

Coulomb excitation 2020Bu01

Type	Author	History	Citation	Literature Cutoff Date
Full Evaluation	Balraj Singh, M. S. Basunia, Jun Chen et al. ,		NDS 192,315 (2023)	25-Sep-2023

Dataset prepared by Balraj Singh, Jun Chen, and IAEA-ICTP-workshop participants: Diwanshu and B. Rohila.

2020Bu01 (also [2020Bu20](#), [2019Bu29](#)): 4.31 MeV/nucleon ^{222}Ra beam obtained in spallation reaction by bombarding uranium carbide target with 1.4-GeV protons from the CERN PS Booster, followed by extraction of ions from a tungsten surface ion source, stripped to 51^+ charge state, and accelerated in HIE-ISOLDE. Targets was 2.1 mg/cm² thick ^{60}Ni and ^{120}Sn . γ rays were detected using Miniball array of 24 HPGe, sixfold segmented detectors, arranged in eight triple clusters. Scattered projectiles and target recoils were detected in a highly segmented silicon detector. Measured $E\gamma$, $E(\text{X-ray})$, $I\gamma$, (recoils) γ -coin, γ -ray yields. Deduced levels, J , π , band structures, matrix elements and corresponding intrinsic electric (quadrupole, octupole, dipole) moments using GOSIA code. Systematics of neighboring Ra isotopes.

A total of 114 experimental yields for ^{222}Ra were fitted to 42 variables, with random (but within reasonable limits) initial values for each of the freely varied matrix elements. The E4 matrix elements were also considered in the fitting procedure, by assuming the rotational model and a constant value of the hexadecapole moment obtained from the theoretical values for β_4 . For ^{222}Ra , observed E3 matrix elements consistent with pear shape and stable octupole deformation.

 ^{222}Ra Levels

Units of matrix elements (M.E.): $eb^{1/2}$ for E1, eb for E2 and $eb^{3/2}$ for E3. Values of E1 matrix elements are from supplemental material of [2020Bu01](#).

$B(E1)$, $B(E2)$, and $B(E3)$ values deduced by evaluators from corresponding transitional matrix elements $M(E\lambda)$ (from J) using $B(E\lambda)\uparrow(\text{from } J)=[M(E\lambda)]^2/(2J+1)$. Units are: eb for $B(E1)$, e^2b^2 for $B(E2)$ and e^3b^3 for $B(E3)$.

Q_0 (rotational model)=5.78 eb [18](#) ([2020Bu01](#)); weighted average of all the experimental values.

O_0 (rotational model)=3.12 $eb^{3/2}$ [19](#) ([2020Bu01](#)); weighted average of all the experimental values.

E(level) [†]	$J^\pi @$	$T_{1/2} &$	Comments
0.0 ^a	0^+		
111 ^a	2^+		$Q=-0.75 +29-28$ Q: from diagonal E2 M.E. $(111,2^+ \rightarrow 111,2^+) = -1.3$ 5. Intrinsic electric quadrupole moment (Q_0)=3.3 eb 14 .
242 ^b	1^-	9.5 ps +21-16	$T_{1/2}$: deduced from $B(E1)\uparrow(0,0^+ \rightarrow 242,1^-) = 0.000067 +12-11$. Other: 9.6 ps +24-36 from $B(E1)\uparrow(111,2^+ \rightarrow 242,1^-) = 0.000026 +13-4$. Note that the contribution from the experimental $B(E3)$ value for the 131-keV transition is negligible as deduced from $B(E3,131\gamma)/B(E1,242\gamma)$ ratio. E1 M.E. $(0,0^+ \rightarrow 242,1^-) = +0.0082$ 7; $B(E1)\uparrow = 0.000067 +12-11$. E1 M.E. $(111,2^+ \rightarrow 242,1^-) = -0.0114 +9-25$; $B(E1)\uparrow = 0.000026 +13-4$. E3 M.E. $(111,2^+ \rightarrow 242,1^-) = +0.85$ 24; $B(E3)\uparrow = 0.15 +9-7$. Intrinsic E1 moment: $D_0(0,0^+ \rightarrow 242,1^-) = 0.0168 eb^{1/2}$ 14 . Intrinsic E1 moment: $D_0(111,2^+ \rightarrow 242,1^-) = 0.0165 eb^{1/2} +37-13$. Intrinsic E3 moment: $O_0(111,2^+ \rightarrow 242,1^-) = 2.00 eb^{3/2}$ 60 . $Q=-1.59 +29-28$ Q: from diagonal E2 M.E. $(301,4^+ \rightarrow 301,4^+) = -2.8$ 5.
301 ^a	4^+	135 ps +17-14	$T_{1/2}$: deduced from $B(E2)(111,2^+ \rightarrow 301,4^+) = 1.78$ 18 . Note that the contribution from the experimental $B(E3)$ value for the 59-keV transition is negligible as deduced from $\beta(E3,59\gamma)/\beta(E2,190\gamma)$ ratio. E2 M.E. $(111,2^+ \rightarrow 301,4^+) = +2.98$ 15 , coupled to $0^+ \rightarrow 2^+$ M.E.; $B(E2)\uparrow = 1.78$ 18 . E3 M.E. $(242,1^- \rightarrow 301,4^+) = -2.1$ 5, coupled to higher-lying matrix elements; $B(E3)\uparrow = 0.49 +26-21$. Intrinsic E2 moment: $Q_0(301,4^+ \rightarrow 301,4^+) = 5.80 eb$ 10 . Intrinsic E2 moment: $Q_0(111,2^+ \rightarrow 301,4^+) = 5.90 eb$ 30 . Intrinsic E3 moment: $O_0(242,1^- \rightarrow 301,4^+) = 4.4 eb^{3/2}$ 10 . $Q=-1.59 +29-28$ Q: from diagonal E2 M.E. $(301,4^+ \rightarrow 301,4^+) = -2.8$ 5.
317 ^b	3^-	4.7 ps +26-14	$T_{1/2}$: deduced from $B(E1)(111,2^+ \rightarrow 317,3^-) = 0.000135 +57-47$. Other: 4.7 ps +34-18 from

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Coulomb excitation **2020Bu01 (continued)** ^{222}Ra Levels (continued)

E(level) [†]	J ^π @	T _{1/2} &	Comments
			B(E2)(242,1 ⁻ → 317,3 ⁻)=1.84 +36–48. Note that contributions from the experimental B(E1) and B(E3) values for the 15.8-keV transition, and experimental B(E3) values for the 206- and 317-keV transitions are negligible as deduced from respective ratios of transition probabilities.
			E1 M.E. (111,2 ⁺ → 317,3 ⁻)=+0.026 5; B(E1)↑=0.000135 +57–47. E1 M.E. (301,4 ⁺ → 317,3 ⁻)=-0.027 26; B(E1)↑=0.0000810 +2311–809. E2 M.E. (242,1 ⁻ → 317,3 ⁻)=+2.35 22; B(E2)↑=1.84 +36–48. E3 M.E. (0,0 ⁺ → 317,3 ⁻)=+1.13 9; B(E3)↑=1.28 +21–41. E3 M.E. (111,2 ⁺ → 317,3 ⁻)=-0.9 5; B(E3)↑=0.16 +23–13. E3 M.E. (301,4 ⁺ → 317,3 ⁻)=+2.6 +6–9, coupled to higher-lying matrix elements; B(E3)↑=0.75 +39–43. Intrinsic E1 moment: D ₀ (111,2 ⁺ → 317,3 ⁻)=0.031 eb ^{1/2} 6. Intrinsic E1 moment: D ₀ (301,4 ⁺ → 317,3 ⁻)=0.028 eb ^{1/2} 26. Intrinsic E2 moment: Q ₀ (242,1 ⁻ → 317,3 ⁻)=5.60 eb 50. Intrinsic E3 moment: O ₀ (0,0 ⁺ → 317,3 ⁻)=3.03 eb ^{3/2} 24. Intrinsic E3 moment: O ₀ (111,2 ⁺ → 317,3 ⁻)=2.1 eb ^{3/2} 12. Intrinsic E3 moment: O ₀ (301,4 ⁺ → 317,3 ⁻)=5.5 eb ^{3/2} +13–18.
474 ^b	5 ⁻	24 ps +5–9	T _{1/2} : deduced from B(E1)(301,4 ⁺ → 474,5 ⁻)=0.000036 +22–7; and considering deduced branching ratio from B(E2)/B(E1) ratio for an unobserved 156.5γ. E1 M.E. (301,4 ⁺ → 474,5 ⁻)=+0.0180 +48–19; B(E1)↑=0.000036 +22–7. E2 M.E. (317,3 ⁻ → 474,5 ⁻)=+3.1 4; B(E2)↑=1.37 +38–33. E3 M.E. (111,2 ⁺ → 474,5 ⁻)=+1.79 20; B(E3)↑=0.64 +15–14. E3 M.E. (301,4 ⁺ → 474,5 ⁻)=-1.7 10, coupled to higher-lying matrix elements; B(E3)↑=0.32 +49–27. Intrinsic E1 moment: D ₀ (301,4 ⁺ → 474,5 ⁻)=0.0165 eb ^{1/2} +44–18. Intrinsic E2 moment: Q ₀ (317,3 ⁻ → 474,5 ⁻)=5.30 eb 70. Intrinsic E3 moment: O ₀ (111,2 ⁺ → 474,5 ⁻)=3.10 eb ^{3/2} 40. Intrinsic E3 moment: O ₀ (301,4 ⁺ → 474,5 ⁻)=3.2 eb ^{3/2} 18.
550 ^a	6 ⁺	34 ps +6–5	T _{1/2} : weighted average of 37 ps +6–5 deduced from B(E2)(301,4 ⁺ → 550,6 ⁺)=1.42 +15–14 and 29 ps +8–6 from B(E1)(474,5 ⁻ → 550,6 ⁺)=0.0000698 +57–54. E1 M.E. (474,5 ⁻ → 550,6 ⁺)=+0.0277 11; B(E1)↑=0.0000698 +57–54. E2 M.E. (301,4 ⁺ → 550,6 ⁺)=+3.57 18; B(E2)↑=1.42 +15–14. Intrinsic E1 moment: D ₀ (474,5 ⁻ → 550,6 ⁺)=0.0231 eb ^{1/2} 10. Intrinsic E2 moment: Q ₀ (301,4 ⁺ → 550,6 ⁺)=5.59 eb 28.
703 ^b	7 ⁻	15 ps 5	T _{1/2} : weighted average of 17 ps 5 deduced from B(E1)(550,6 ⁺ → 703,7 ⁻)=0.0000573 +92–85 and 9 ps +10–5 from B(E2)(474,5 ⁻ → 703,7 ⁻)=1.76 +34–31. E1 M.E. (550,6 ⁺ → 703,7 ⁻)=+0.0273 21; B(E1)↑=0.0000573 +92–85. E2 M.E. (474,5 ⁻ → 703,7 ⁻)=+4.4 4; B(E2)↑=1.76 +34–31. E3 M.E. (301,4 ⁺ → 703,7 ⁻)=+3.3 +3–5, coupled to higher-lying matrix elements; B(E3)↑=1.21 +23–34. Intrinsic E1 moment: D ₀ (550,6 ⁺ → 703,7 ⁻)=0.0211 eb ^{1/2} 16. Intrinsic E2 moment: Q ₀ (474,5 ⁻ → 703,7 ⁻)=6.30 eb 60. Intrinsic E3 moment: O ₀ (301,4 ⁺ → 703,7 ⁻)=4.60 eb ^{3/2} +50–60.
843 ^a	8 ⁺	11.1 ps +31–24	T _{1/2} : weighted average of 10.5 ps +31–24 from B(E2)(550,6 ⁺ → 843,8 ⁺)=1.32 +15–14 and 11.8 ps +31–27 from B(E1)(703,7 ⁻ → 843,8 ⁺)=0.0000670 +78–74. E1 M.E. (703,7 ⁻ → 843,8 ⁺)=+0.0317 18; B(E1)↑=0.0000670 +78–74. E2 M.E. (550,6 ⁺ → 843,8 ⁺)=+4.15 23; B(E2)↑=1.32 +15–14. Intrinsic E1 moment: D ₀ (703,7 ⁻ → 843,8 ⁺)=0.0230 eb ^{1/2} 13. Intrinsic E2 moment: Q ₀ (550,6 ⁺ → 843,8 ⁺)=5.60 eb 30.
914 ^{#c}	0 ⁺		
992 ^b	9 ⁻	5.1 ps +17–13	T _{1/2} : weighted average of 4.9 ps +17–13 from B(E1)(843,8 ⁺ → 992,9 ⁻)=0.000136 +24–22 and 5.9 ps +40–22 from B(E2)(703,7 ⁻ → 992,9 ⁻)=2.40 +87–73. E1 M.E. (843,8 ⁺ → 992,9 ⁻)=+0.048 4; B(E1)↑=0.000136 +24–22.

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Coulomb excitation [2020Bu01](#) (continued) ^{222}Ra Levels (continued)

E(level) [†]	J ^π @	T _{1/2} &	Comments
1000? ^{‡d}	(2 ⁺)		E2 M.E. ($703,7^- \rightarrow 992,9^-$)= $+6.0$ 10; B(E2)↑= 2.40 +87–73.
1025 ^{#c}	2 ⁺		Intrinsic E1 moment: D ₀ ($843,8^+ \rightarrow 992,9^-$)= 0.0326 eb ^{1/2} 25.
1050? ^{‡d}	(3 ⁺)		Intrinsic E2 moment: Q ₀ ($703,7^- \rightarrow 992,9^-$)= 7.6 eb 12.
1150? ^{‡d}	(4 ⁺)		
1173 ^a	10 ⁺	5.0 ps +24–17	T _{1/2} : weighted average of 5.3 ps +27–17 from B(E2)($843,8^+ \rightarrow 1173,10^+$)= 1.30 +29–26 and 5.0 ps +24–17 from B(E1)($992,9^- \rightarrow 1173,10^+$)= 0.000084 +23–20. E1 M.E. ($992,9^- \rightarrow 1173,10^+$)= $+0.040$ 5; B(E1)↑= 0.000084 +23–20. E2 M.E. ($843,8^+ \rightarrow 1173,10^+$)= $+4.7$ 5; B(E2)↑= 1.30 +29–26. Intrinsic E1 moment: D ₀ ($992,9^- \rightarrow 1173,10^+$)= 0.026 eb ^{1/2} 3. Intrinsic E2 moment: Q ₀ ($843,8^+ \rightarrow 1173,10^+$)= 5.60 eb 60.
1200? ^{‡c}	(4 ⁺)		
1331 ^b	11 ⁻	3.6 ps +18–12	T _{1/2} : deduced from B(E1)($1173,10^+ \rightarrow 1331,11^-$)= 0.000119 +30–27. E1 M.E. ($1173,10^+ \rightarrow 1331,11^-$)= $+0.050$ 6; B(E1)↑= 0.000119 +30–27. Intrinsic E1 moment: D ₀ ($1173,10^+ \rightarrow 1331,11^-$)= 0.031 eb ^{1/2} 4.
1500? ^{‡c}	(6 ⁺)		
1537 ^a	12 ⁺	4.6 ps +26–16	T _{1/2} : deduced from B(E1)($1331,11^- \rightarrow 1537,12^+$)= 0.000042 +11–10. E1 M.E. ($1331,11^- \rightarrow 1537,12^+$)= $+0.031$ 4; B(E1)↑= 0.000042 +11–10. Intrinsic E1 moment: D ₀ ($1331,11^- \rightarrow 1537,12^+$)= 0.0182 eb ^{1/2} 22.
2000? ^{‡c}	(8 ⁺)		

[†] Rounded values from Adopted Levels.[‡] A level at an assumed energy included in the extraction of matrix elements in the GOSIA analysis of experimental Coulomb excitation yields. This level is not included in the Adopted Levels.[#] A known level from literature included in the extraction of matrix elements in the GOSIA analysis of experimental Coulomb excitation yields. This level is not included in the Adopted Levels.[@] As given in [2020Bu01](#) based on previous assignment in literature.[&] Deduced by evaluators from B(E2)↑ and B(E1)↑ values deduced from corresponding matrix elements in [2020Bu01](#), and adopted γ-ray branching ratios from Adopted Gammas.^a Band(A): g.s. band.^b Band(B): Octupole band.^c Band(C): Band based on 914, 0⁺. Levels above 2⁺ are assumed.^d Band(D): Assumed γ band. $\gamma(^{222}\text{Ra})$

Total conversion coefficients are from the Adopted Levels, Gammas dataset, where E_y values are given more precisely than the rounded values in this dataset, taken from [2020Bu01](#).

E _i (level)	J ^π _i	E _γ [†]	I _γ [‡]	E _f	J ^π _f	Mult. [‡]	α@	Comments
111	2 ⁺	111	100	0.0	0 ⁺	E2	6.12 9	
242	1 ⁻	131	31.2 15	111	2 ⁺	(E1)	0.2500 35	I _γ (131γ,E3)/I _γ (242γ,E1)= 1.9×10^{-9} 7, deduced by evaluators from B(E3)/B(E1) ratio.
301	4 ⁺	242 (59)	100.0 30 7.7×10^{-9} 38	0.0	0 ⁺	E1 [E3]	0.0575 8 5.2×10^3 6	I _γ (59γ,E3)/I _γ (190γ,E2)= 7.7×10^{-11} 38 deduced by evaluators from B(E3)/B(E2) ratio. This γ is

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Coulomb excitation [2020Bu01 \(continued\)](#) $\gamma(^{222}\text{Ra})$ (continued)

E_i (level)	J_i^π	E_γ^\dagger	I_γ^\ddagger	E_f	J_f^π	Mult. [‡]	$a^@$	Comments
								not included in the Adopted Levels, Gammas dataset.
301	4 ⁺	190	100	111	2 ⁺	E2	0.700 10	
317	3 ⁻	(15.8 <i>I</i>)	<0.2	301	4 ⁺	[E1]	3.77 9	E_γ : from level-energy difference in the Adopted Levels; γ not included in the Adopted dataset.
								I_γ : from $B(E1,15.8\gamma)/B(E1,206\gamma)$.
								$I_\gamma(15.8\gamma,E3)/I_\gamma(206\gamma,E1)=10\times10^{-16}$ 5, deduced by evaluators from $B(E3)/B(E1)$ ratio.
		75 [‡]	0.017 4	242	1 ⁻	[E2]	36.8 5	
		206	100.0 32	111	2 ⁺	E1	0.0839 12	$I_\gamma(206\gamma,E3)/I_\gamma(75\gamma,E2)<11\times10^{-5}$, deduced by evaluators from $B(E3)/B(E2)$ ratio.
		(317)	2.5×10^{-5} 12	0.0	0 ⁺	[E3]	0.747 15	I_γ : from $B(E3,317\gamma)/B(E1,206\gamma)$; γ not included in the Adopted dataset.
474	5 ⁻	(156.5 <i>I</i>)	4.3 23	317	3 ⁻	[E2]	1.480 21	E_γ : from level-energy difference in the Adopted Levels.
								I_γ deduced by evaluators from $B(E2,156.5\gamma)/B(E1,172\gamma)$ ratio.
		172	100	301	4 ⁺	[E1]	0.1288 18	$I_\gamma(173\gamma,E3)/I_\gamma(173\gamma,E1)=30\times10^{-9}$ +60–29, deduced by evaluators from $B(E3)/B(E1)$ ratio.
		(363)	5.8×10^{-4} 29	111	2 ⁺	[E3]	0.433 8	I_γ : from $B(E3,363\gamma)/B(E1,172\gamma)$; γ not included in the Adopted dataset.
550	6 ⁺	77	29 [#] 4	474	5 ⁻	[E1]	0.2211 31	E_γ : new γ ray in the present work.
		249	100 [#]	301	4 ⁺	[E2]	0.276 4	
703	7 ⁻	153	100 32	550	6 ⁺	[E1]	0.1715 28	
		229	18 6	474	5 ⁻	[E2]	0.362 6	
		(402)	0.0025 6	301	4 ⁺	[E3]	0.295 5	I_γ : from $B(E3,402\gamma)/B(E1,153\gamma)$; γ not included in the Adopted dataset.
843	8 ⁺	140	100 18	703	7 ⁻	[E1]	0.2126 31	
		293	92 8	550	6 ⁺	[E2]	0.1636 23	
992	9 ⁻	149	100 16	843	8 ⁺	[E1]	0.1822 30	
		289	88 10	703	7 ⁻	[E2]	0.1705 26	
1173	10 ⁺	181	100 23	992	9 ⁻	[E1]	0.1147 16	
		330	75 7	843	8 ⁺	[E2]	0.1147 16	
1331	11 ⁻	157	64 10	1173	10 ⁺	[E1]	0.1604 26	
		338 [‡]	100 10	992	9 ⁻	[E2]	0.1069 16	
1537	12 ⁺	206 [‡]	64 12	1331	11 ⁻	[E1]	0.0839 13	$B(E1)(W.u.)=0.00164$ +93–62
		364 [‡]	100 10	1173	10 ⁺	[E2]	0.0871 13	

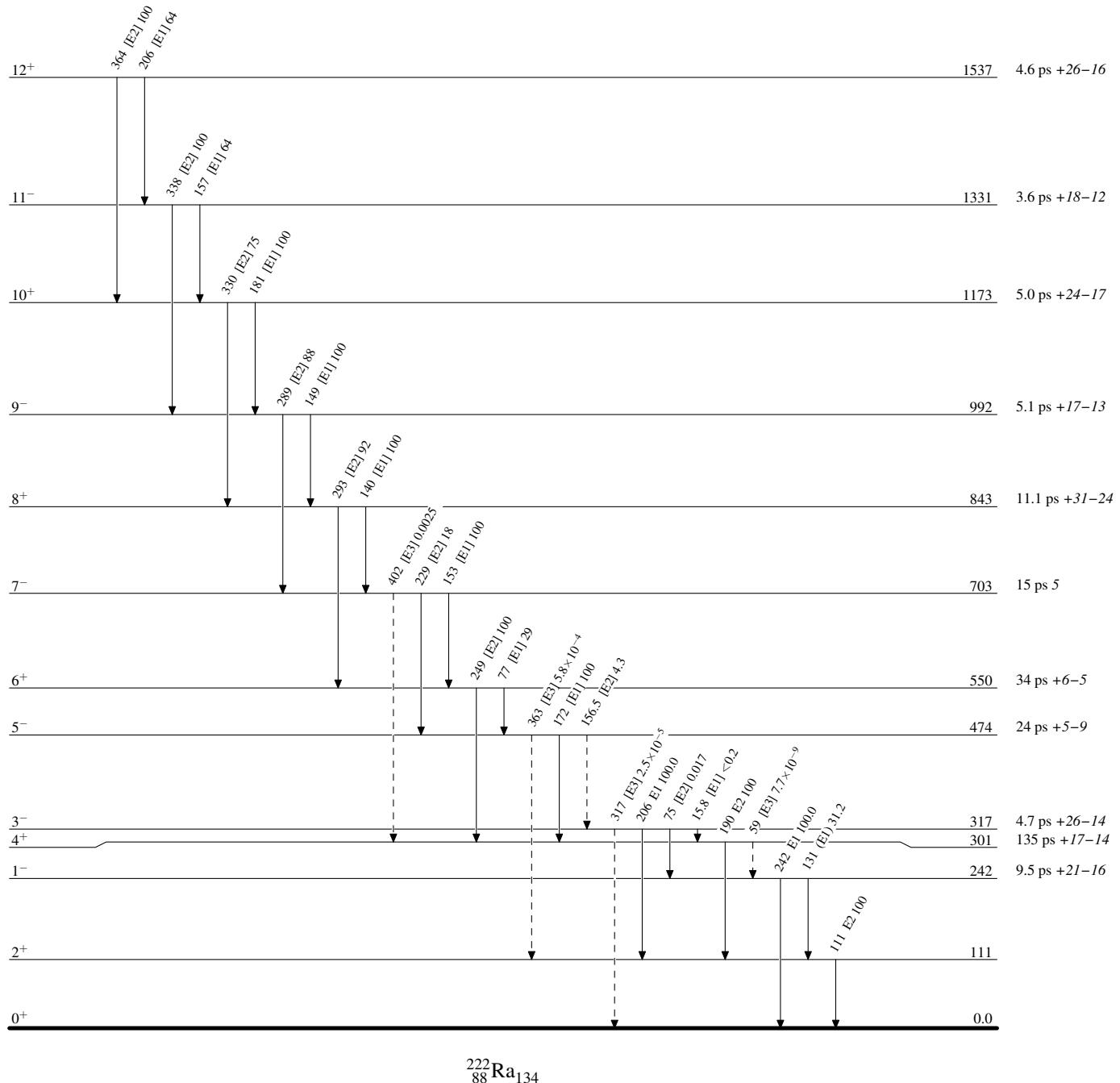
[†] From supplemental material of [2020Bu01](#), unless otherwise indicated.[‡] From the Adopted Levels, Gammas dataset, with exceptions noted. Energies are rounded values.# Branching ratio deduced by evaluators from $B(E2)\uparrow/B(E1)\uparrow$ ratio.@ Total theoretical internal conversion coefficients, calculated using the BrIcc code ([2008Ki07](#)) with Frozen orbital approximation based on γ -ray energies, assigned multipolarities, and mixing ratios, unless otherwise specified.

Coulomb excitation 2020Bu01

Legend

Level Scheme

Intensities: Relative photon branching from each level

- - - - - ► γ Decay (Uncertain)

Coulomb excitation 2020Bu01

Band(C): Band based on
914, 0⁺

(8⁺) —— 2000

Band(A): g.s. band

