

**$^{33}\text{Na}$   $\beta^-$  decay (8.1 ms)    2001Nu02,1984Gu19**

Type	Author	History	Citation	Literature Cutoff Date
Full Evaluation	Jun Chen and Balraj Singh		NDS 199,1 (2025)	30-Sep-2024

Parent:  $^{33}\text{Na}$ :  $E=0.0$ ;  $J^\pi=(3/2^+)$ ;  $T_{1/2}=8.1$  ms 3;  $Q(\beta^-)=18.82\times 10^3$  45;  $\% \beta^-$  decay=100

$^{33}\text{Na}$ - $Q(\beta^-)$ : from 2021Wa16.

$^{33}\text{Na}$ - $J^\pi, T_{1/2}$ : From the Adopted Levels of  $^{33}\text{Na}$ .

$^{33}\text{Na}$ - $\% \beta^-$  decay:  $\% \beta^- n=47$  6,  $\% \beta^- 2n=13$  3 (2001Nu02,2002Ra16).

2001Nu02, 2002Ra16 (also 2002Nu02,2004Co29):  $^{33}\text{Na}$  source was produced in fragmentation reactions by 1.4 GeV protons from the PS/Booster at CERN impinging on a uranium-carbide target. Fragments were ionized, accelerated and mass separated by the ISOLDE facility, and then transported to the experimental setup.  $\gamma$  rays were detected with two large-volume Ge detectors;  $\beta$  particles were detected with a thin plastic scintillator detector;  $\beta$ -delayed neutrons were detected with eight low-threshold neutron detectors. Measured  $E_\gamma$ ,  $I_\gamma$ ,  $E_\beta$ ,  $I_\beta$ ,  $\gamma\gamma$ -coin,  $\beta\gamma$ -coin,  $\beta\gamma\gamma$ -coin,  $\beta n\gamma$ -coin,  $n\gamma$ -coin,  $\beta(t)$ ,  $\gamma(t)$ ,  $\beta n(t)$ . Deduced levels,  $J$ ,  $\pi$ , parent  $T_{1/2}$ ,  $\beta$ -decay branching ratios,  $\log ft$ ,  $\beta$ -delayed neutron emission probabilities. Comparisons with shell-model calculations.

1984Gu19: Na isotopes were produced in the fragmentation of a 30 g/cm<sup>2</sup> iridium target by 10 GeV protons from CERN synchrotron.  $\gamma$  rays were detected with two Ge(Li) detectors and  $\beta$  particles were detected with a thin 2 $\pi$  plastic scintillator. Measured  $E_\gamma$ ,  $I_\gamma$ ,  $E_\beta$ ,  $I_\beta$ ,  $\gamma\gamma$ -coin,  $\beta\gamma\gamma$ -coin. Four unplaced  $\gamma$  rays reported.

1984La03: similar setup as that in 1984Gu19, plus a 4 $\pi$  liquid-scintillator neutron detector. Measured  $\beta$ -delayed neutrons. Deduced parent  $T_{1/2}$ ,  $\beta$ -delayed neutron emission probabilities.

1998NoZW:  $^{33}\text{Na}$  source was produced by fragmentation of a 95 MeV/nucleon  $^{40}\text{Ar}$  beam from the RIKEN Ring Cyclotron and separated by the RIPS separator.  $\beta$  particles were detected with silicon detectors. Measured  $\beta(t)$ . Deduced parent  $T_{1/2}$ .

$^{33}\text{Na}$  also decays to  $^{31}\text{Mg}$  by  $\beta^- 2n$  (13% 3) and to  $^{32}\text{Mg}$  by  $\beta^- n$  (47% 6) (2001Nu02).

All data are from 2001Nu02, unless otherwise stated.

The data on neutron energies are not available in detail to deduce all the level energies in  $^{33}\text{Mg}$  populated by  $^{33}\text{Na}$   $\beta$  decay.

Several  $\gamma$  rays are unplaced and there still could be unobserved transitions in the large energy gap allowed by the  $Q(\beta^-)$  value, indicating that the level scheme is incomplete.

 $^{33}\text{Mg}$  Levels

E(level) <sup>†</sup>	$J^\pi$ <sup>‡</sup>	$T_{1/2}$	Comments
0.0	$3/2^-$	90.3 ms 10	$J^\pi$ : 2001Nu02 proposed $(3/2^+)$ . $T_{1/2}$ : from the Adopted Levels.
158.8? 5			E(level): 2001Nu02 proposed a level at 158 keV with $J^\pi=(7/2^-)$ from tentative placement of 546 $\gamma$ from 705 level to a 158 level, but no $\gamma$ decay from this level was reported. The 546.2 $\gamma$ is now placed from a level of this energy, thus the existence of 158 level is suspect and it has been omitted in Adopted Levels.
484.11 8	$(5/2^-)$		$J^\pi$ : 2001Nu02 proposed $(3/2)^-$ .
546.21 10	$(3/2^-)$		
705.01 8	$(3/2, 5/2^+)$		$J^\pi$ : 2001Nu02 proposed $(5/2^+)$ .
1242.42 11	$(1/2^-, 3/2^-)$		$J^\pi$ : 2001Nu02 proposed $(1/2^+)$ .
3780 <sup>#</sup>			E(level): from neutron group at 800 60 keV.
4000 <sup>#</sup>			E(level): from neutron group at 1020 80 keV.
2280+x			E(level): $x < 16540$ 450 from $Q(\beta^-)(^{33}\text{Na})\text{-S}(n)(^{33}\text{Mg})$ , where $Q(\beta^-)=18820$ 450 and $\text{S}(n)=2280$ 4 from 2021Wa16. This represents a range of unobserved levels that subsequently decay to $^{32}\text{Mg}$ via one-neutron emission, including 3780 and 4000 levels above.
8058+y			E(level): $y < 10760$ 450 from $Q(\beta^-)(^{33}\text{Na})\text{-S}(2n)(^{33}\text{Mg})$ , where $\text{S}(2n)=8058$ 4 from 2021Wa16. This represents a range of unobserved levels that subsequently decay to $^{31}\text{Mg}$ via two-neutron emission.

<sup>†</sup> From a least-squares fit to  $\gamma$ -ray energies, unless otherwise noted.

<sup>‡</sup> From the Adopted Levels.

<sup>#</sup> Decays to  $^{32}\text{Mg}$  by neutron emission.

**$^{33}\text{Na}$   $\beta^-$  decay (8.1 ms) 2001Nu02,1984Gu19 (continued)** $\beta^-$  radiations

E(decay)	E(level)	$I\beta^-$ <sup>‡</sup>	Log $ft$	Comments
( $5 \times 10^3$ @ 5)	8058+y	13 3		$I\beta^-$ : from adopted $\% \beta^- 2n=13.3$ for the decay of $^{33}\text{Na}$ g.s. (2001Nu02,2002Ra16).
( $8 \times 10^3$ @ 8)	2280+x	47 6		$I\beta^-$ : from adopted $\% \beta^- n=47.6$ for the decay of $^{33}\text{Na}$ g.s. (2001Nu02,2002Ra16).
( $1.76 \times 10^4$ 5)	1242.42	$2.9^{\dagger}_{12}$	$5.8^{\dagger}$	av $E\beta=8.45 \times 10^3$ 22
( $1.81 \times 10^4$ 5)	705.01	$7.0^{\dagger}_{26}$	$5.5^{\dagger}$	av $E\beta=8.71 \times 10^3$ 22
( $1.83 \times 10^4$ 5)	546.21	$8.8^{\dagger}_{33}$	$5.4^{\dagger}$	av $E\beta=8.79 \times 10^3$ 22
( $1.83 \times 10^4$ # 5)	484.11	$<1.5^{\dagger}$	$>6.2^{\dagger}$	av $E\beta=8.83 \times 10^3$ 22
( $1.88 \times 10^4$ # 5)	0.0	20 10	5.0	av $E\beta=9.06 \times 10^3$ 22
$I\beta^-$ , Log $ft$ : branching ratio is from $100 - \% \beta^- n - \% \beta^- 2n - \Sigma I(\gamma \text{ to g.s.})$ and considered as upper limit and log $ft$ as lower limit, due to possible unobserved $\gamma$ transitions and levels. Parent $J^\pi=(3/2^+)$ of $^{33}\text{Na}$ indicates a forbidden decay to this $3/2^-$ g.s. in $^{33}\text{Mg}$ , which would expect a much higher log $ft$ value than 5.1 quoted here. This supports that there are unobserved feedings and the deduced g.s. feeding of 20 10 might be attributed mostly to them. Due to the forbidden nature and possible unobserved feedings, the evaluators consider this decay branch with a large feeding questionable.				

<sup>†</sup>  $\beta$  branching ratios are from  $\gamma$ -ray intensity imbalance and considered by the evaluators as upper limits due to possible unobserved transitions and associated log  $ft$  values as lower limits.

<sup>‡</sup> Absolute intensity per 100 decays.

# Existence of this branch is questionable.

@ Estimated for a range of levels.

 $\gamma(^{33}\text{Mg})$ 

$I_\gamma$  normalization: Deduced by 2001Nu02 from absolute  $\gamma$ -intensity measurements using the activity of well-known  $^{26}\text{Na}$  as standard, simultaneous detection of  $\beta$  and  $\gamma$  rays, and efficiencies of  $\beta^-$ - and  $\gamma$ -detectors.

$E_\gamma$ <sup>†</sup>	$I_\gamma$ <sup>†#</sup>	$E_i(\text{level})$	$J_i^\pi$	$E_f$	$J_f^\pi$	Comments
221.0 1	8.7 10	705.01	(3/2,5/2 <sup>+</sup> )	484.11	(5/2 <sup>-</sup> )	$\%I_\gamma=1.9.7$ $E_\gamma, I_\gamma$ : doublet. The second component is assigned to a transition in $^{31}\text{Mg}$ populated by $^{33}\text{Na}$ $\beta^- 2n$ decay.
$^{x}297.9^{\dagger}_{12}$ 1	4.0 4					$\%I_\gamma=0.88.33$
484.1 1	18.7 19	484.11	(5/2 <sup>-</sup> )	0.0	3/2 <sup>-</sup>	$\%I_\gamma=4.1.16$ Other: $E_\gamma=484.9.10$ , $I_\gamma=14.11$ (1984Gu19).
546.2 1	40 4	546.21	(3/2 <sup>-</sup> )	0.0	3/2 <sup>-</sup>	$\%I_\gamma=8.8.33$ 2001Nu02 considered different scenarios for the placement of 546 $\gamma$ and proposed placement from 705 level to a 159 level as the probable one, which is also adopted by 2021Ba28 in $^9\text{Be}(^{34}\text{Mg}, ^{33}\text{Mg}\gamma)$ without further supporting evidence. However, this $\gamma$ could also define a level of this energy, a possibility which 2001Nu02 considered less likely based on rather weak arguments. 2006El03 observed a 561.17 $\gamma$ in $^1\text{H}(^{34}\text{Mg}, ^{33}\text{Mg}\gamma)$ , which they suggested was most likely the same as 546.2 $\gamma$ in decay work, but no 704.9 $\gamma$ was seen in that study, which may imply that 546.2 $\gamma$ and 704.9 $\gamma$ de-excite different levels. Moreover, the non-observation of this 546 $\gamma$ and observations of 220 $\gamma$ and 703 $\gamma$ from 703 level

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$^{33}\text{Na}$   $\beta^-$  decay (8.1 ms) [2001Nu02,1984Gu19](#) (continued) $\gamma(^{33}\text{Mg})$  (continued)

$E_\gamma$ <sup>†</sup>	$I_\gamma$ <sup>†#</sup>	$E_i(\text{level})$	$J_i^\pi$	$E_f$	$J_f^\pi$	Comments
						by <a href="#">2017Ri06</a> in $^9\text{Be}(^{46}\text{Ar}, ^{33}\text{Mg}\gamma)$ , and the observations of all those three transitions by <a href="#">2021Ba28</a> with 546 $\gamma$ much stronger than 703 $\gamma$ further support that 546 $\gamma$ and 703 $\gamma$ deexcite different levels. Therefore a level at 546.2 keV has been defined in Adopted Levels by the evaluators and is also adopted here and the placement from 705 level is considered as questionable. Other: $E_\gamma=546.5$ 10, $I_\gamma=40$ 13 ( <a href="#">1984Gu19</a> ). $E_\gamma$ : tentative placement ( <a href="#">2001Nu02</a> ), but the evaluators suggest that the main placement is from 546 level. See comments at 546.2 $\gamma$ from 546 level.
546.2@		705.01	(3/2,5/2 <sup>+</sup> )	158.8?		
704.9 1	23.2 21	705.01	(3/2,5/2 <sup>+</sup> )	0.0	3/2 <sup>-</sup>	% $I_\gamma=5.1$ 19 Other: $E_\gamma=704.3$ 10, $I_\gamma=23$ 11 ( <a href="#">1984Gu19</a> ).
758.2 1	6.1 7	1242.42	(1/2 <sup>-</sup> ,3/2 <sup>-</sup> )	484.11	(5/2 <sup>-</sup> )	% $I_\gamma=1.3$ 5
<sup>x</sup> 845.7 <sup>‡</sup> 2	2.5 4					% $I_\gamma=0.55$ 22
<sup>x</sup> 1011.3 <sup>‡</sup> 2	1.6 4					% $I_\gamma=0.35$ 16
1242.8 2	7.1 19	1242.42	(1/2 <sup>-</sup> ,3/2 <sup>-</sup> )	0.0	3/2 <sup>-</sup>	% $I_\gamma=1.6$ 7 Other: $E_\gamma=1242.6$ 18, $I_\gamma=26$ 10 ( <a href="#">1984Gu19</a> ).
<sup>x</sup> 1857.7 <sup>‡</sup> 4	4.1 6					% $I_\gamma=0.9$ 4
<sup>x</sup> 1976.9 5	6.7 19					% $I_\gamma=1.5$ 7
<sup>x</sup> 2236.9 5	7.0 9					% $I_\gamma=1.5$ 6

<sup>†</sup> From [2001Nu02](#). Intensities are relative to 100 for 885.3 $\gamma$  in  $^{32}\text{Mg}$  populated in  $\beta^-n$  decay of  $^{33}\text{Na}$ .

<sup>‡</sup> The evaluators note that 1857.7-1011.3=846.4, which matches the gamma energy of 845.7 2 within the uncertainty range and may suggest a level at 1011.3+845.7=1856 and another level either at 1011 or 846. Also, 845.7-297.9=547.8 which is close in energy to 546.2 $\gamma$ .

# For absolute intensity per 100 decays, multiply by 0.22 8.

@ Placement of transition in the level scheme is uncertain.

<sup>x</sup>  $\gamma$  ray not placed in level scheme.

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## Decay Scheme

Intensities:  $I_{(\gamma+ce)}$  per 100 parent decays

## Legend

- $I_\gamma < 2\% \times I_\gamma^{max}$
- $I_\gamma < 10\% \times I_\gamma^{max}$
- $I_\gamma > 10\% \times I_\gamma^{max}$
- - - - -→  $\gamma$  Decay (Uncertain)
- Coincidence

