1            | 1.0                | 0.5             | 25.5            | 6.9           | 60.6            |
| 2                            | 1.000E+1 |                  |                 |                 |               |                 | 1.0                | 0.6             | 15.9            | 6.3           | 62.7            |
| 3                            | 6.065E+0 |                  |                 |                 |               |                 | 0.8                | 0.5             | 8.9             | 5.1           | 46.4            |
| 4                            | 3.679E+0 | 0.7              | 0.5             | 6.8             | 4.2           | 37.0            | 0.6                | 0.5             | 6.4             | 4.0           | 26.5            |
| 5                            | 2.231E+0 |                  |                 |                 |               |                 | 0.6                | 0.5             | 6.4             | 4.5           | 19.1            |
| 6                            | 1.353E+0 |                  |                 |                 |               |                 | 0.6                | 0.5             | 7.6             | 3.6           | 16.1            |
| 7                            | 8.209E-1 | 0.6              | 0.5             | 11.3            | 2.9           | 22.1            | 0.6                | 0.5             | 8.5             | 3.3           | 16.8            |
| 8                            | 4.979E-1 |                  |                 |                 |               |                 | 0.6                | 0.6             | 10.5            | 3.2           | 20.4            |
| 9                            | 3.020E-1 |                  |                 |                 |               |                 | 0.6                | 0.6             | 12.7            | 2.7           | 25.2            |
| 10                           | 1.832E-1 | 0.7              | 0.5             | 15.0            | 2.4           | 30.6            | 0.7                | 0.6             | 15.0            | 2.4           | 30.1            |
| 11                           | 1.111E-1 |                  |                 |                 |               |                 | 0.7                | 0.6             | 15.1            | 2.4           | 31.5            |
| 12                           | 6.738E-2 |                  |                 |                 |               |                 | 0.7                | 0.5             | 15.1            | 2.5           | 32.2            |
| 13                           | 4.087E-2 | 0.7              | 0.5             | 14.7            | 2.6           | 32.9            | 0.7                | 0.6             | 19.4            | 2.8           | 34.0            |
| 14                           | 2.479E-2 |                  |                 |                 |               |                 | 0.7                | 0.7             | 50.0            | 3.0           | 34.0            |
| 15                           | 1.503E-2 |                  |                 |                 |               |                 | 0.7                | 0.6             | 50.0            | 3.2           | 34.0            |
| 16                           | 9.119E-3 | 0.7              | 3.2             | 48.5            | 5.2           | 33.9            | 0.7                | 0.5             | 50.0            | 3.4           | 34.0            |
| 17                           | 5.531E-3 |                  |                 |                 |               |                 | 0.7                | 0.5             | 50.0            | 4.0           | 34.0            |
| 18                           | 3.355E-3 |                  |                 |                 |               |                 | 0.7                | 0.5             | 50.0            | 4.6           | 34.0            |
| 19                           | 2.035E-3 | 0.7              | 0.8             | 0.0             | 2.1           | 4.6             | 0.7                | 5.7             | 41.8            | 6.3           | 29.4            |
| 20                           | 1.234E-3 |                  |                 |                 |               |                 | 0.7                | 3.1             | 0.0             | 3.8           | 13.1            |
| 21                           | 7.485E-4 |                  |                 |                 |               |                 | 0.7                | 0.4             | 0.0             | 2.3           | 5.2             |
| 22                           | 4.540E-4 | 0.7              | 0.4             | 0.0             | 1.3           | 0.6             | 0.7                | 0.3             | 0.0             | 1.6           | 2.5             |
| 23                           | 3.043E-4 |                  |                 |                 |               |                 | 0.7                | 0.4             | 0.0             | 1.5           | 1.6             |
| 24                           | 1.486E-4 |                  |                 |                 |               |                 | 0.7                | 0.3             | 0.0             | 1.4           | 1.3             |
| 25                           | 9.166E-5 |                  |                 |                 |               |                 | 0.7                | 0.4             | 0.0             | 1.4           | 1.1             |
| 26                           | 6.790E-5 |                  |                 |                 |               |                 | 0.7                | 0.4             | 0.0             | 1.5           | 1.3             |
| 27                           | 4.017E-5 |                  |                 |                 |               |                 | 0.7                | 0.4             | 0.0             | 1.4           | 1.1             |
| 28                           | 2.260E-5 | 0.7              | 0.6             | 0.0             | 1.5           | 0.7             | 0.7                | 0.6             | 0.0             | 1.6           | 1.1             |
| 29                           | 1.371E-5 |                  |                 |                 |               |                 | 0.7                | 0.6             | 0.0             | 1.6           | 1.0             |
| 30                           | 8.315E-6 |                  |                 |                 |               |                 | 0.7                | 0.5             | 0.0             | 1.5           | 1.2             |
| 31                           | 4.000E-6 |                  |                 |                 |               |                 | 0.7                | 1.2             | 0.0             | 1.7           | 1.8             |
| 32                           | 5.400E-7 |                  |                 |                 |               |                 | 0.7                | 0.8             | 0.0             | 1.7           | 2.2             |
| 33                           | 1.000E-7 |                  |                 |                 |               |                 | 0.7                | 0.4             | 0.0             | 3.1           | 1.6             |
|                              |          | 0.7              | 0.3             | 0.0             | 4.9           | 1.7             | 0.7                | 0.4             | 0.0             | 4.8           | 1.7             |

## Improvements of AFCI1.2 based on the Results of AFCI1.1 Applications

In AFCI1.1, correlation effects in U235 capture matrix were considered more suspicious than standard deviations.

### GODIVA $k_{\text{eff}}$ Uncertainties (%)

|                               | BOLNA<br>diagonal | AFCI1.1<br>diagonal | BOLNA<br>full | AFCI1.1<br>full |
|-------------------------------|-------------------|---------------------|---------------|-----------------|
| Isotope                       | U235              | U235                | U235          | U235            |
| $\nu$                         | 0.27              | 0.21                | 0.56          | 0.56            |
| $\sigma_{\text{fiss}}$        | 0.14              | 0.11                | 0.26          | 0.26            |
| $\sigma_{\text{inel}}$        | 0.22              | 0.16                | 0.32          | 0.32            |
| $\sigma_{\text{el}}$          | 0.07              | 0.05                | 0.11          | 0.11            |
| $\sigma_{\text{capt}}$        | 0.51              | 0.37                | 0.99          | 1.01            |
| <b>Total</b>                  | <b>0.63</b>       | <b>0.47</b>         | <b>1.22</b>   | <b>1.24</b>     |
| <b>Overall <sup>(a)</sup></b> | <b>0.64</b>       | <b>0.47</b>         | <b>1.23</b>   | <b>1.24</b>     |

<sup>(a)</sup> Total of all isotopes

### GODIVA $k_{\text{eff}}$ AFCI1.1 Diagonal Uncertainties (%) Energy Breakdown

|              |          | U235        |                        |                        |                      |                        |
|--------------|----------|-------------|------------------------|------------------------|----------------------|------------------------|
| Gr.          | [MeV]    | $\nu$       | $\sigma_{\text{fiss}}$ | $\sigma_{\text{inel}}$ | $\sigma_{\text{el}}$ | $\sigma_{\text{capt}}$ |
| 1            | 1.964E+1 | -           | -                      | -                      | -                    | -                      |
| 2            | 1.000E+1 | 0.02        | 0.01                   | 0.01                   | -                    | -                      |
| 3            | 6.065E+0 | 0.06        | 0.02                   | 0.04                   | 0.01                 | 0.01                   |
| 4            | 3.679E+0 | 0.09        | 0.04                   | 0.04                   | 0.01                 | 0.03                   |
| 5            | 2.231E+0 | 0.09        | 0.05                   | 0.05                   | 0.02                 | 0.06                   |
| 6            | 1.353E+0 | 0.08        | 0.05                   | 0.08                   | 0.02                 | 0.07                   |
| 7            | 8.209E-1 | 0.08        | 0.05                   | 0.09                   | 0.02                 | 0.10                   |
| 8            | 4.979E-1 | 0.07        | 0.04                   | 0.06                   | 0.02                 | 0.14                   |
| 9            | 3.020E-1 | 0.05        | 0.03                   | 0.04                   | 0.02                 | 0.18                   |
| 10           | 1.832E-1 | 0.04        | 0.02                   | 0.01                   | 0.01                 | 0.19                   |
| 11           | 1.111E-1 | 0.02        | 0.01                   | -                      | -                    | 0.14                   |
| 12           | 6.738E-2 | 0.01        | -                      | -                      | -                    | 0.08                   |
| 13           | 4.087E-2 | 0.01        | -                      | -                      | -                    | 0.05                   |
| 14           | 2.479E-2 | -           | -                      | -                      | -                    | 0.02                   |
| 15           | 1.503E-2 | -           | -                      | -                      | -                    | 0.01                   |
| 16           | 9.119E-3 | -           | -                      | -                      | -                    | 0.01                   |
| 17           | 5.531E-3 | -           | -                      | -                      | -                    | -                      |
| to           |          | -           | -                      | -                      | -                    | -                      |
| 33           | 1.000E-7 | -           | -                      | -                      | -                    | -                      |
| <b>Total</b> |          | <b>0.21</b> | <b>0.11</b>            | <b>0.16</b>            | <b>0.05</b>          | <b>0.37</b>            |



## U235 Standard Deviations (%)

| Gr. | [MeV]    |
|-----|----------|
| 1   | 1.964E+1 |
| 2   | 1.000E+1 |
| 3   | 6.065E+0 |
| 4   | 3.679E+0 |
| 5   | 2.231E+0 |
| 6   | 1.353E+0 |
| 7   | 8.209E-1 |
| 8   | 4.979E-1 |
| 9   | 3.020E-1 |
| 10  | 1.832E-1 |
| 11  | 1.111E-1 |
| 12  | 6.738E-2 |
| 13  | 4.087E-2 |
| 14  | 2.479E-2 |
| 15  | 1.503E-2 |
| 16  | 9.119E-3 |
| 17  | 5.531E-3 |
| 18  | 3.355E-3 |
| 19  | 2.035E-3 |
| 20  | 1.234E-3 |
| 21  | 7.485E-4 |
| 22  | 4.540E-4 |
| 23  | 3.043E-4 |
| 24  | 1.486E-4 |
| 25  | 9.166E-5 |
| 26  | 6.790E-5 |
| 27  | 4.017E-5 |
| 28  | 2.260E-5 |
| 29  | 1.371E-5 |
| 30  | 8.315E-6 |
| 31  | 4.000E-6 |
| 32  | 5.400E-7 |
| 33  | 1.000E-7 |

| U235: BOLNA 15Gr |                        |                        |                      |                        |
|------------------|------------------------|------------------------|----------------------|------------------------|
| $\nu$            | $\sigma_{\text{fiss}}$ | $\sigma_{\text{inel}}$ | $\sigma_{\text{el}}$ | $\sigma_{\text{capt}}$ |
| 0.9              | 0.5                    | 21.7                   | 9.6                  | 61.1                   |
| 0.7              | 0.5                    | 6.8                    | 4.2                  | 37.0                   |
| 0.6              | 0.5                    | 6.4                    | 4.5                  | 19.1                   |
| 0.6              | 0.5                    | 7.6                    | 3.6                  | 16.1                   |
| 0.6              | 0.5                    | 11.3                   | 2.9                  | 22.1                   |
| 0.7              | 0.5                    | 15.0                   | 2.4                  | 30.6                   |
| 0.7              | 0.5                    | 14.7                   | 2.6                  | 32.9                   |
| 0.7              | 0.6                    | 50.0                   | 3.2                  | 34.0                   |
| 0.7              | 3.2                    | 48.5                   | 5.2                  | 33.9                   |
| 0.7              | 0.8                    | 0.0                    | 2.1                  | 4.6                    |
| 0.7              | 0.4                    | 0.0                    | 1.3                  | 0.6                    |
| 0.7              | 0.6                    | 0.0                    | 1.5                  | 0.7                    |
| 0.7              | 0.4                    | 0.0                    | 1.8                  | 1.4                    |
| 0.7              | 0.3                    | 0.0                    | 3.4                  | 1.6                    |
| 0.7              | 0.3                    | 0.0                    | 4.9                  | 1.7                    |

| U235: AFCI1.1 33Gr |                        |                        |                      |                        |
|--------------------|------------------------|------------------------|----------------------|------------------------|
| $\nu$              | $\sigma_{\text{fiss}}$ | $\sigma_{\text{inel}}$ | $\sigma_{\text{el}}$ | $\sigma_{\text{capt}}$ |
| 1.0                | 0.5                    | 25.5                   | 6.9                  | 60.6                   |
| 1.0                | 0.6                    | 15.9                   | 6.3                  | 62.7                   |
| 0.8                | 0.5                    | 8.9                    | 5.1                  | 46.4                   |
| 0.6                | 0.5                    | 6.4                    | 4.0                  | 26.5                   |
| 0.6                | 0.5                    | 6.4                    | 4.6                  | 19.1                   |
| 0.6                | 0.5                    | 7.0                    | 4.1                  | 16.2                   |
| 0.6                | 0.5                    | 8.5                    | 3.3                  | 16.8                   |
| 0.6                | 0.6                    | 10.5                   | 3.2                  | 20.4                   |
| 0.6                | 0.6                    | 12.7                   | 2.7                  | 25.2                   |
| 0.7                | 0.6                    | 15.0                   | 2.4                  | 30.1                   |
| 0.7                | 0.6                    | 15.1                   | 2.4                  | 31.5                   |
| 0.7                | 0.5                    | 15.1                   | 2.5                  | 32.2                   |
| 0.7                | 0.6                    | 19.4                   | 2.8                  | 34.0                   |
| 0.7                | 0.7                    | 50.0                   | 3.0                  | 34.0                   |
| 0.7                | 0.5                    | 50.0                   | 3.4                  | 34.0                   |
| 0.7                | 0.5                    | 50.0                   | 4.0                  | 34.0                   |
| 0.7                | 0.5                    | 50.0                   | 4.6                  | 34.0                   |
| 0.7                | 5.7                    | 41.8                   | 6.3                  | 29.4                   |
| 0.7                | 3.1                    | 0.0                    | 3.8                  | 13.1                   |
| 0.7                | 0.4                    | 0.0                    | 2.3                  | 5.2                    |
| 0.7                | 0.3                    | 0.0                    | 1.6                  | 2.5                    |
| 0.7                | 0.4                    | 0.0                    | 1.5                  | 1.6                    |
| 0.7                | 0.3                    | 0.0                    | 1.4                  | 1.3                    |
| 0.7                | 0.4                    | 0.0                    | 1.4                  | 1.1                    |
| 0.7                | 0.4                    | 0.0                    | 1.5                  | 1.3                    |
| 0.7                | 0.4                    | 0.0                    | 1.4                  | 1.1                    |
| 0.7                | 0.6                    | 0.0                    | 1.6                  | 1.1                    |
| 0.7                | 0.6                    | 0.0                    | 1.6                  | 1.0                    |
| 0.7                | 0.5                    | 0.0                    | 1.5                  | 1.2                    |
| 0.7                | 1.2                    | 0.0                    | 1.7                  | 1.8                    |
| 0.7                | 0.8                    | 0.0                    | 1.7                  | 2.2                    |
| 0.7                | 0.4                    | 0.0                    | 3.1                  | 1.6                    |
| 0.7                | 0.4                    | 0.0                    | 4.8                  | 1.7                    |

| U235: AFCI1.2 33Gr |                        |                        |                      |                        |
|--------------------|------------------------|------------------------|----------------------|------------------------|
| $\nu$              | $\sigma_{\text{fiss}}$ | $\sigma_{\text{inel}}$ | $\sigma_{\text{el}}$ | $\sigma_{\text{capt}}$ |
| 0.8                | 0.5                    | 25.5                   | 7.5                  | 60.6                   |
| 0.2                | 0.6                    | 15.9                   | 6.5                  | 62.7                   |
| 0.2                | 0.5                    | 8.9                    | 5.0                  | 46.4                   |
| 0.2                | 0.5                    | 6.4                    | 4.0                  | 26.5                   |
| 0.2                | 0.5                    | 6.4                    | 4.5                  | 19.1                   |
| 0.1                | 0.5                    | 7.0                    | 4.0                  | 16.2                   |
| 0.1                | 0.5                    | 8.5                    | 3.3                  | 16.8                   |
| 0.1                | 0.6                    | 10.5                   | 3.1                  | 19.6                   |
| 0.2                | 0.6                    | 12.7                   | 2.7                  | 20.0                   |
| 0.3                | 0.6                    | 15.0                   | 2.3                  | 20.0                   |
| 0.2                | 0.6                    | 15.1                   | 2.1                  | 20.0                   |
| 0.3                | 0.5                    | 15.1                   | 2.1                  | 20.0                   |
| 0.3                | 0.6                    | 19.4                   | 2.2                  | 20.0                   |
| 0.2                | 0.7                    | 50.0                   | 2.4                  | 20.0                   |
| 0.3                | 0.5                    | 50.0                   | 2.6                  | 20.0                   |
| 0.3                | 0.5                    | 50.0                   | 2.9                  | 20.0                   |
| 0.3                | 0.5                    | 50.0                   | 3.3                  | 20.0                   |
| 0.3                | 5.7                    | 41.8                   | 4.7                  | 18.3                   |
| 0.6                | 3.1                    | 0.0                    | 3.8                  | 13.1                   |
| 0.4                | 0.4                    | 0.0                    | 2.3                  | 5.2                    |
| 0.7                | 0.3                    | 0.0                    | 1.6                  | 2.5                    |
| 1.1                | 0.4                    | 0.0                    | 1.5                  | 1.6                    |
| 1.1                | 0.3                    | 0.0                    | 1.4                  | 1.3                    |
| 0.1                | 0.4                    | 0.0                    | 1.4                  | 1.1                    |
| 0.1                | 0.4                    | 0.0                    | 1.5                  | 1.3                    |
| 0.1                | 0.4                    | 0.0                    | 1.4                  | 1.1                    |
| 0.1                | 0.6                    | 0.0                    | 1.6                  | 1.1                    |
| 0.1                | 0.6                    | 0.0                    | 1.6                  | 1.0                    |
| 0.1                | 0.5                    | 0.0                    | 1.5                  | 1.2                    |
| 0.1                | 1.2                    | 0.0                    | 1.7                  | 1.8                    |
| 0.1                | 0.8                    | 0.0                    | 1.7                  | 2.2                    |
| 0.1                | 0.4                    | 0.0                    | 3.1                  | 1.6                    |
| 0.1                | 0.4                    | 0.0                    | 4.8                  | 1.7                    |

## Improvements of AFCI1.2 based on the Results of AFCI1.1 Applications

**GODIVA  $k_{\text{eff}}$  Uncertainties (%)**

|                                          | <b>BOLNA<br/>diagonal</b> | <b>AFCI1.1<br/>diagonal</b> | <b>AFCI1.2<br/>diagonal</b> | <b>BOLNA<br/>full</b> | <b>AFCI1.1<br/>full</b> | <b>AFCI1.2<br/>full</b> |
|------------------------------------------|---------------------------|-----------------------------|-----------------------------|-----------------------|-------------------------|-------------------------|
| <b>Isotope</b>                           | <b>U235</b>               | <b>U235</b>                 | <b>U235</b>                 | <b>U235</b>           | <b>U235</b>             | <b>U235</b>             |
| <b><math>\nu</math></b>                  | 0.27                      | 0.21                        | 0.06                        | 0.56                  | 0.56                    | 0.08                    |
| <b><math>\sigma_{\text{fiss}}</math></b> | 0.14                      | 0.11                        | 0.11                        | 0.26                  | 0.26                    | 0.26                    |
| <b><math>\sigma_{\text{inel}}</math></b> | 0.22                      | 0.16                        | 0.16                        | 0.32                  | 0.32                    | 0.33                    |
| <b><math>\sigma_{\text{el}}</math></b>   | 0.07                      | 0.05                        | 0.05                        | 0.11                  | 0.11                    | 0.01i                   |
| <b><math>\sigma_{\text{capt}}</math></b> | 0.51                      | 0.37                        | 0.29                        | 0.99                  | 1.01                    | 0.79                    |
| <b>Total</b>                             | <b>0.63</b>               | <b>0.47</b>                 | <b>0.36</b>                 | <b>1.22</b>           | <b>1.24</b>             | <b>0.90</b>             |
| <b>Overall <sup>(a)</sup></b>            | <b>0.64</b>               | <b>0.47</b>                 | <b>0.37</b>                 | <b>1.23</b>           | <b>1.24</b>             | <b>0.90</b>             |

<sup>(a)</sup> Total of all isotopes

# Improvements of AFCI1.2 based on the Results of AFCI1.1 Applications

In AFCI1.1, unrealistic standard deviations were observed for Cm242 reactions.

GFR Burnup Uncertainties (%)

|                        | AFCI1.1<br>diagonal | BOLNA<br>diagonal | AFCI1.1<br>full | BOLNA<br>full |
|------------------------|---------------------|-------------------|-----------------|---------------|
| Isotope                | Cm242               | Cm242             | Cm242           | Cm242         |
| $\sigma_{\text{capt}}$ | 2.92                | 0.40              | 7.03            | 0.63          |
| $\sigma_{\text{fiss}}$ | 8.17                | 3.62              | 8.17            | 6.87          |
| $\nu$                  | 1.14                | 1.07              | 1.14            | 1.83          |
| $\sigma_{\text{inel}}$ | 0.29                | 0.06              | 0.49            | 0.09          |
| Total                  | 8.75                | 3.79              | 10.85           | 7.13          |
| Overall <sup>(a)</sup> | 11.87               | 9.77              | 14.64           | 16.94         |

<sup>(a)</sup> Total of all isotopes

Cm242 Standard Deviations (%)

|     |          | Cm242: BOLNA 15Gr |                        |                        |                        | Cm242: AFCI1.1 33Gr |                        |                        |                        |
|-----|----------|-------------------|------------------------|------------------------|------------------------|---------------------|------------------------|------------------------|------------------------|
| Gr. | [MeV]    | $\nu$             | $\sigma_{\text{fiss}}$ | $\sigma_{\text{inel}}$ | $\sigma_{\text{capt}}$ | $\nu$               | $\sigma_{\text{fiss}}$ | $\sigma_{\text{inel}}$ | $\sigma_{\text{capt}}$ |
| 1   | 1.964E+1 | 10.6              | 31.5                   | 34.4                   | 52.8                   | 11.0                | 50.0                   | ↑                      | 52.8                   |
| 2   | 1.000E+1 |                   |                        |                        |                        | 11.4                | 85.5                   |                        | 157.2                  |
| 3   | 6.065E+0 | 11.1              | 52.6                   | 11.0                   | 37.4                   | 11.5                |                        | 100.0                  |                        |
| 4   | 3.679E+0 |                   |                        |                        |                        | 11.2                |                        |                        |                        |
| 5   | 2.231E+0 | 10.7              | 19.0                   | 11.4                   | 23.6                   | 11.0                |                        | ↓                      |                        |
| 6   | 1.353E+0 |                   |                        |                        |                        |                     |                        |                        |                        |
| 7   | 8.209E-1 | 5.5               | 23.4                   | 18.0                   | 19.0                   |                     |                        | 44.0                   |                        |
| 8   | 4.979E-1 |                   |                        |                        |                        |                     |                        | 10.1                   |                        |
| 9   | 3.020E-1 | 5.6               | 66.0                   | 27.2                   | 18.2                   |                     |                        | 37.0                   |                        |
| 10  | 1.832E-1 |                   |                        |                        |                        |                     | ↑                      | 53.2                   | ↑                      |
| 11  | 1.111E-1 | 5.6               | 62.7                   | 53.2                   | 20.3                   |                     |                        | 39.8                   |                        |
| 12  | 6.738E-2 |                   |                        |                        |                        |                     |                        | -                      |                        |
| 13  | 4.087E-2 | 5.6               | 28.2                   | 31.7                   | 22.4                   | ↑                   |                        | -                      |                        |
| 14  | 2.479E-2 |                   |                        |                        |                        |                     |                        | -                      |                        |
| 15  | 1.503E-2 | 5.6               | 16.2                   | -                      | 21.3                   |                     |                        | -                      |                        |
| 16  | 9.119E-3 |                   |                        |                        |                        |                     |                        | -                      |                        |
| 17  | 5.531E-3 | 5.6               | 21.0                   | -                      | 18.7                   |                     | 100.0                  | -                      | 200.0                  |
| 18  | 3.355E-3 |                   |                        |                        |                        |                     |                        | -                      |                        |
| 19  | 2.035E-3 |                   |                        |                        |                        | 10.0                |                        | -                      |                        |
| 20  | 1.234E-3 | 5.6               | 11.7                   | -                      | 6.8                    |                     |                        | -                      |                        |
| 21  | 7.485E-4 |                   |                        |                        |                        |                     |                        | -                      |                        |
| 22  | 4.540E-4 |                   |                        |                        |                        |                     |                        | -                      |                        |
| 23  | 3.043E-4 |                   |                        |                        |                        |                     |                        | -                      |                        |
| 24  | 1.486E-4 | 5.6               | 9.3                    | -                      | 4.6                    |                     | ↓                      | -                      | ↓                      |
| 25  | 9.166E-5 |                   |                        |                        |                        | ↓                   |                        | -                      |                        |
| 26  | 6.790E-5 |                   |                        |                        |                        |                     |                        | -                      |                        |
| 27  | 4.017E-5 |                   |                        |                        |                        |                     |                        | -                      |                        |
| 28  | 2.260E-5 |                   |                        |                        |                        |                     |                        | -                      |                        |
| 29  | 1.371E-5 | 5.6               | 24.0                   | -                      | 3.7                    |                     |                        | -                      |                        |
| 30  | 8.315E-6 |                   |                        |                        |                        |                     |                        | -                      |                        |
| 31  | 4.000E-6 | 5.6               | 35.6                   | -                      | 32.5                   |                     |                        | -                      |                        |
| 32  | 5.400E-7 | 5.6               | 41.2                   | -                      | 39.2                   |                     |                        | -                      |                        |
| 33  | 1.000E-7 | 5.6               | 42.6                   | -                      | 40.8                   |                     | 50.0                   | -                      |                        |

Improvements of  
AFCI1.2 based on  
the Results of  
AFCI1.1  
Applications

Argonne  
NATIONAL LABORATORY

**GFR Burnup Uncertainties (%)**

|                                          | <b>BOLNA<br/>diagonal</b> | <b>AFCI1.1<br/>diagonal</b> | <b>AFCI1.2<br/>diagonal</b> | <b>BOLNA<br/>full</b> | <b>AFCI1.1<br/>full</b> | <b>AFCI1.2<br/>full</b> |
|------------------------------------------|---------------------------|-----------------------------|-----------------------------|-----------------------|-------------------------|-------------------------|
| <b>Isotope</b>                           | <b>Cm242</b>              | <b>Cm242</b>                | <b>Cm242</b>                | <b>Cm242</b>          | <b>Cm242</b>            | <b>Cm242</b>            |
| <b><math>\sigma_{\text{capt}}</math></b> | 0.40                      | 2.92                        | 1.22                        | 0.63                  | 7.03                    | 2.73                    |
| <b><math>\sigma_{\text{fiss}}</math></b> | 3.62                      | 8.17                        | 8.17                        | 6.87                  | 8.17                    | 20.12                   |
| <b><math>\nu</math></b>                  | 1.07                      | 1.14                        | 1.14                        | 1.83                  | 1.14                    | 2.54                    |
| <b><math>\sigma_{\text{inel}}</math></b> | 0.06                      | 0.29                        | 0.30                        | 0.09                  | 0.49                    | 0.52                    |
| <b>Total</b>                             | <b>3.79</b>               | <b>8.75</b>                 | <b>8.34</b>                 | <b>7.13</b>           | <b>10.85</b>            | <b>20.46</b>            |
| <b>Overall <sup>(a)</sup></b>            | <b>9.77</b>               | <b>11.87</b>                | <b>11.58</b>                | <b>16.94</b>          | <b>14.64</b>            | <b>27.47</b>            |

<sup>(a)</sup> Total of all isotopes

## Standard Deviations (%)

| Gr. | [MeV]    | Pu238 $\sigma_{\text{fiss}}$ |         |         | Pu240 $\sigma_{\text{capt}}$ |         |         | Pu241 $\sigma_{\text{fiss}}$ |         |         | Cm244 $\sigma_{\text{fiss}}$ |         |         |
|-----|----------|------------------------------|---------|---------|------------------------------|---------|---------|------------------------------|---------|---------|------------------------------|---------|---------|
|     |          | BOLNA                        | AFCI1.1 | AFCI1.2 | BOLNA                        | AFCI1.1 | AFCI1.2 | BOLNA                        | AFCI1.1 | AFCI1.2 | BOLNA                        | AFCI1.1 | AFCI1.2 |
| 1   | 1.964E+1 | 25.2                         | 20.0    | 20.0    | 52.2                         | 55.0    | 55.0    | 24.1                         | 10.0    | 10.0    | 17.9                         | 20.0    | 20.0    |
| 2   | 1.000E+1 |                              | 20.0    | 20.0    |                              | 40.8    | 40.8    |                              | 6.5     | 6.5     |                              | 20.0    | 20.0    |
| 3   | 6.065E+0 | 20.5                         | 20.0    | 20.0    | 32.5                         | 35.0    | 35.0    | 14.2                         | 5.0     | 5.0     | 31.3                         | 20.0    | 20.0    |
| 4   | 3.679E+0 |                              | 13.8    | 13.8    |                              | 28.8    | 35.0    |                              | 5.0     | 5.0     |                              | 20.0    | 20.0    |
| 5   | 2.231E+0 | 33.8                         | 10.0    | 10.0    | 19.7                         | 25.0    | 35.0    | 21.3                         | 5.0     | 5.0     | 43.8                         | 20.0    | 20.0    |
| 6   | 1.353E+0 | 17.1                         | 50.0    | 50.0    | 16.3                         | 100.0   | 100.0   | 16.6                         | 16.6    | 15.0    | 50.0                         | 10.0    | 15.0    |
| 7   | 8.209E-1 |                              | 50.0    | 50.0    |                              | 56.5    | 56.5    |                              | 14.7    | 16.2    |                              | 10.0    | 11.9    |
| 8   | 4.979E-1 | 17.1                         | 50.0    | 50.0    | 14.3                         | 29.9    | 29.9    | 13.5                         | 13.6    | 17.0    | 36.5                         | 10.0    | 10.0    |
| 9   | 3.020E-1 |                              | 50.0    | 50.0    |                              | 17.5    | 17.5    |                              | 17.5    | 18.9    |                              | 10.0    | 10.0    |
| 10  | 1.832E-1 | 8.8                          | 50.0    | 50.0    | 13.8                         | 10.0    | 10.0    | 19.9                         | 19.9    | 20.0    | 47.6                         | 10.0    | 10.0    |
| 11  | 1.111E-1 |                              | 50.0    | 50.0    |                              | 10.0    | 10.0    |                              | 12.9    | 16.9    |                              | 10.0    | 10.0    |
| 12  | 6.738E-2 | 11.9                         | 50.0    | 50.0    | 11.3                         | 10.0    | 10.0    | 8.7                          | 8.8     | 15.0    | 26.3                         | 10.0    | 10.0    |
| 13  | 4.087E-2 |                              | 50.0    | 50.0    |                              | 10.1    | 10.0    |                              | 10.3    | 11.9    |                              | 10.0    | 10.0    |
| 14  | 2.479E-2 | 11.2                         | 50.0    | 50.0    | 10.2                         | 10.2    | 10.0    | 11.3                         | 11.3    | 10.0    | 19.0                         | 10.0    | 10.0    |
| 15  | 1.503E-2 |                              | 50.0    | 50.0    |                              | 7.0     | 6.9     |                              | 10.8    | 10.0    |                              | 10.0    | 10.0    |
| 16  | 9.119E-3 | 7.5                          | 50.0    | 50.0    | 4.4                          | 5.0     | 5.0     | 10.4                         | 10.4    | 10.0    | 11.9                         | 10.0    | 10.0    |
| 17  | 5.531E-3 |                              | 50.0    | 50.0    |                              | 5.0     | 5.0     |                              | 11.6    | 10.0    |                              | 10.0    | 12.5    |
| 18  | 3.355E-3 |                              | 50.0    | 50.0    |                              | 5.0     | 5.0     |                              | 12.3    | 10.0    |                              | 10.0    | 14.1    |
| 19  | 2.035E-3 | 4.3                          | 50.2    | 49.9    | 1.5                          | 5.0     | 5.0     | 12.7                         | 12.7    | 10.0    | 5.3                          | 10.0    | 15.0    |
| 20  | 1.234E-3 |                              | 65.3    | 39.8    |                              | 5.0     | 5.0     |                              | 16.1    | 7.5     |                              | 7.8     | 17.6    |
| 21  | 7.485E-4 |                              | 74.4    | 33.7    |                              | 5.0     | 5.0     |                              | 18.1    | 5.9     |                              | 6.5     | 19.1    |
| 22  | 4.540E-4 | 8.1                          | 80.0    | 30.0    | 1.6                          | 5.0     | 5.0     | 19.4                         | 19.4    | 5.0     | 5.7                          | 5.7     | 20.0    |
| 23  | 3.043E-4 |                              | 58.8    | 24.8    |                              | 5.2     | 4.7     |                              | 14.1    | 5.0     |                              | 9.7     | 20.0    |
| 24  | 1.486E-4 |                              | 36.7    | 19.4    |                              | 5.4     | 4.3     |                              | 8.6     | 5.0     |                              | 13.8    | 20.0    |
| 25  | 9.166E-5 |                              | 28.7    | 17.4    |                              | 5.4     | 4.2     |                              | 6.6     | 5.0     |                              | 15.3    | 20.0    |
| 26  | 6.790E-5 |                              | 25.4    | 16.6    |                              | 5.4     | 4.1     |                              | 5.8     | 5.0     |                              | 15.9    | 20.0    |
| 27  | 4.017E-5 |                              | 21.5    | 15.6    |                              | 5.5     | 4.0     |                              | 4.8     | 5.0     |                              | 16.6    | 20.0    |
| 28  | 2.260E-5 | 19.0                         | 19.0    | 15.0    | 5.5                          | 5.5     | 4.0     | 4.2                          | 4.2     | 5.0     | 17.1                         | 17.1    | 20.0    |
| 29  | 1.371E-5 |                              | 12.1    | 15.0    |                              | 3.1     | 4.0     |                              | 15.0    | 5.0     |                              | 19.4    | 20.0    |
| 30  | 8.315E-6 |                              | 7.9     | 15.0    |                              | 1.6     | 4.0     |                              | 21.6    | 5.0     |                              | 20.9    | 20.0    |
| 31  | 4.000E-6 | 4.6                          | 4.6     | 15.0    | 0.4                          | 0.4     | 4.0     | 26.8                         | 26.8    | 5.0     | 22.0                         | 22.0    | 20.0    |
| 32  | 5.400E-7 | 4.6                          | 4.6     | 5.0     | 3.2                          | 3.2     | 1.0     | 2.9                          | 2.9     | 1.0     | 26.4                         | 26.4    | 20.0    |
| 33  | 1.000E-7 | 4.9                          | 4.9     | 5.0     | 4.8                          | 4.8     | 1.0     | 3.3                          | 3.3     | 1.0     | 27.2                         | 27.2    | 20.0    |

# Standard Deviations (%)

Improvements of AFCI1.2 based on the Results of AFCI1.1 Applications

| Gr. | [MeV]    | Na $\sigma_{inel}$ |         |         | Fe56 $\sigma_{inel}$ |         |         | Pb206 $\sigma_{inel}$ |         |         | B10 $\sigma_{capt}$ |         |         |
|-----|----------|--------------------|---------|---------|----------------------|---------|---------|-----------------------|---------|---------|---------------------|---------|---------|
|     |          | BOLNA              | AFCI1.1 | AFCI1.2 | BOLNA                | AFCI1.1 | AFCI1.2 | BOLNA                 | AFCI1.1 | AFCI1.2 | BOLNA               | AFCI1.1 | AFCI1.2 |
| 1   | 1.964E+1 | 18.8               | 10.8    | 10.8    | 13.0                 | 2.6     | 5.1     | 19.8                  | 42.0    | 42.0    | 15.0                | 0.9     | 0.9     |
| 2   | 1.000E+1 |                    | 4.9     | 4.9     |                      | 2.3     | 4.5     |                       | 3.6     | 3.6     |                     | 1.2     | 1.2     |
| 3   | 6.065E+0 | 8.9                | 5.1     | 5.1     | 7.2                  | 1.4     | 2.9     | 5.5                   | 4.6     | 4.6     | 15.0                | 0.8     | 0.8     |
| 4   | 3.679E+0 |                    | 5.3     | 5.3     |                      | 1.2     | 2.4     |                       | 23.1    | 23.1    |                     | 1.2     | 1.2     |
| 5   | 2.231E+0 | 12.6               | 8.1     | 8.1     | 25.4                 | 1.4     | 2.8     | 14.2                  | 29.9    | 29.9    | 15.0                | 0.9     | 0.9     |
| 6   | 1.353E+0 | 28.0               | 11.1    | 11.1    | 16.1                 | 1.4     | 2.8     | 9.2                   | 18.4    | 18.4    | 15.0                | 0.7     | 0.7     |
| 7   | 8.209E-1 |                    | 11.6    | 11.6    |                      | -       | -       |                       | 2.2     | 2.2     |                     | 0.9     | 0.9     |
| 8   | 4.979E-1 | 50.0               | 38.3    | 38.3    | -                    | -       | -       | -                     | -       | -       | 15.0                | 1.0     | 1.0     |
| 9   | 3.020E-1 |                    | -       | -       |                      | -       | -       |                       | -       | -       |                     | 1.0     | 1.0     |
| 10  | 1.832E-1 | -                  | -       | -       | -                    | -       | -       | -                     | -       | -       | 10.0                | 1.0     | 1.0     |
| 11  | 1.111E-1 |                    | -       | -       |                      | -       | -       |                       | -       | -       |                     | 0.8     | 0.8     |
| 12  | 6.738E-2 | -                  | -       | -       | -                    | -       | -       | -                     | -       | -       | 10.0                | 0.8     | 0.8     |
| 13  | 4.087E-2 |                    | -       | -       |                      | -       | -       |                       | -       | -       |                     | 0.7     | 0.7     |
| 14  | 2.479E-2 | -                  | -       | -       | -                    | -       | -       | -                     | -       | -       | 8.0                 | 0.7     | 0.7     |
| 15  | 1.503E-2 |                    | -       | -       |                      | -       | -       |                       | -       | -       |                     | 0.7     | 0.7     |
| 16  | 9.119E-3 | -                  | -       | -       | -                    | -       | -       | -                     | -       | -       | 8.0                 | 0.7     | 0.7     |
| 17  | 5.531E-3 |                    | -       | -       |                      | -       | -       |                       | -       | -       |                     | 0.7     | 0.7     |
| 18  | 3.355E-3 | -                  | -       | -       | -                    | -       | -       | -                     | -       | -       | 5.0                 | 0.7     | 0.7     |
| 19  | 2.035E-3 |                    | -       | -       |                      | -       | -       |                       | -       | -       |                     | 0.7     | 0.7     |
| 20  | 1.234E-3 | -                  | -       | -       | -                    | -       | -       | -                     | -       | -       | 5.0                 | 0.7     | 0.7     |
| 21  | 7.485E-4 |                    | -       | -       |                      | -       | -       |                       | -       | -       |                     | 0.7     | 0.7     |
| 22  | 4.540E-4 | -                  | -       | -       | -                    | -       | -       | -                     | -       | -       | 5.0                 | 0.7     | 0.7     |
| 23  | 3.043E-4 |                    | -       | -       |                      | -       | -       |                       | -       | -       |                     | 0.7     | 0.7     |
| 24  | 1.486E-4 | -                  | -       | -       | -                    | -       | -       | -                     | -       | -       | 5.0                 | 0.7     | 0.7     |
| 25  | 9.166E-5 |                    | -       | -       |                      | -       | -       |                       | -       | -       |                     | 0.7     | 0.7     |
| 26  | 6.790E-5 | -                  | -       | -       | -                    | -       | -       | -                     | -       | -       | 5.0                 | 0.7     | 0.7     |
| 27  | 4.017E-5 |                    | -       | -       |                      | -       | -       |                       | -       | -       |                     | 0.7     | 0.7     |
| 28  | 2.260E-5 | -                  | -       | -       | -                    | -       | -       | -                     | -       | -       | 5.0                 | 0.7     | 0.7     |
| 29  | 1.371E-5 |                    | -       | -       |                      | -       | -       |                       | -       | -       |                     | 0.7     | 0.7     |
| 30  | 8.315E-6 | -                  | -       | -       | -                    | -       | -       | -                     | -       | -       | 3.0                 | 0.7     | 0.7     |
| 31  | 4.000E-6 |                    | -       | -       |                      | -       | -       |                       | -       | -       |                     | 0.7     | 0.7     |
| 32  | 5.400E-7 | -                  | -       | -       | -                    | -       | -       | -                     | -       | -       | 1.0                 | 0.7     | 0.7     |
| 33  | 1.000E-7 | -                  | -       | -       | -                    | -       | -       | -                     | -       | -       | 1.0                 | 0.7     | 0.7     |

# *Sodium Cooled Fast Neutron Systems: Nominal Values and Total Uncertainties (%)*

| Reactor   |               | Multiplication Factor | Power Peaking Factor | Doppler Coefficient     | Coolant Void Worth        | Burnup Reactivity Swing <sup>(a)</sup> |
|-----------|---------------|-----------------------|----------------------|-------------------------|---------------------------|----------------------------------------|
| ABR Metal | Nominal Value | 0.972326              |                      |                         | 1402 pcm <sup>(1)</sup>   |                                        |
|           | BOLNA         | 1.47                  |                      |                         | 13.10                     |                                        |
|           | AFCI1.1       | 1.22                  |                      |                         | 9.10                      |                                        |
|           | AFCI1.2       | 1.54                  |                      |                         | 10.32                     |                                        |
| ABR Oxide | Nominal Value | 0.988232              |                      |                         | 2443 pcm <sup>(2)</sup>   |                                        |
|           | BOLNA         | 1.44                  |                      |                         | 7.82                      |                                        |
|           | AFCI1.1       | 1.08                  |                      |                         | 5.38                      |                                        |
|           | AFCI1.2       | 1.49                  |                      |                         | 5.60                      |                                        |
| SFR       | Nominal Value | 1.05280               | 1.53 <sup>(3)</sup>  | 231 pcm <sup>(4)</sup>  | 1831 pcm <sup>(5)</sup>   | -3981.1 pcm <sup>(6)</sup>             |
|           | BOLNA         | 1.86                  | 0.45                 | 5.57                    | 17.11                     | 3.55                                   |
|           | AFCI1.1       | 1.09                  | 0.19                 | 3.92                    | 10.88                     | 1.94                                   |
|           | AFCI1.2       | 2.16                  | 0.22                 | 6.88                    | 14.02                     | 4.25                                   |
| EFR       | Nominal Value | 1.10848               | 1.63 <sup>(7)</sup>  | 1289 pcm <sup>(8)</sup> | 1934.5 pcm <sup>(9)</sup> | -9123.9 pcm <sup>(10)</sup>            |
|           | BOLNA         | 1.27                  | 1.18                 | 3.80                    | 7.83                      | 3.49                                   |
|           | AFCI1.1       | 1.15                  | 0.96                 | 3.50                    | 5.10                      | 1.58                                   |
|           | AFCI1.2       | 1.29                  | 1.01                 | 4.03                    | 5.40                      | 3.43                                   |

<sup>(a)</sup> The uncertainties show the component due to cross section uncertainties  
(the component due to the isotope buildup is not taken into account)

|                                                                                                                                    |                                                                                                                                                                                                       |                                                                                                                                                                                                                    |
|------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>ABR Metal</b><br><sup>(1)</sup> Na loss at the core center<br><br><b>ABR Oxide</b><br><sup>(2)</sup> Na loss at the core center | <b>SFR</b><br><sup>(3)</sup> (R , Z) =(66.59 , 143.03) <sub>cm</sub><br><sup>(4)</sup> T <sub>fuel</sub> =300K - T <sub>fuel</sub> =850K<br><sup>(5)</sup> Na loss in core<br><sup>(6)</sup> 155 days | <b>EFR</b><br><sup>(7)</sup> (R , Z) =(153.24 , 125) <sub>cm</sub><br><sup>(8)</sup> T <sub>fuel</sub> =300K - T <sub>fuel</sub> =1520K<br><sup>(9)</sup> Na loss in core and blanket<br><sup>(10)</sup> 1700 days |
|------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|



## Fast Neutron Systems: Nominal Values and Total Uncertainties (%)

| Reactor |               | Multiplication Factor | Power Peaking Factor | Doppler Coefficient      | Coolant Void Worth         | Burnup Reactivity Swing <sup>(a)</sup> |
|---------|---------------|-----------------------|----------------------|--------------------------|----------------------------|----------------------------------------|
| GFR     | Nominal Value | 1.01049               | 1.45 <sup>(1)</sup>  | 1549 pcm <sup>(2)</sup>  | 350.1 pcm <sup>(3)</sup>   | 1081.3 pcm <sup>(4)</sup>              |
|         | BOLNA         | 1.89                  | 1.68                 | 5.51                     | 7.67                       | 16.94                                  |
|         | AFCI1.1       | 1.66                  | 1.66                 | 4.67                     | 6.47                       | 14.64                                  |
|         | AFCI1.2       | 1.95                  | 1.71                 | 5.44                     | 6.75                       | 27.47                                  |
| LFR     | Nominal Value | 1.00023               | 1.29 <sup>(5)</sup>  | 228.1 pcm <sup>(6)</sup> | 6575.5 pcm <sup>(7)</sup>  | -1464 pcm <sup>(8)</sup>               |
|         | BOLNA         | 1.40                  | 0.64                 | 4.35                     | 7.18                       | 2.42                                   |
|         | AFCI1.1       | 1.19                  | 0.31                 | 7.96                     | 9.05                       | 1.62                                   |
|         | AFCI1.2       | 1.67                  | 0.58                 | 6.20                     | 9.81                       | 3.39                                   |
| ABMAB   | Nominal Value | 0.94816               | 2.67 <sup>(9)</sup>  | 28.3 pcm <sup>(10)</sup> | 3138.4 pcm <sup>(11)</sup> | -1347.6 pcm <sup>(12)</sup>            |
|         | BOLNA         | 2.90                  | 21.42                | -                        | 15.49                      | 56.63                                  |
|         | AFCI1.1       | 1.22                  | 9.07                 | -                        | 11.37                      | 48.69                                  |
|         | AFCI1.2       | 2.46                  | 17.99                | -                        | 13.89                      | 105.11                                 |

<sup>(a)</sup> The uncertainties show the component due to cross section uncertainty  
(the component due to the isotope buildup is not taken into account)

|                                                                                                                                                                                                               |                                                                                                                                                                                                        |                                                                                                                                                                                                            |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>GFR</b><br><sup>(1)</sup> Center core radially and axially<br><sup>(2)</sup> T <sub>fuel</sub> =300K - T <sub>fuel</sub> =1263K<br><sup>(3)</sup> He loss in core and reflector<br><sup>(4)</sup> 415 days | <b>LFR</b><br><sup>(5)</sup> (R , Z) =(100.96 , 117.90) <sub>cm</sub><br><sup>(6)</sup> T <sub>fuel</sub> =300K - T <sub>fuel</sub> =900K<br><sup>(7)</sup> Pb loss in core<br><sup>(8)</sup> 310 days | <b>ADMAB</b><br><sup>(9)</sup> (R , Z) =(20 , 102.5) <sub>cm</sub><br><sup>(10)</sup> T <sub>fuel</sub> =1773K - T <sub>fuel</sub> =980K<br><sup>(11)</sup> Pb-Bi loss in core<br><sup>(12)</sup> 366 days |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

*Isotope/Reaction Contributing to 90% of Multiplication Factor Uncertainty with AFCI1.2*

|                        |           | ABR Metal | ABR Oxide | SFR  | EFR  | GFR  | LFR  | ADMAB |
|------------------------|-----------|-----------|-----------|------|------|------|------|-------|
| U238                   | inelastic | 1.00      | 0.78      |      | 0.90 | 1.49 | 0.74 |       |
| U238                   | capture   |           |           |      | 0.25 |      |      |       |
| Pu238                  | fission   | 0.56      | 0.57      | 1.36 | 0.34 | 0.53 | 0.94 | 0.53  |
| Pu239                  | capture   |           |           |      | 0.25 |      |      |       |
| Pu240                  | nu        | 0.31      | 0.31      | 0.42 | 0.27 |      | 0.34 |       |
| Pu240                  | fission   | 0.28      | 0.30      |      |      |      |      |       |
| Pu240                  | capture   |           | 0.30      | 0.46 | 0.34 |      | 0.39 |       |
| Pu241                  | fission   | 0.67      | 0.77      | 1.02 | 0.39 | 0.79 | 0.64 | 1.05  |
| Am241                  | fission   |           |           |      |      |      |      | 0.94  |
| Am241                  | capture   |           |           |      |      |      |      | 0.79  |
| Am242m                 | fission   |           |           | 0.69 |      |      |      |       |
| Am243                  | fission   |           |           |      |      |      |      | 0.44  |
| Cm244                  | nu        |           |           |      |      |      |      | 0.50  |
| Cm244                  | fission   |           |           |      |      |      |      | 0.65  |
| Cm245                  | fission   |           |           | 0.43 |      |      |      | 1.09  |
| Pb206                  | inelastic |           |           |      |      |      | 0.41 |       |
| Total <sup>(a)</sup>   |           | 1.39      | 1.35      | 1.98 | 1.18 | 1.77 | 1.51 | 2.22  |
| Overall <sup>(b)</sup> |           | 1.54      | 1.49      | 2.16 | 1.29 | 1.95 | 1.67 | 2.46  |

<sup>(a)</sup> Total uncertainty yield by the cross sections listed in the Table;

<sup>(b)</sup> Overall uncertainty yield by all cross sections.

## Isotope/Reaction Contributing to 90% of Multiplication Factor Uncertainty with BOLNA

|         |           | ABR Metal | ABR Oxide | SFR  | EFR  | GFR  | LFR  | ADMAB |
|---------|-----------|-----------|-----------|------|------|------|------|-------|
| U238    | inelastic | 0.97      | 0.76      |      | 0.87 | 1.42 | 0.73 |       |
| U238    | capture   | 0.28      | 0.33      |      | 0.37 | 0.41 | 0.25 |       |
| Pu238   | nu        |           |           | 0.36 |      |      | 0.23 |       |
| Pu238   | fission   | 0.22      |           | 0.56 |      |      | 0.34 |       |
| Pu239   | capture   |           |           |      | 0.25 |      |      |       |
| Pu240   | nu        | 0.30      | 0.31      | 0.41 | 0.27 |      | 0.33 |       |
| Pu240   | fission   | 0.27      | 0.26      |      |      |      | 0.29 |       |
| Pu240   | capture   |           | 0.25      |      | 0.26 |      | 0.27 |       |
| Pu241   | fission   | 0.65      | 0.77      | 1.01 | 0.39 | 0.82 | 0.61 | 1.04  |
| Pu242   | fission   |           |           | 0.38 |      |      |      |       |
| Am241   | fission   |           |           |      |      |      |      | 0.82  |
| Am242m  | fission   |           |           | 0.77 |      |      |      |       |
| Cm244   | fission   |           |           | 0.41 |      |      |      | 1.90  |
| Cm245   | fission   |           | 0.26      | 0.41 |      |      | 0.22 | 1.04  |
| Fe56    | inelastic | 0.35      | 0.35      | 0.46 |      |      |      | 0.83  |
| C       | elastic   |           |           |      |      | 0.31 |      |       |
| O16     | capture   |           |           |      | 0.29 |      |      |       |
| B10     | capture   |           |           |      |      |      | 0.44 |       |
| Total   |           | 1.33      | 1.30      | 1.71 | 1.16 | 1.72 | 1.28 | 2.67  |
| Overall |           | 1.47      | 1.44      | 1.86 | 1.27 | 1.89 | 1.40 | 2.90  |

Pu238 Fission, Pu240 Capture, Pb206 Inelastic are much larger with AFCI1.2

Pu241 Fission, Cm244 Fission, Na Inelastic, Fe56 Inelastic, B10 Capture are much larger with BOLNA

## Conclusions

The present work shows the first application of the recent AFCI1.2 matrix, with the determination of the uncertainty for the main integral parameters (multiplication factor, power peaking factor, Doppler reactivity coefficient, coolant void reactivity worth and burnup reactivity swing) of a series of fast reactors (ABR metal core, ABR oxide core, SFR, EFR, GFR, LFR, ADMAB). The obtained AFCI1.2 parameter uncertainties are also compared with the results presented in previous studies with the BOLNA correlation matrix.

The impact in terms of parameters uncertainties of the improvements made in the AFCI1.2 matrix with respect to the previous matrix AFCI1.1 has been analyzed.

In AFCI1.2, all covariance data related to the reactions from the Maslov evaluations have been completed with the inclusion of energy correlation terms that were missing in AFCI1.1.

With AFCI1.2 data, U235 capture has reduced standard deviations in the energy range 2 keV - 0.2 MeV compared to the AFCI1.1 data but it still brings a large component of uncertainty (0.8%) on the GODIVA multiplication factor because of the strong effects associated to the energy correlation terms.

With AFCI1.2 data, the component of uncertainty from Cm242 capture (which is relevant for parameters like the GFR burnup reactivity swing) is decreased compared to AFCI1.1 because of the reduced standard deviations, however large uncertainties are still associated with Cm242 fission.

As with AFCI1.1 data, compared to the BOLNA results the use of AFCI1.2 data yields much larger components of uncertainty from Pu238 fission, Pu240 capture and Pb206 inelastic, while smaller uncertainties are obtained from Pu241 fission, Cm244 fission, Na inelastic, Fe56 inelastic, B10 capture.

The overall parameter uncertainties estimated with AFCI1.2 data generally are larger than the AFCI1.1 uncertainties (the biggest effects, especially for SFR and ADMAB, show even a factor of 2) and quite comparable with the BOLNA results (except for parameters like GFR or ADMAB burnup reactivity).