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PAPIN: A FORTRAN-IV PROGRAM TO CALCULATE CROSS SECTION PROBABILITY
TABLES, BONDARENKO AND TRANSMISSION SELF-SHIELDING FACTORS FOR
FERTILE ISOTOPES IN THE UNRESOLVED RESONANCE REGION

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LIST OF LATIN SYMBOLS

a_0	Scattering length
AWRI	Ratio of the mass of the target nucleus to the neutron mass
$\langle D \rangle_{\ell, J}$	Average level spacing in the ℓ, J series
E_f	Upper limit of the sampling energy region
E_L	Lower limit of the sampling energy region
E_{ref}	Reference neutron energy
E_r	Energy of the, r , resonance
$(EU)_{\ell, J}$	Upper limit of the energy in the (ℓ, J) series
$(EL)_{\ell, J}$	Lower limit of the energy in the (ℓ, J) series
$f_{c, i}$	Bondarenko capture factor at group i
$f_{tf, i}$	Bondarenko average weighted flux total cross section at group i
$f_{tc, i}$	Bondarenko average weighted current total cross section at group i
g_J	Spin statistical factor
I	Spin of the target nucleus
J	Spin of the resonance state
K	Wave number
K_0	Reduced wave number
ℓ	Angular momentum
N	Number of ladders
NR2	Parameter to set the energy limits of the ladder
R	Channel Radius
T	Effective temperature
V_ℓ	Penetration factors
$U(x, y)$	Voigt Profiles function
$V(x, y)$	Voigt Profiles function

LIST OF GREEK SYMBOLS

$\Gamma_{nr}^{(\ell, J)}$	Neutron width of the, r, resonance in the (ℓ, J) series
$\Gamma_{\gamma r}^{(\ell, J)}$	Gamma width of the r resonance in the (ℓ, J) series
$\Gamma_r^{(\ell, J)}$	Total width of the r resonance in the (ℓ, J) series
$\Gamma_{nr}^o(\ell, J)$	Reduced neutron width of the r resonance in the (ℓ, J) series
$\langle \Gamma_{n,0} \rangle$	Average neutron width for s-waves
$\langle \Gamma_{\gamma} \rangle$	Average gamma width for s-waves
$\langle \Gamma \rangle$	Average total width for s-waves
Δ	Doppler width
ϕ_{ℓ}	Hard sphere phase shift
$\sigma_{n\gamma}^{(\ell)}$	Capture cross section for the ℓ partial wave
$\sigma_t^{(\ell)}$	Total cross section for the ℓ partial wave
σ_o	Dilution cross section
$\bar{\sigma}_{c,i}(\sigma_o)$	Bondarenko shielded group capture cross section
$\bar{\sigma}_{ft,i}(\sigma_o)$	Bondarenko weighted flux shielded group total cross section
$\bar{\sigma}_{ct,i}(\sigma_o)$	Bondarenko weighted current shielded group total cross section
σ_{pot}	Potential cross section
σ_{min}	Lower limit of the cross section probability table band structure
σ_{max}	Upper limit of the cross section probability table band structure
$\langle \sigma_t \rangle_i$	Infinite dilute total cross section at group i
$\langle \sigma_c \rangle_i$	Infinite dilute capture cross section at group i
η_{TR}	Transmission self-shielding factor
η_{SIR}	Self-indication self-shielding factor

ABSTRACT

The Fortran IV code PAPIN has been developed to calculate cross section probability tables, Bondarenko self-shielding factors and average self-indication ratios for non-fissile isotopes, below the inelastic threshold, on the basis of the ENDF/B prescriptions for the unresolved resonance region. Monte-Carlo methods are utilized to generate ladders of resonance parameters in the unresolved resonance region, from average resonance parameters and their appropriate distribution functions.

The neutron cross-sections are calculated by the single level Breit-Wigner (SLBW) formalism, with s, p and d-wave contributions. The cross section probability tables are constructed by sampling the Doppler-broadened cross sections.

The various self-shielded factors are computed numerically as Lebesgue integrals over the cross section probability tables.

The program PAPIN has been validated through extensive comparisons with several deterministic codes.

I. INTRODUCTION

PAPIN has been developed as a flexible program to construct cross section probability tables for the calculation of Bondarenko and transmission self-shielding factors for fertile isotopes, in the unresolved resonance region. This report is intended to describe the main features of the program as well as to serve as a user's manual.

II. DESCRIPTION OF THE PROGRAM

In this section we give a brief outline of the program, whose main features are illustrated in the block diagram in Fig. 1. The main program reads the input data and generates resonance ladders, over specified neutron energy regions, by Monte-Carlo methods. This step provides the input for the calculation of the various neutron cross sections, by the subroutines, BREDO, SHIF and VIL. The output cross sections are then Doppler-broadened by the subroutines, SVS, W and QUICKW. On the basis of this information the main program constructs the probability tables, which are utilized by the subroutines BREKO and SHELF to compute Bondarenko factors and transmission self-shielded factors respectively as Lebesgue integrals over the probability tables.^{1,2,3}

III. PAPIN MAIN OPERATIONS

Here we describe some of the main operations in PAPIN with detail.

A. Generation of Resonance Ladders

The upper and lower limits E_f and E_i , respectively, of the energy region where the cross section sampling is to be performed, are selected by the expressions,

$$E_f = E_{ref} + TEMP \times D_{min} \quad (1)$$

$$E_i = E_{ref} - TEMP \times D_{min} \quad (2)$$

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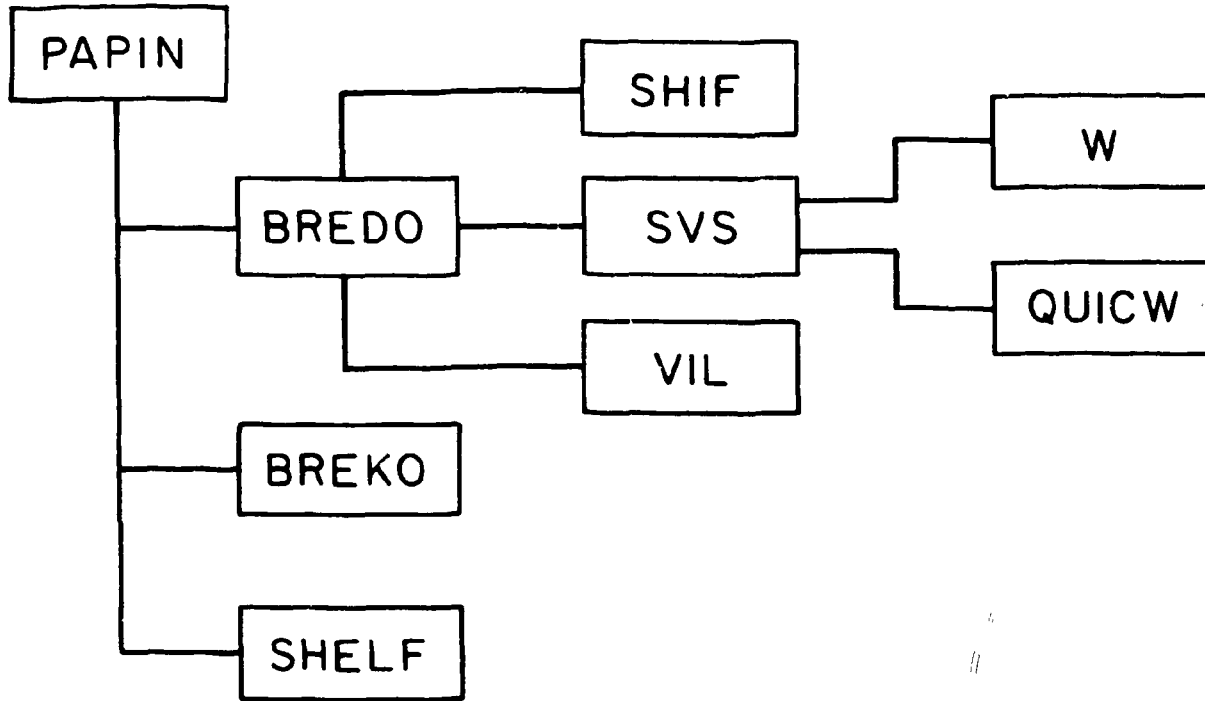


Fig. 1. Block diagram of subroutines in the PAPI program.

where $TEMP = \frac{NR2}{2} - 5$, E_{ref} and $NR2$ are input parameters described in section VII, and D_{min} is the smallest value among the quantities $\langle D \rangle_{\ell,J}$ corresponding to E_{ref} in the ENDF/B-V files.

To allow for the contribution of resonances outside the sampling region a wider energy region is defined by means of the upper and lower energy limits, $(EU)_{\ell,J}$ and $(EL)_{\ell,J}$, respectively:

$$(EU)_{\ell,J} = E_{ref} + \frac{NR2}{2} \cdot \langle D \rangle_{\ell,J} \quad (3)$$

$$(EL)_{\ell,J} = E_{ref} - \frac{NR2}{2} \cdot \langle D \rangle_{\ell,J} \quad (4)$$

The resonance energies are generated from the Wigner Level Space Distribution Function,^{3,4} by means of the expression:

$$E_{\ell,J,i+1} = E_{\ell,J,i} + \frac{2}{\sqrt{\pi}} \cdot \langle D \rangle_{\ell,J} \cdot (\log R)^{1/2} \quad (5)$$

where R , is a random number between 0 and 1. The neutron level widths are obtained from Chi-squared distributions with 0 degrees of freedom ($\nu = 1$ or 2), by well known rejection techniques.³ Finally, the capture level widths are considered constants (equal to their ENDF/B-V prescribed average values).

B. Neutron Cross Section Calculations

For each ladder of resonances, the neutron capture cross section $\sigma_{n\gamma}$, and the total cross section σ_t are computed by the S.L.B.W. formalism in the framework of the ENDF/B prescriptions.^{5,6} The Doppler-Broadened cross sections^{7,8} are given by the expressions:

$$\sigma_{n\gamma}^{(\ell)} = \frac{2\pi^{3/2}}{k^2} \sum_J g_J \sum_{r=1}^{NR_J} \frac{\Gamma_{nr}^{(\ell,J)} \cdot \Gamma_{yr}^{(\ell,J)}}{\Gamma_r^{(\ell,J)} \cdot \Delta} \cdot U(x,y) \quad (6)$$

$$\sigma_t^{(\ell)} = \frac{4\pi}{K^2} \cdot (2\ell + 1) \cdot \sin^2 \phi_\ell + \frac{2\pi^{3/2}}{K^2} \sum_J g_J \sum_{r=1}^{NR_J} \frac{\Gamma_{nr}^{(\ell, J)}}{\Delta} (U(x, y) \cdot \cos(2\phi_\ell) - V(x, y) \sin(2\phi_\ell)) \quad (7)$$

where,

$$K = \text{wave number} = 2.196771 \frac{AWRI}{AWRI + 1} \cdot 10^{-3} \cdot \sqrt{E_{REF}} \quad (8)$$

$$\Delta = \text{Doppler width} = 10^{-2} (3.4468 \cdot E_{ref} \cdot T/AWRI)^{1/2} \quad (9)$$

AWRI = Ratio of the mass of the target nucleus to the neutron mass

$$g_J = \text{spin statistical factor} = \frac{2J + 1}{2 \cdot (2I + 1)} \quad (10)$$

$$\Gamma_{nr}^{(\ell, J)} = \Gamma_n^{(o)(\ell, J)} \cdot V_\ell(E_{ref}) \cdot (E_{ref})^{1/2} \quad (11)$$

Where $\Gamma_n^{(o)(\ell, J)}$ are the reduced neutron width and the factors $V_\ell(E_{ref})$ are given by the expressions (for $\ell = 0, 1$ and 2).

$$V_0 = 1 \quad (12)$$

$$V_1 = \frac{\rho^2}{1 + \rho^2} \quad (13)$$

$$V_2 = \frac{\rho^4}{9 + 3\rho^2 + \rho^4} \quad (14)$$

with

$$\rho = 0.002196771 \cdot \left(\left(\frac{AWRI}{AWRI + 1} \right) \cdot (E_{ref})^{1/2} R \right) \quad (15)$$

where R is the channel radius in units of 10^{-12} cm. The hard sphere phase shift are computed (for $\ell = 0, 1$ and 2) by:

$$\phi(\rho_1) = \rho_1 \quad (16)$$

$$\phi_1(\rho_1) = \rho_1 - \tan^{-1}(\rho_1) \quad (17)$$

$$\phi_2(\rho_1) = \rho_1 - \tan^{-1} \left(\frac{3\rho_1}{3 - \rho_1^2} \right) \quad (18)$$

with,

$$\rho_1 = \rho \cdot \frac{a_0}{R} \quad (19)$$

where a_0 is the scattering length. The U and V functions are obtained from the expressions:

$$U(x,y) = \frac{1}{\pi} \int_{-\infty}^{\infty} \frac{y \cdot e^{-s^2}}{y^2 + (x-s)^2} \cdot ds \quad (20)$$

$$V(x,y) = \frac{1}{\pi} \int_{-\infty}^{\infty} \frac{(x-s) \cdot e^{-s^2}}{y^2 + (x-s)^2} \cdot ds \quad (21)$$

where

$$x = \frac{Er - E}{\Delta} \quad (22)$$

$$y = \frac{\Gamma_{nr} + \Gamma}{2\Delta} \gamma \quad (23)$$

The expressions (20) and (21) are computed by the Doppler routine QUICKW. The capture and total cross sections are computed from equations (6) and (7) at one hundred equally spaced energy points. This calculation is then corrected for the contribution of the truncated levels by means of the expression^{7,9} (s-waves only):

$$\sigma^{\infty} = \frac{4\pi}{K_0^2} \cdot S_0 \cdot \frac{\langle \Gamma \rangle}{4\sqrt{E}} \cdot \left(\frac{EU-EL + \langle D \rangle}{(EU-E-0.5 \langle D \rangle)(E-EL+0.5 \langle D \rangle)} - K_0 a_0 \ln \left(\frac{E-EL + 0.582 \langle D \rangle}{EU-E+0.582 \langle D \rangle} \right) \right) \quad (24)$$

where s_0 is the s-wave strength function, K_0 is the reduced wave number, $\langle D \rangle$, the average level spacing for s-wave neutrons, a_0 , the scattering length, and EU and EL the upper and lower limits respectively of the resonance ladder. Finally when ENDF/B-V contains a smooth contribution (File 3) to the cross section, this contribution is added to (6) or (7).

C. Construction of the Cross Section Probability Tables

The cross-section band structure is made of 20 bands of width determined by a logarithmic scale,

$$\sigma_n = \sigma_{\min} \cdot p^n \quad (25)$$

where

$$p = \exp 0.05 \ln \left(\frac{\sigma_{\max}}{\sigma_{\min}} \right) \quad (26)$$

The lower and upper limits of the band structure σ_{\min} and σ_{\max} can be defined arbitrarily or calculated by:

$$\sigma_{\min} = 0.2 \sigma_{\text{pot}} \quad (27)$$

$$\sigma_{\max} = \sigma_{\text{pot}} + \frac{\pi}{K^2} \frac{\langle \Gamma_{n,0} \rangle}{\langle \Gamma_{n,0}^k \rangle + \langle \Gamma_{\gamma} \rangle} \quad (28)$$

where all the symbols have been defined previously. Two additional cross section bands are included to collect cross sections values below σ_{\min} and above σ_{\max} .

The total cross section probability table is constructed by sampling the total cross section at the one hundred equidistant points over each ladder of resonances, and determining the fraction belonging to each band in the table. The average value of the total and capture cross sections in each band is also determined (see the work of Levitt,¹ for more details).

IV. CALCULATION OF SHIELDED CROSS SECTIONS

A. Bondarenko Group Cross Sections and Self-Shielding Factors

The Bondarenko shielded group cross sections are defined as ensemble averages over the cross section probability tables,¹⁰ i.e.:

$$\bar{\sigma}_{c,i}(\sigma_0) = \frac{1}{\langle \alpha \rangle_i} \left\langle \frac{\sigma_c}{\sigma_t + \sigma_0} \right\rangle_i \quad (29)$$

$$\bar{\sigma}_{tf,i}(\sigma_0) = \frac{1}{\langle \alpha \rangle_i} \left\langle \frac{\sigma_t}{\sigma_t + \sigma_0} \right\rangle_i \quad (30)$$

$$\bar{\sigma}_{tc,i}(\sigma_0) = \frac{1}{\langle \alpha^2 \rangle_i} \left\langle \frac{1}{\sigma_t + \sigma_0} \right\rangle_i \sigma_0 \quad (31)$$

with,

$$\alpha_i = \frac{1}{\sigma_{ti} + \sigma_0} \quad (32)$$

and where $\bar{\sigma}_{ci}(\sigma_0)$, $\bar{\sigma}_{tf,i}(\sigma_0)$, $\bar{\sigma}_{tc,i}(\sigma_0)$ are the capture, flux weighted and current weighted shielded group total cross sections, for the i^{th} neutron energy group and dilution σ_0 .

Calling $\langle \sigma_c \rangle_i$, $\langle \sigma_t \rangle_i$ the i^{th} group dilute capture and total cross section (i.e. for $\sigma_0 \rightarrow \infty$), the program PAPIIN calculates the self-shielding factors:

$$f_{c,i}(\sigma_0) = \bar{\sigma}_{c,i}(\sigma_0) / \langle \sigma_c \rangle_i \quad (33)$$

$$f_{tf,i}(\sigma_0) = \bar{\sigma}_{tf,i}(\sigma_0) / \langle \sigma_t \rangle_i \quad (34)$$

$$f_{tc,i}(\sigma_0) = \bar{\sigma}_{tc,i}(\sigma_0) / \langle \sigma_t \rangle_i \quad (35)$$

B. Calculation of Transmission and Self-Indication Self-Shielding Factors

The transmission self-shielding factor¹¹ η_{TR} , and the self-indication self-shielding factor,¹¹ η_{SIR} , are computed as the following ensemble averages over the cross section probability tables:

$$\eta_{\text{TR}} = \langle \exp(-n_1 (\sigma_t - \langle \sigma_t \rangle)) \rangle \quad (36)$$

$$\eta_{\text{SIR}} = \langle \sigma_Y \exp(-n_1 (\sigma_t - \langle \sigma_t \rangle)) \rangle \quad (37)$$

where n_1 is the sample thickness in atoms per barn. With these factors, "the program computes the average transmission and the average self-indication ratio."

C. Statistical Uncertainties

For a given cross section, σ , the statistical error, $\Delta\sigma$, inherent to the sampling process is given by:¹²

$$\Delta\sigma = \frac{1}{\sqrt{N}} \left(\frac{1}{N} \sum_{j=1}^N \sigma_j^2 - \langle\sigma\rangle^2 \right)^{1/2} \quad (38)$$

with

$$\sigma_j = \frac{1}{n} \sum_{i=1}^n \sigma_{ij} \quad (39)$$

$$\langle\sigma\rangle = \frac{1}{N} \sum_{j=1}^N \sigma_j \quad (40)$$

where σ_{ij} is the cross section at the i^{th} sampling energy in the j^{th} ladder; $n=100$ is the number of sampling points within each ladder; and N the total number of ladders. For ratios of the general type,

$$Y_{AB} = \frac{\langle A \rangle}{\langle B \rangle} \quad (41)$$

the error ΔY_{AB} is computed according to the expression:

$$\Delta Y_{AB} = \left[\left(\frac{\partial Y}{\partial \langle A \rangle} \right)^2 V_{AA} + \left(\frac{\partial Y}{\partial \langle B \rangle} \right)^2 V_{BB} + 2 \left(\frac{\partial Y}{\partial \langle A \rangle} \right) \left(\frac{\partial Y}{\partial \langle B \rangle} \right) C_{AB} \right]^{1/2} \quad (42)$$

where we defined the following matrix elements:

$$V_{AA} = \frac{1}{N} \left[\frac{1}{N} \sum_{j=1}^N A_j^2 - \langle A \rangle^2 \right] \quad (43)$$

with a similar expression for V_{BB} , and

$$C_{AB} = \frac{1}{N^2} \sum_{j=1}^N (A_j - \langle A \rangle)(B_j - \langle B \rangle) \quad (44)$$

V. PROGRAM VALIDATION

The program PAPIN has been validated through extensive and detailed comparisons with the deterministic codes, NJOY,¹³ UXS,¹⁴ ETOX,¹⁵ and MC²-2,¹⁶ which are based on analytical averages of the various cross section functionals over the appropriate resonance width and level spacing distributions.

The result of the validation step with 100 ladders, NR2=100 are shown in Table I and Table II.

Table I. Values of the Shielded Group Cross Section for the U^{238} at 4000 eV and 300 K (ENDF/B-V)

	NJOY (a)	UXS (a)	ETOX (a)	MC ² -2 (a)	PAPIN
Dilution $\sigma_0(b)$	Capture X-Section (b)				
1	0.4769	0.4838	0.4830	0.4833	0.4804 \pm 0.0066
10	0.5602	*	*	*	0.5604 \pm 0.0078
100	0.7698	0.7698	0.7697	0.7698	0.7688 \pm 0.0121
1000	0.8986	*	*	*	0.9021 \pm 0.0155
	Flux Weighted Total X-Section (b)				
1	11.94	12.382	12.380	12.382	12.19 \pm 0.07
10	12.998	*	*	*	13.19 \pm 0.07
100	15.50	15.502	15.502	15.502	15.62 \pm 0.13
1000	17.46	*	*	*	17.58 \pm 0.21

Table II. Values of the Shielded Group Cross Section for the
 U^{238} at 9250 eV and 300 K (ENDF/B-V)

	NJOY (a)	UXS (a)	ETOX (a)	MC ² -2 (a)	PAPIN
<u>Dilution σ_0 (b)</u>	<u>Capture X-Section (b)</u>				
1	*	0.5365	0.5335	0.5365	0.5380 \pm 0.0050
10	0.5794	*	*	*	0.5853 \pm 0.0052
100	0.6649	0.6650	0.6649	0.6650	0.6701 \pm 0.0059
1000	0.6995	*	*	*	0.7041 \pm 0.0063
	<u>Flux Weighted Total X-Section (b)</u>				
1	*	12.681	12.672	12.681	12.596 \pm 0.060
10	13.130	*	*	*	13.337 \pm 0.061
100	14.766	14.767	14.766	14.767	14.825 \pm 0.096
1000	15.596	*	*	*	15.582 \pm 0.216

VI. INPUT DATA

A. Structure and Format of Input Cards

1. Card: FORMAT (1X,I3) N1
2. Card: FORMAT (3F12.5) CSMIN, CSMAX, FIJO
3. Card: FORMAT (1X, F 12.4, F12.1) DICRO, DICRI
4. Card: FORMAT (1X, F5.0) FOTAS
5. Data: FORMAT (6F12.4) EREF, AP, AWRI, R, T, CSDR
6. DATA: FORMAT (I3, 3F12.4) NR2, SPI, AN1, CSD3
7. Number of J sequences for each L value
 FORMAT (3I3)
 NJS(1), NJS(2), NJS(3)
8. Average resonance parameters in each (I,J) series
 FORMAT (5E 12.4)
 AD(I,J), AGNO(I,J),
 AMUN(I,J), AGG(I,J),
 AJ(I,J)

B. Function of Input Data

N1	Number of ladders.
CSMIN	Lower limit of the probability table.
CSMAX	Upper limit of the probability table
FIJO	A flag, if FIJO is equal to 1, the above values of CSMIN and CSMAX are used. If FIJO \neq 1, CSMIN and CSMAX are computed by means of Eq. (26) and (27).
DICRO	Calculates the values of the dilution cross section σ_o , according to the expression, $DICRO \times 10^J$ $J = 1, 2, 3, 4$
DICRI	The infinite dilution parameter (typically $\sigma_o = 10^5$).
FOTAS	A flag, if the value of FOTAS is set equal to 1 the program does not utilize convergence factors for the cross section. If FOTAS is different from 1, PAZIN utilizes a convergence factor at each ladder defined as:

$$\left(\frac{1}{100} \cdot \sum_i \sigma_{tij} + \sigma_3\right) F_j = \sigma_{ref}$$

where σ_{ref} is the reference total cross section, σ_{tij} is the i Doppler Broadened total cross section at energy E_i and ladder j , σ_3 is the smooth cross section due to the difference between the real value of the scattering length and the ENDF/B-V value. F_j is the convergence factor for the j^{th} ladder. (This option was not employed in the results of section 5).

EREF	The reference neutron energy in eV.
AP	The scattering length in units of 10^{-12} cm.
AWRI	The ratio of the mass of a particular isotope to that of the neutron.
R	The channel radius defined as: $R = 0.123 AWRI^{1/3} + 0.08$ (10^{-12} cm)

T Effective absolute temperature in °K.

CSDR Reference total cross section in barns.

NR2 Parameter to set the energy limits of the ladder, $NR2 \leq 100$.
Usually 100 is a convenient value.

SPI Nuclear spin of the target nucleus.

AN1 Initial thickness of the shielding sample in atom/barn. The program computes the average transmission and the self-shielding factors at several thicknesses as:

$$AN1 + 0.01I \quad I = 1, 2, \dots, 10$$

CSD3 ENDF/B-V smooth cross section.

NJS(I) Number of J values for each L value.

AD(I,J) Average level spacing in the (I,J) series.

AGNO(I,J) Average reduced neutron width in the (I,J) series.

AMUN(I,J) Number of degrees of freedom of the neutron width distribution in the (I,J) series.

AGG(I,J) Average gamma width of the (I,J) series.

AJ(I,J) The spin of the resonance state.

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Appendix I. Fortran Listing of PAPIN Program and Subprograms


```

COMPILER OPTIONS = NAME= MAIN,OPT=02,LINECNT=50,SIZE=0000K
SOURCE,EBCDIC,NOLIST,NODECK,LOAD,MAP,NOEDIT,NOXREF
C THIS PROGRAM COMPUTES A LADDER, FIRST OF ALL IT
C COMPUTES THE LIMITS OF THE LADDER, THEN IT GENERATES
C THE RESONANCE ENERGIES FOR EACH (L,J) SERIES AND THE
C WIDTH, TAKING ACCOUNT THE DEGREES OF FREEDOM.
C FIRST WE READ THE AVERAGE RESONANCE PARAMETERS FOR
C EACH ENERGY.
C EREF = REFERENCE ENERGY IN EV, NJS(I) IS THE NUMBER OF
C J STATES FOR A PARTICULAR L STATE.
DIMENSION SUMCE2(22),VARCE(22),ERRGP(22),ERRTP(22),ERREP(22)
DIMENSION CSDE1(100),SPCE(100),CSDS(22),CSDA(100,22),SUMCE(22),
1CCSV(22)
DIMENSION ERPR(22),WIPR(22)
DIMENSION VARC(22)
DIMENSION COBI(100,4)
DIMENSION SUMG2(22),SPR(22)
DIMENSION VARPR(22),SUPR2(22),SUCSS(22),VARCS(22),SUMCG(22)
DIMENSION SUCS2(22)
DIMENSION AD(3,6),AMUN(3,6),E(100)
1CSDT1(100),CSP(30),CSDTS(30),CSDGS(30),COUNT(30),PR(100,22),
1SPCS(100),F(100),F2(100)
DIMENSION CSDG1(100),SUPRO(22)
DIMENSION PR2(100,22),CSDTA(100,22),CSDTB(100,22),CSDGA(100,22)
COMMON/DSELD/ATCS(100),SPCS(100)
COMMON/DERR/YPT(100,4),YPTG(100,4),YPTT(100,4),YPTC(100,4)
COMMON/DSELF/CCSV(22),PRT(22),CCSVG(22)
COMMON/DBRED/ER(3,6,150),GNO(3,6,150),AGG(3,6),NR(3,6),
1EL(3,6),EUT(3,6),NJS(3),AJ(3,6),AGNO(3,6)
20 PRINT 20
FORMAT(' PROGRAM PAPIN VERSION FEBRUARY 1981://')
READ 30,N1
50 FORMAT(1X,I3)
PRINT 50,N1
55 FORMAT(10H NUMBER OF LADDFRS=,I3)
READ 40,CSMIN,CSMAX,F1JC
40 FORMAT(3F12,8)
READ 51,DICRO,DICR1
PRINT 51,DICRO,DICR1
51 FORMAT(1X,F12,4,F12,1)
READ 52,FOTAS
PRINT 52,FOTAS
52 FORMAT(1X,F5,0)
READ 100,EREF,AP,AWRI,R,T,CSDR
100 FORMAT(6F12,4)
PRINT 101,EREF,AP,AWRI,R,T,CSDR
101 FORMAT(10H NEUTRON ENERGY=,F12,2/
110H SCATTERING LENGTH=,F8,4/
215H ATOMIC WEIGHT=,F8,3/
310H CHANNEL RADIUS=,F8,4/
413H TEMPERATURE=,F8,2/
531H TOTAL-REFERENCE-CROSS-SECTION=,F10,4)
READ 110,NR2,SP1,AN1,CSD3
110 FORMAT(13,3F12,4)
PRINT 111,NR2,SP1,AN1,CSD3
111 FORMAT(5H NR2=,I3/
116H NUCLEAR SPIN=,F8,4/
231H INITIAL THICKNES IN ATOM/BARN=,F8,4/
328H COMPENSATION CROSS SECTION=,F10,4)
READ 200,(NJS(I),I=1,3)
PRINT 200,(NJS(I),I=1,3)
200 FORMAT(3I3)
PRINT 219
219 FORMAT(' UNRESOLVED RESONANCE PARAMETERS ' /
1' L J D AGNO AMUN AGG ')
DO 230 I=1,3
NJSI = NJS(I)
DO 230 J=1, NJSI
READ 220, AD(I,J), AGNO(I,J), AMUN(I,J), AGG(I,J), AJ(I,J)
220 FORMAT(5E12,4)
230 PRINT 221,I,AJ(I,J),AD(I,J),AGNO(I,J),AMUN(I,J),AGG(I,J)
221 FORMAT(1X,I2,3E12,4,F6,1,E12,4)
DICR2=DICRO
C COMPUTES THE SMALLER OF THE AD(I,J)
ADMIN = AD(I,I)
DO 250 I=1,3
NJSI = NJS(I)
DO 250 J=1, NJSI
IF (AD(I,J),LE,ADMIN) ADMIN = AD(I,J)
250 CONTINUE
C COMPUTES THE LIMITS EINIT AND ENF OF THE LADDER
TEMP=FLOAT(NR2)/2,-5
EINIT = EREF+TEMP*ADMIN
ENF = EREF+TEMP*ADMIN
C COMPUTES THE LOWEST VALUE OF THE ENERGY EL(I,J) IN EACH
C (I,J) SERIES.

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TEMP=TEMP*5
DO 260 I=1,3
NJSI = NJS(I)
DO 260 J=1,NJSI
EL(I,J) = EREF+TEMP*AD(I,J)
260 EU(I,J)=EREF+TEMP*AD(I,J)
C GENERATION OF RESONANCE PARAMETERS.
C GENERATION OF RESONANCE ENERGIES ER(I,J,K)
NR=NR2
DO 261 L=1,N1
DO 270 I=1,3
NJSI=NJS(I)
DO 270 J=1,NJSI
ER(I,J,1)=EL(I,J)
DO 270 K=2,NR2
270 ER(I,J,K)=ER(I,J,K-1)+1.128379*AD(I,J)*SORT(=ALOG(RANF(0)))
DO 263 I=1,3
NJSI=NJS(I)
DO 263 J=1,NJSI
M=1
IF (ER(I,J,NR2).GT.EU(I,J)) GO TO 262
NR(I,J)=NR2
GO TO 263
265 M=M+1
262 NR3=NR2-M
IF (ER(I,J,NR3).LT.EU(I,J)) GO TO 264
IF (ER(I,J,NR3).GT.EU(I,J)) GO TO 265
NR(I,J)=NR2-M
GO TO 263
264 NR(I,J)=NR2-M+1
263 CONTINUE
C GENERATION OF THE WIDTH
DC 280 I=1,3
NJSI=NJS(I)
DO 280 J=1,NJSI
IF (AMCN(I,J).GT.1.) GO TO 281
NR=NR(I,J)
DO 283 K=1,NR4
C CHI-SQUARED ONE DEGREE OF FREEDOM
282 R1=-ALOG(RANF(0))
R2=-ALOG(RANF(0))
IF (R1+1.0)**2.GT.2.0**R2) GO TO 282
283 GNO(I,J,K)=AGNO(I,J)*R1**2
GO TO 280
C CHI-SQUARED TWO DEGREES OF FREEDOM
281 NR4=NR(I,J)
DO 285 K=1,NR4
285 GNO(I,J,K)=-AGNO(I,J)*ALOG(RANF(0))
280 CONTINUE
C MAKES THE ENERGY GRID
DELE=(EFIN-EINIT)/99.
E(I)=EINIT
DC 290 I=1,99
290 E(I+1)=EINIT+FLOAT(I)*DELE
C COMPUTES THE CROSS-SECTIONS IN EACH POINT OF THE GRID.
DO 291 I=1,100
E=E(I)
CALL BREDC(E,EREF,AD,A,RI,R,I,SPI,CSDG,CSDI,CSD,CSDI)
CSDI(I)=CSDI
CSDG(I)=CSDG
CSDT(I)=CSDT+CSDG
291 CONTINUE
SPCE(L)=0.0
SPCG(L)=0.0
SPCS(L)=0.0
DO 292 I=1,100
SPCE(L)=SPCE(L)+CSDI(I)
SPCG(L)=SPCG(L)+CSDG(I)
292 SPCS(L)=SPCS(L)+CSDT(I)
ATC(L)=SPCG(L)/100.
F(L)=CSDR/ATC(L)
F2(L)=F(L)*F(L)
IF (FOTAS.EQ.1.) F(L)=1.
DO 293 I=1,100
CSDG(I)=F(L)*CSDG(I)
CSDT(I)=F(L)*CSDT(I)
293 DO 295 J=1,4
YPT(L,J)=0.0
YPT(L,J)=0.0
YPTC(L,J)=0.0
YPTG(L,J)=0.0
DO 296 I=1,100
COBI(L,J)=CSDT(I)+D1CR2*10.**J
YPT(L,J)=YPT(L,J)+(1./COBI(L,J))
YPTT(L,J)=YPTT(L,J)+(CSDT(I)/COBI(L,J))
YPTC(L,J)=YPTC(L,J)+(1./COBI(L,J))*CSDI(L,J)
296 YPTG(L,J)=YPTG(L,J)+(CSDG(I)/COBI(L,J))
YPTC(L,J)=YPTC(L,J)/100.

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YPT(L,J)=YPTY(L,J)/100.
YPTT(L,J)=YPTT(L,J)/100.
YPTG(L,J)=YPTG(L,J)/100.
293 CONTINUE
IF (PIJO.EQ.1.) GO TO 294
SIGOR=(6.51*10.**S/EREF)*((AWRI+1.)/AWRI)**2
AGNR=SQRT(EREF)*AGNO(1,1)
AGGR=AGG(1,1)
CSMIN=0.2*CSP
CSMAX=CSP+1.0*SIGOR*AGNR/(AGNR*AGGR)
294 CONTINUE
TK=EXP(0.05*ALOG(CSMAX/CSMIN))
CSPP(1)=CSMIN
DO 300 K=2,20
300 CSPP(K)=CSPP(1)*TK**(K-1)
C CONSTRUCT THE PROBABILITY TABLE OF THE LADDER
DO 306 K=1,22
CSDS(K)=0.0
CSDTS(K)=0.0
COUNT(K)=0
306 CSDGS(K)=0.0
DO 301 I=1,100
IF (CSDT(I).LE.0.0) GO TO 307
C7=ALOG(CSDT(I)/CSPP(I))
C9=ALOG(TK)
C3=C7/C9
IF (C3.LT.0.0) GO TO 307
IF (C3.GT.20.) GO TO 308
C8=INT(C3)
K1=IFIX(C8+2.)
COUNT(K1)=COUNT(K1)+1.
CSDTS(K1)=CSDTS(K1)+CSDT(I)
CSDS(K1)=CSDS(K1)+CSDS(I)
CSDGS(K1)=CSDGS(K1)+CSDG(I)
GO TO 301
307 COUNT(I)=COUNT(I)+1.
CSDS(I)=CSDS(I)+CSDS(I)
CSDTS(I)=CSDTS(I)+CSDT(I)
CSDGS(I)=CSDGS(I)+CSDG(I)
GO TO 301
308 COUNT(22)=COUNT(22)+1.
CSDS(22)=CSDS(22)+CSDS(I)
CSDTS(22)=CSDTS(22)+CSDT(I)
CSDGS(22)=CSDGS(22)+CSDG(I)
301 CONTINUE
C CSDTA(L,K) = SAMPLING CROSS-SECTION
DO 310 K=1,22
PR1(K)=COUNT(K)/100.
PR2(L,K)=(PR1(L,K))**2
IF (COUNT(K).EQ.0.0) GO TO 311
CSDTA(L,K)=CSDTS(K)/COUNT(K)
CSDTB(L,K)=CSDTA(L,K)*CSDTA(L,K)
CSDGA(L,K)=CSDGS(K)/COUNT(K)
CSDEA(L,K)=CSDS(K)/COUNT(K)
GO TO 310
311 CSDTA(L,K)=0.0
CSDTB(L,K)=0.0
CSDGA(L,K)=0.0
CSDEA(L,K)=0.0
310 CONTINUE
C COMPUTE THE FACTOR OF FITTING
500 CONTINUE
IF (POTAS.EQ.1.) GO TO 551
SUMP=0.0
SUMP2=0.0
DO 540 L=1,N1
SUMP=SUMP+F(L)
SUMP2=SUMP2+F2(L)
540 CONTINUE
C COMPUTES THE VARIANCE OF F, VARF
VARF=(SUMP2/FLOAT(N1))-(SUMP/FLOAT(N1))**2
AVF=SUMP/FLOAT(N1)
PRINT 550,VARF
550 FORMAT(15H VARIANCE OF F=,F12.5)
551 CONTINUE
C COMPUTES THE VARIANCE OF THE PROBABILITIES VARPR(K)
AND THE PROBABILITY TABLE
DO 560 K=1,22
SUPRO(K)=0.0
560 SUPR2(K)=0.0
DO 570 K=1,22
DO 575 L=1,N1
SUPRO(K)=SUPRO(K)+PR(L,K)
575 SUPR2(K)=SUPR2(K)+PR2(L,K)
PRT(K)=SUPRO(K)/FLOAT(N1)
VARPR(K)=(SUPR2(K)/FLOAT(N1))-(SUPRO(K)/FLOAT(N1))**2
WIPR(K)=SQRT(VARPR(K))
ERPR(K)=WIPR(K)/SQRT(FLOAT(N1))

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C 570 CONTINUE
C COMPUTES THE VARIANCE OF SAMPLING CORRECTED CROSS-SECTIONS VARCS
C AND THE CORRECTED CROSS-SECTION VALUES CCSV
DO 600 K=1,22
SUMCE(K)=0.0
SUMCE2(K)=0.0
SPR(K)=0.0
SUCSS(K)=0.0
SUCS2(K)=0.0
SUMCG(K)=0.0
600 SUMG2(K)=0.0
DO 610 K=1,22
DO 611 L=1,N1
SUMCE(K)=SUMCE(K)+PR(L,K)*CSDEA(L,K)
SUMCE2(K)=SUMCE2(K)+PR(L,K)*CSDEA(L,K)*CSDEA(L,K)
SUCSS(K)=SUCSS(K)+PR(L,K)*CSDTA(L,K)
SUCS2(K)=SUCS2(K)+PR(L,K)*CSDTA(L,K)*CSDTA(L,K)
SUMCG(K)=SUMCG(K)+PR(L,K)*CSDGA(L,K)
SUMG2(K)=SUMG2(K)+PR(L,K)*CSDGA(L,K)**2
611 SPR(K)=SPR(K)+PR(L,K)
IF (SPR(K).EQ.0.0) GO TO 612
CCSVE(K)=SUMCE(K)/SPR(K)
CCSV(K)=SUCSS(K)/SPR(K)
CCSVG(K)=SUMCG(K)/SPR(K)
VARCE(K)=SUMCE2(K)/SPR(K)-(SUMCE(K)/SPR(K))**2
VARCS(K)=(SUCS2(K)/SPR(K)-(SUCSS(K)/SPR(K))**2
VARCG(K)=SUMG2(K)/SPR(K)-(SUMCG(K)/SPR(K))**2
GO TO 610
612 CCSV(K)=0.0
CCSVE(K)=0.0
CCSVG(K)=0.0
VARCS(K)=0.0
VARCG(K)=0.0
610 CONTINUE
DO 635 K=1,22
ERRGP(K)=SQRT (ABS (VARCG (K))) /SQRT (FLOAT (N1))
ERRTP(K)=SQRT (ABS (VARCS (K))) /SQRT (FLOAT (N1))
635 ERREP(K)=SQRT (ABS (VARCE (K))) /SQRT (FLOAT (N1))
PRINT 629
629 FORMAT (9X, 'PROBABILITY TABLE' /
1X, 'UPPER LIMIT', 1X, 'PROBABILITY', 1X, ' ERROR ', 1X, ' TOTAL-X-S'
1X, ' ERROR ', 1X, 'CAPTURE X-S', 1X, ' ERROR ')
CSPP(22)=10000.
DO 631 K=1,22
631 PRINT 630, CSPP(K), PRT(K), ERPR(K), CCSV(K), ERRTP(K), CCSVG(K), ERRGP(K)
)
630 FORMAT (1X, F11.5, 1X, E11.4, 1X, E11.4, 1X, E11.4, 1X, E11.4, 1X, E11.4, 1X, E11.4)
AFGC2=0.0
AFTC2=0.0
AFEC2=0.0
AFGC3=0.0
AFEC3=0.0
DO 653 K=1,22
AFEC3=AFEC3+PRT(K)*CCSV(K)
AFEC2=AFEC2+PRT(K)*CCSVE(K)
AFGC3=AFGC3+PRT(K)*CCSVG(K)
AFTC2=AFTC2+PRT(K)*CCSV(K)**2
653 AFGC2=AFGC2+PRT(K)*CCSVG(K)**2
VFT=AFTC2-AFTCS**2
VFG=AFGC2-AFGCS**2
WFT=SQRT(VFT)
WFG=SQRT(VFG)
XPCG=0.0
XPCG2=0.0
XPCT=0.0
XPCT2=0.0
DO 700 L=1,N1
XPCG=XPCG+SPCG(L)/100.
XPCG2=XPCG2+(SPCG(L)/100.)**2
XPCT=XPCT+SPCS(L)/100.
700 XPCT2=XPCT2+(SPCS(L)/100.)**2
DIN=SQRT(FLOAT(N1))
EFT=SQRT(XPCT2/FLOAT(N1)-(XPCT/FLOAT(N1))**2)/DIN
EFG=SQRT(XPCG2/FLOAT(N1)-(XPCG/FLOAT(N1))**2)/DIN
PRINT 654, AFTCS, EFT, AFGCS, EFG
654 FORMAT (16H AVERAGE=TOT=CS=F12.4, 16H ERROR=F12.4, 16H AVERAGE=GAMMA=
1CS=F12.4, 6H ERROR=F12.4)
CALL BREKO(DICRO, DICRI, N1, EFT, EFG)
CALL SHELF(CSDR, AN1, N1, EFG)
STOP
END

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SUBROUTINE BREKO(DICRO,DICRI,N1,EFT,EPG)
DIMENSION AGDCS(4),ATDCS(4),BFG(4),BFT(4),EBFG(4),EBFT(4),EDTCS(4)
1 EDCCS(4)
DIMENSION VAYPTG(4),VAYPTT(4),COVG(4),COVT(4)
DIMENSION SYPT(4),SYPT2(4),SYPTG(4),SYPTG2(4),SYPTT(4),SYPTT2(4)
DIMENSION ASYPT(4),ASYPTG(4),ASYPTT(4),VAYPT(4)
DIMENSION DENOM(22),DENOI(22)
DIMENSION AFDCS(4),BFF(4),SYPTC(4),SYPTC2(4),ASYPTC(4),COVTC(4)
1 EDCCS(4),VAYPT(4),EBFF(4)
COMMON/DERR/YPT(100,4),YPTG(100,4),YPTT(100,4),YPTC(100,4)
COMMON/DSELF/CCSV(22),PRT(22),CCSVG(22)
C COMPUTE THE GROUP CROSS SECTIONS WITH DILUTE X-SECTION,AGDCS,ATDCS
DICRI=DICRO
DO 50 J=1,4
DICRO=DICRI*10**J
SAVIF=0.0
SAVII=0.0
SAVIG=0.0
SAVIT=0.0
DO 10 K=1,22
DENOM(K)=CCSV(K)*DICRO
SAVII=SAVII+PRT(K)/DENOM(K)
SAVIG=SAVIG+PRT(K)*CCSVG(K)/DENOM(K)
SAVIF=SAVIF+PRT(K)*CCSV(K)/DENOM(K)
10 SAVIT=SAVIT+PRT(K)*(1./DENOM(K)*DENOM(K))
ATDCS(J)=(SAVII/SAVIT)-DICRO
AGDCS(J)=SAVIG/SAVII
AFDCS(J)=SAVIF/SAVII
C COMPUTE THE INFINITE DILUTE CROSS-SECTION IDCSG,IDCST
SAID1=0.0
SAIDG=0.0
SAIDF=0.0
SAIDT=0.0
DO 20 K=1,22
DENOI(K)=CCSV(K)*DICRI
SAID1=SAID1+PRT(K)/DENOI(K)
SAIDG=SAIDG+PRT(K)*CCSVG(K)/DENOI(K)
SAIDF=SAIDF+PRT(K)*CCSV(K)/DENOI(K)
20 SAIDT=SAIDT+PRT(K)*(1./DENOI(K)*DENOI(K))
IDCSG=SAIDG/SAID1
IDCST=SAID1/SAIDT-DICRI
IDCSF=SAIDF/SAID1
C COMPUTE THE BOUDARENKO FACTORS BFG, BFT
BFG(J)=(1./IDCSG)*AGDCS(J)
BFT(J)=(1./IDCST)*ATDCS(J)
BFF(J)=(1./IDCSF)*AFDCS(J)
50 CONTINUE
DO 60 J=1,4
SYPT(J)=0.0
SYPTC(J)=0.0
SYPTC2(J)=0.0
SYPT2(J)=0.0
SYPTT(J)=0.0
SYPTT2(J)=0.0
SYPTG(J)=0.0
SYPTG2(J)=0.0
DO 70 L=1,N1
SYPT(J)=SYPT(J)+YPT(L,J)
SYPT2(J)=SYPT2(J)+YPT(L,J)*YPT(L,J)
SYPTG(J)=SYPTG(J)+YPTG(L,J)
SYPTG2(J)=SYPTG2(J)+YPTG(L,J)*YPTG(L,J)
SYPTC(J)=SYPTC(J)+YPTC(L,J)
SYPTC2(J)=SYPTC2(J)+YPTC(L,J)*YPTC(L,J)
SYPTT(J)=SYPTT(J)+YPTT(L,J)
70 SYPTT2(J)=SYPTT2(J)+YPTT(L,J)*YPTT(L,J)
ASYPTT(J)=SYPTT(J)/FLOAT(N1)
ASYPTC(J)=SYPTC(J)/FLOAT(N1)
ASYPT(J)=SYPT(J)/FLOAT(N1)
ASYPTG(J)=SYPTG(J)/FLOAT(N1)
COVG(J)=0.0
COVT(J)=0.0
COVTC(J)=0.0
DO 71 L=1,N1
COVG(J)=COVG(J)+(1./FLOAT(N1))*(1./FLOAT(N1))*(YPT(L,J)-ASYPT(J))*
1 (YPTG(L,J)-ASYPTG(J))
COVTC(J)=COVTC(J)+(1./FLOAT(N1))*(1./FLOAT(N1))*(YPTC(L,J)-ASYPTC(
1 J))*(YPTT(L,J)-ASYPTT(J))
71 COVT(J)=COVT(J)+(1./FLOAT(N1))*(1./FLOAT(N1))*(YPTT(L,J)-ASYPTT(J))
1*(YPT(L,J)-ASYPT(J))
VAYPT(J)=(1./FLOAT(N1))*(SYPT2(J)/FLOAT(N1)-ASYPT(J)**2)
VAYPTG(J)=(1./FLOAT(N1))*(SYPTG2(J)/FLCAT(N1)-ASYPTG(J)**2)
VAYPTT(J)=(1./FLOAT(N1))*(SYPTT2(J)/FLCAT(N1)-ASYPTT(J)**2)
VAYPTC(J)=(1./FLOAT(N1))*(SYPTC2(J)/FLCAT(N1)-ASYPTC(J)**2)
EDCCS(J)=SQRT((1./ASYPT(J)**2)*VAYPTG(J)+(ASYPTG(J)/ASYPT(J)**2)**2)
12=VAYPT(J)-2.*(ASYPTG(J)/ASYPT(J)**3)*COVG(J)
EDTCS(J)=SQRT((1./ASYPT(J)**2)*VAYPTT(J)+(ASYPTT(J)/ASYPT(J)**2)**2)
12=VAYPT(J)-2.*(ASYPTT(J)/ASYPT(J)**3)*COVT(J)
EDCCS(J)=SQRT((1./ASYPTC(J)**2)*VAYPT(J)+(ASYPT(J)/ASYPTC(J)**2)**2)

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12=VAYPTC(J)=2.*(ASYPT(J)/ASYPTC(J)**3)*COVTC(J)
EBFG(J)=SQRT((1./((DICSG*DICSG))*EDGCS(J)**2*(AGDCS(J)/DICSG**2)**2)
1=EPG**2)
EBFF(J)=SQRT((1./((DICSF*DICSF))*EDTCS(J)**2*(AFDCS(J)/DICSF**2)**2)
1=EPT**2)
60 EBPT(J)=SQRT((1./((DICST*DICST))*EDCCS(J)**2*(ATDCS(J)/DICST**2)**2)
1=EPT**2)
PRINT 57
57 FORMAT(' BONDARENKO GROUP CROSS SECTIONS  (//)
PRINT 55
55 FORMAT(' AWFY AVERAGE WEIGHTED FLUX TOTAL X-SECTION,AWCT AVERAGE
WEIGHTED CURRENT TOTAL X-SECTION  (/)
PRINT 59
59 FORMAT(' DILUTION CAPTURE X-SECTION ERROR AWFY X-SECT
ION ERROR AWCT=X-SECTION ERROR')
DO 62 J=1,4
DICRO=DICR1*10.**J
62 PRINT 63,DICRO,AGDCS(J),EDGCS(J),AFDCS(J),EDTCS(J),ATDCS(J),EDCCS(
J)
63 FORMAT(6X,F7.1,6X,F12.4,5X,F7.4,5X,F12.4,3X,F7.4,3X,F12.4,3X,F7.4)
PRINT 58
58 FORMAT(' BONDARENKO SELF-SHIELDING FACTORS  (//)
PRINT 69
69 FORMAT(' BFT BONDARENKO WEIGHTED FLUX SELF SHIELDING FACTOR'/
BFC BONDARENKO WEIGHTED CURRENT SELF SHIELDING FACTOR')
PRINT 68
68 FORMAT(' DILUTION CAPTURE FACTOR ERROR BFC FACTOR
ERROR BFF FACTOR ERROR')
DO 66 J=1,4
DICRO=DICR1*10.**J
66 PRINT 67,DICRO,BFG(J),EBFG(J),BFT(J),EBFT(J),BFF(J),EBFF(J)
67 FORMAT(6X,F7.1,6X,F8.5,5X,F8.5,6X,F8.5,6X,F8.5,3X,F8.5,5X,F8.5)
RETURN
END

SUBROUTINE BREDIE,EREF,AP,AWR1,R,T,SPI,CSDG,CSDT,CSP,CSDI)
C THIS SUBROUTINE COMPUTES THE DOPPLER BROADENED TOTAL CROSS SECTION
AND GAMMA CROSS SECTION, CSDT AND CSDG.
DIMENSION CSP1(3),G(3,6),GN(3,6,150),CSDG3(3,6,150),CSDG1(3,6),
ICSDG2(3),CSDT3(3,6),CSDT4(3,6,150),CSDT5(3)
COMMON/UBWED/ER(3,6,150),GNB(3,6,150),AGG(3,6),NR(3,6),
IEL(3,6),EL(3,6),NJS(3),AJ(3,6),AGND(3,6)
COMMON/CSIF/FI(3)
COMMON/DVIL/V(3)
DATA INDICE/0/
SE=SQRT(E)
IF(INDICE.EG.1) GO TO 10
INDICE=1
SE=SQRT(EREF)
SAF=2.196771*(AWR1/(AWR1+1.))*SEF/1000.
SIGO=(6.51*10.**5/EREF)*((AWR1+1.)/AWR1)**2
R03=SAF*AP
DELTA=SQRT(3.446*EREF*T/AWR1)/100.
CALL VIL(R03)
CALL SHIF(RC)
DC 40 I=1,3
40 CSP1(I)=2.*(FLOAT(I)-1.)+1.)*SIGO*(SIN(FI(I)))**2
CSP=CSP1(1)+CSP1(2)+CSP1(3)
DC 50 I=1,3
NJSI=NJS(I)
50 G(I,J)=(2.*AJ(I,J)+1.)/(4.*SPI+2.)
10 CONTINUE
FA=(LAGND(I,1)+SE+AGG(I,1))/(4.*SA)
FB=(EU(I,1)-EL(I,1)+20.)/((EL(I,1)+E+10.)*(E-EL(I,1)+10.))
FC=2.1875*AP*ALOG((E-EL(I,1)+11.84)/(EU(I,1)-E+11.84))/1000.
FVS=1.313*10.**5*AGND(I,1)*(FA*FB-FC)
C COMPUTE DOPPLER BROADENED GAMMA CROSS SECTIONS, CSDG.
C COMPUTE DOPPLER BROADENED TCTAL CROSS-SECTION.
DC 100 I=1,3
NJSI=NJS(I)
DC 100 J=1,NJSI
NR=NR(I,J)
DO 100 K=1,NRI
GN(I,J,K)=GN0(I,J,K)*V(I)*SEF
ADJ=3.544667*SIGO*G(I,J)
BDEGN(I,J,K)=AGG(I,J)/((GN(I,J,K)+AGG(I,J))*DELTA)
BDI=GN(I,J,K)/DELTA
X=(ER(I,J,K)-E)/DELTA
Y=(GN(I,J,K)+AGG(I,J))/(2.*DELTA)
CALL SVS(X,Y,LEVI)
CSDG3(I,J,K)=ADJ*BDEGN
CSDT1=ADJ*BDI*COS(2.*FI(I))*U
CSDT3=ADJ*BDI*SIN(2.*FI(I))*V

```

```

100 CSDT4(I,J,K)=CSDT1-CSDT2
    DO 300 I=1,J
      NJSI=NJS(I)
      DO 300 J=1,NJSI
        CSDT3(I,J)=0.0
        CSDG1(I,J)=0.0
        NRI=NR(I,J)
        DO 300 K=1,NRI
          CSDG1(I,J)=CSDG1(I,J)+CSDG3(I,J,K)
300 CSDT3(I,J)=CSDT3(I,J)+CSDT4(I,J,K)
        DO 301 I=1,J
          CSDT5(I)=0.0
          CSDG2(I)=0.0
          NJSI=NJS(I)
          DO 301 J=1,NJSI
            CSDG2(I)=CSDG2(I)+CSDG1(I,J)
301 CSDT5(I)=CSDT5(I)+CSDT3(I,J)
          CSDG2(I)=CSDG2(I)+CSDG2(I)
          CSDT=CSDT5(1)+CSDT5(2)+CSDT5(3)+CSP
          CSDT=CSDT+FVS
          CSDG=CSDT-CSDG
        RETURN
      END

```

```

SUBROUTINE SHELF(CSDR,AN1,N1,EPG)
COMMON/DSED/ATCS(100),SPCG(100)
C COMPUTES AVERAGE TRANSMISSION, AVERAGE SELF-INDICATION RATIO,
C TRANSMISSION SELF-SHIELDING FACTOR, SELF INDICATION RATIO=
C SELF-SHIELDING FACTOR.
C DIMENSION EXFLUM(100),EXFLU2(100),EXFLUT(100),EXFLT2(100),EXSIR(10
10),EXSIR2(100),EXAS1(100),EXAS2(100)
C DIMENSION EFLUC(22),EFLUD(22)
COMMON/DSELF/CCSV(22),PRT(22),CCSVG(22)
C COMPUTES THE TRANSMISSION SELF-SHIELDING FACTOR, TSSF
DIN=FLOAT(N1)
DIN=SQRT(FLOAT(N1))
PRINT 5
5 FORMAT(' AVERAGE TRANSMISSION ATR,TRANSMISSION SELF SHIELDING FAC
10 TOR TSSF//
2' AVERAGE SELF INDICATION RATIO SIR AND SELF INDICATION SELF SH
IELDING FACTOR SIRSS'//)
PRINT 6
6 FORMAT(' ATOM/BARRN AT ERROR TSSF ERROR SIR ER
10 ROR SIRSS ERROR'//)
DO 40 J=1,10
  TSSF=0.0
  TSSF2=0.0
  AN1=AN1+0.01
  DO 10 K=1,22
    EFLUC(K)=EXP(-AN1*(CCSV(K)-CSDR))
    TSSF2=TSSF2+PRT(K)*(EFLUC(K))**2
  10 TSSF=TSSF+PRT(K)*EFLUC(K)
  C COMPUTES THE AVERAGE TRANSMISSION, ATR
  ATR=TSSF*EXP(-AN1*CSDR)
  C COMPUTES THE SELF-INDICATION RATIO=SELF-SHIELDING-FACTOR, SIRSS
  SIRSS=0.0
  DO 20 K=1,22
    EFLUD(K)=CCSVG(K)*EFLUC(K)
  20 SIRSS=SIRSS+PRT(K)*EFLUD(K)
  C COMPUTES THE AVERAGE SELF-INDICATION RATIO, ASIR
  SUMG2=0.0
  DO 30 K=1,22
    SUMG2=SUMG2+PRT(K)*CCSVG(K)
  30 ASIR=SIRSS*EXP(-AN1*CSDR)/SUMG2
  DO 41 L=1,N1
    EXFLUM(L)=EXP(-AN1*(ATCS(L)-CSDR))
    EXFLU2(L)=EXP(-AN1*ATCS(L))
    EXFLUT(L)=EXP(-AN1)*EXFLUM(L)
    EXFLT2(L)=EXFLUT(L)*EXFLUT(L)
    EXSIR(L)=(SPCG(L)/100.)*EXFLUM(L)
    EXSIR2(L)=EXSIR(L)*EXSIR(L)
  41 EXAS1(L)=(SPCG(L)/100.)*EXFLUT(L)
    EXAS2(L)=EXAS1(L)*EXAS1(L)
    SEFLUM=0.0
    SEFLU2=0.0
    SEFLUT=0.0
    SEFLT2=0.0
    SESIR=0.0
    SESIR2=0.0
    SEAS1=0.0
    SEAS2=0.0

```

```

SEAS12=0.0
DO 50 L=1,N1
SEFLUM=SEFLUM+EXFLUM(L)
SEFLU2=SEFLU2+EXFLU2(L)
SEFLUT=SEFLUT+EXFLUT(L)
SEFLT2=SEFLT2+EXFLT2(L)
SESIR=SESIR+EXSIR(L)
SESIR2=SESIR2+EXSIR2(L)
50 SEAS11=SEAS11+EXAS11(L)
SEAS12=SEAS12+EXAS12(L)
ERTSF=SQRT((SEFLU2/DIN2-(SEFLUM/DIN2)**2)/DIN)
ERAT=SQRT((SEFLT2/DIN2-(SEFLUT/DIN2)**2)/DIN)
ERSIR1=SQRT((SESIR2/DIN2-(SESIR/DIN2)**2)/DIN)
ERSIR2=SQRT((SESIR2/DIN2-(SESIR/DIN2)**2)/DIN)
ERSIR1=SQRT((SEAS12/DIN2-(SEAS11/DIN2)**2)/DIN)
ERSIR2=SQRT((SEAS12/DIN2-(SEAS11/DIN2)**2)/DIN)
ERSIR=SQRT((1./SUMG2**2)*ERSIR1**2+(SIRSS*EXP(-AN1*CSDR)/SUMG2**2)*
1**2*EFG**2)
PRINT 60,ANI,ATR,ERAT,Y55F,ERTSF,ASIR,ESIR,SIRSS,ERSIRF
60 FORMAT(1X,F8.4,2X,F7.5,2X,F7.4,2X,F8.4,2X,F7.4,2X,F7.4,2X,F7.4,2X,
1F7.4,2X,F7.4)
40 CONTINUE
RETURN
END

```

```

SUBROUTINE SHIF(RO)
COMMON/OSIF/FI(3)
FI(1)=RO
FI(2)=RO-ATAN(RO)
FI(3)=RO-ATAN(3.*RO/(3.-RO*RO))
RETURN
END

```

```

SUBROUTINE VIL(RO1)
COMMON/DVIL/V(3)
V(1)=RO1
V(2)=RO1*RO1/(1.+RO1*RO1)
V(3)=RO1**4/(9.+3.*RO1*RO1+RO1**4)
RETURN
END

```

```

SUBROUTINE SVS(A,B,C,D)
COMMON/TRTI/TR(62,62),TI(62,62),AIMW,AX,KI,REW,YI
DATA K/0/
IF(K.EQ.1) GO TO 3
K=1
KI=1
X=0.1
DO 2 I=1,62
Y=0.1
DO 1 J=1,62
1 CALL W(X,Y,TR(I,J),TI(I,J))
2 X=X+.1
3 CONTINUE
AX=A
YI=B
CALL QUICKW
C=REW
D=AIMW
RETURN
END

```

OK 0090
OK 0100

```

SUBROUTINE W (REZ, AIM, REW, AIMW)
REW=0.
AIMW=0.
AIMZ=ABS (AIM)
IF (REZ) 27, 2001, 27
2001 IF (AIM) 27, 2002, 27
2002 REW=1.
RETURN
27 RZ=REZ*REZ
AIZ=AIMZ*AIMZ
ABREZ=ABS (REZ)
IF (ABREZ+1.35*AIMZ-5.0) 102, 102, 100
100 IF (ABREZ+1.1*AIMZ-6.6) 117, 117, 116
101 IF (ABREZ+1.43333*AIMZ-4.3) 119, 119, 118
102 IF (ABREZ+1.863636*AIMZ-4.1) 111, 111, 104
103 IF (AIMZ-1.5) 110, 120, 120
104 IF (AIMZ-1.4) 115, 115, 101
105 IF (ABREZ+1.07317*AIMZ-4.4) 119, 119, 118
106 IF (ABREZ+2.7) 127, 128, 128
107 IF (ABREZ+3.1) 106, 108, 108
108 IF (ABREZ+3.4) 129, 130, 130
109 IF (RZ+1.18*AIZ-5.74) 103, 107, 107
110 IF (RZ+1.7227*AIZ-4.4) 125, 126, 126
111 IF (RZ+1.71*AIZ-2.89) 113, 109, 109
112 IF (RZ+1.69*AIZ-1.69) 123, 124, 124
113 IF (RZ+2.0408*AIZ-1.0) 114, 112, 112
114 IF (RZ+1.5825*AIZ-2.25) 121, 122, 122
115 IF (ABREZ+1.43333*AIMZ-4.3) 120, 120, 105
116 NMAX=1
GO TO 15
117 NMAX=2
GO TO 15
118 NMAX=3
GO TO 15
119 NMAX=4
GO TO 15
120 NMAX=6
GO TO 15
121 NMAX=2
GO TO 20
122 NMAX=3
GO TO 20
123 NMAX=4
GO TO 20
124 NMAX=5
GO TO 20
125 NMAX=6
GO TO 20
126 NMAX=7
GO TO 20
127 NMAX=8
GO TO 20
128 NMAX=9
GO TO 20
129 NMAX=10
GO TO 20
130 NMAX=11
GO TO 20
20 KW=2
AIMZ=AIM1
GO TO 200
19 KW=1
IF (AIM1) 2000, 150, 150
2000 KW=2
AIMZ=AIM1
GO TO 200
C WA IS OBTAINED FROM ASYMTOTIC SERIES
150 RV=2.*(RZ-AIZ)
AK=4.*REZ*AIMZ
EL=AK
H=0.
B=0.
A=0.
TEMP=0.
TEME=0.
G=1.
C=1.1283792*AIMZ
D=1.1283792*REZ
AM=RV-1.
AAK=1.
K=0
11 AJTEMP=2.*AAK
TEMP4=(1.-AJTEMP)*AJTEMP
AJR=RV*(4.*AAK+1.)
GO TO 40

```



```

41 AK=AAK*1,
   K=K*1
   PR=REW
   PI=AIMW
12 AMAGN=TEMPM**2*TEHEL**2
   REW=(TEMPC*TEMPM*TEMPO*TEHEL)/AMAGN
   AIMW=(TEMPM*TEMPO*TEHEL*TEMPC)/AMAGN
   IF (ABS (REW-PR)=-1,E=6)665,11,11
665 IF (ABS (AIMW-PI)=-1,E=6)665,11,11
68 RETURN
C WT IS OBTAINED FROM TAYLOR SERIES
200 TEMP1=RZ*A12
   TEMP2=RZ*TEMP1*TEMP1
   AJ=(RZ-A12)/TEMP2
   AK=2.*REZ*AIMZ/TEMP2
   C=0.
   SW=0.
   AJSIG=0.
   D=0.
   JSIG=0
   GW=0.
   H=0.
   EL=0.
   A=1.
   AM=1.
   SIG=1.5
   EXPON=EXP (TEMP2*AJ)
   EXPC=EXPON*COS (TEMP2*AK)
   EXPS=EXPON*SIN (TEMP2*AK)
   SIG2P=2.*SIG
4 AJ*SIG=4.*AJSIG
   AJ*SM1=AJ*SIG-1.
   TEMP3=1./ (AJ*SM1*(AJ*SIG+3.))
   TT4=SIG2P*(2.*AJSIG-1.)
   TEMP4=TT4/(AJ*SM1*(AJ*SIG+1.)*(AJ*SIG+3.)*AJ*SM1)
   AJP=AJ*TEMP3
   GO TO 40
42 AJSIG=AJSIG+1.
   JSIG=JSIG+1
6 TEMP7=(AM*AM*EL*EL)*1.7724539
   REF=(AIMZ*(C*AM*D*EL)-REZ*(AM*D-C*EL))/
1 TEMP7/TEMP1
   AIMP=(AIMZ*(AM*D-C*EL)+REZ*(C*AM
   *D*EL))/TEMP7/TEMP1
   PR=REW
   PI=AIMW
   REW=EXPC-REF
   AIMW=EXPS-AIMP
   IF (ABS (REW-PR)=-1,E=6)664,7,7
664 IF (ABS (AIMW-PI)=-1,E=6)664,7,7
64 RETURN
7 SIG2P=2.*AJSIG
   GO TO 4
40 TEMPC=AJP*C*TEMP4*A-AK*D
   TEMPO=AJP*D*TEMP4*B-AK*C
   TEHEL=AJP*EL*TEMP4*H-AK*AM
   TEMPM=AJP*AM*TEMP4*G-AK*EL
   ARC
   B=D
   GB=AM
   HB=EL
   CB=TEMPC
   DB=TEMPO
   AMB=TEMPM
   EL=TEHEL
43 IF (ABS (TEMPM)*ABS (TEHEL)-1.0E15)49,49,43
   C=1.0E-15*C
   D=1.0E-15*D
   AM=1.0E-15*AM
   EL=1.0E-15*EL
   TEMPC=1.0E-15*TEMPC
   TEMPO=1.0E-15*TEMPO
   TEMPM=1.0E-15*TEMPM
   TEHEL=1.0E-15*TEHEL
   GO TO 50
49 IF (ABS (TEMPM)*ABS (TEHEL)-1.0E15)66,66,50
44 C=1.0E15*C
   D=1.0E15*D
   AM=1.0E15*AM
   EL=1.0E15*EL
   TEMPC=1.0E15*TEMPC
   TEMPO=1.0E15*TEMPO
   TEMPM=1.0E15*TEMPM
   TEHEL=1.0E15*TEHEL
50 GO TO (41,42,12345).KW
12345 RETURN
END

```

SOURCE,EBDCIC,NOLIST,NODECK,LOAD,MAP,NOEDIT,NOXREF	
SUBROUTINE QUICKW	QUIC0010
COMMON/TRTI/TR(62,62),TI(62,62),AIMW,AX,KI,REW,Y	QUIC0020
AKI=SIGN(1.,AX)	QUIC0030
X=ABS(AX)	QUIC0040
TEST=X*X*Y*Y	QUIC0050
IF(TEST.LT.36.)GO TO 10	QUIC0060
IF(TEST.LT.144.)GO TO 2	QUIC0070
IF(TEST.LT.10000.)GO TO 3	QUIC0080
A1=1./(1.7724539*TEST)	
REW=Y*A1	
IF(KI.GT.0)AIMW=X*A1*AKI	QUIC0100
RETURN	QUIC0110
10 I1=X*10.	QUIC0120
J1=Y*10.	QUIC0130
I1=I1*2	QUIC0140
J1=J1*2	QUIC0150
N1=J1	QUIC0160
P1=10.*X-I1	QUIC0170
Q1=10.*Y-J1	QUIC0180
15 P2=P1*P1	QUIC0190
Q2=Q1*Q1	QUIC0200
R2=P2*Q2	QUIC0210
HP=5*P	QUIC0220
HQ=5*Q	QUIC0230
HQ2=5*Q2	QUIC0240
HP2=5*P2	QUIC0250
A1=HP2*HQ	QUIC0260
A2=HP2*HP	QUIC0270
A3=1.*PQ=P2*Q2	QUIC0280
A4=HP2*PQ*HP	QUIC0290
A5=HQ2*PQ*HQ	QUIC0300
REW=A1*TR(I,N)+A2*TR(I-1,J)+A3*TR(I,J)+A4*TR(I+1,J)+A5*TR(I,J+1)	QUIC0310
1*PQ*TR(I+1,J+1)	QUIC0320
IF(KI.LE.0)GO TO 8	QUIC0330
3 AIMW=A1*TI(I,N)+A2*TI(I-1,J)+A3*TI(I,J)+A4*TI(I+1,J)+A5*TI(I,J+1)	QUIC0340
1*PQ*TI(I+1,J+1)	QUIC0350
AIMW=AIMW*AKI	QUIC0360
GOTO 8	QUIC0370
2 A1=X*X*Y*Y	QUIC0380
A2=2.*X*Y	QUIC0390
A3=A2*A2	QUIC0400
A4=A1-.2752551	QUIC0410
A5=A1-.725745	QUIC0420
D1=.8124242/(A4*A4*A3)	QUIC0430
D2=.05176536/(A5*A5*A3)	QUIC0440
REW=D1*(A2*X-A4*Y)+D2*(A2*X-A5*Y)	QUIC0450
IF(KI.LE.0)GO TO 8	QUIC0460
7 AIMW=D1*(A4*X	QUIC0470
+A2*Y)+D2*(A5*X+A2*Y)	QUIC0480
AIMW=AIMW*AKI	QUIC0490
GOTO 8	QUIC0500
3 A1(X*X*Y*Y)*2.	
A2=4.*X*Y	QUIC0520
A4=A1-1.	QUIC0530
D1=.1283792/(A4*A4*A2*A2)	QUIC0540
REW=D1*(A2*X-A4*Y)	QUIC0550
IF(KI.LE.0)GO TO 8	QUIC0560
9 AIMW=D1*(A4*X+A2*Y)	QUIC0570
AIMW=AIMW*AKI	QUIC0580
8 RETURN	QUIC0590
END	QUIC0600

Appendix II. Sample Program

A. Listing of Input

```

PROGRAM PAPIN VERSION FEBRUARY 1981

NUMBER OF LADDERS=100
      0.1000      100000.0
1
NEUTRON ENERGY= 4000.00
SCATTERING LENGTH= 0.4900
ATOMIC WEIGHT= 239.000
CHANNEL RADIUS= 0.8400
TEMPERATURE= 2000.00
TOTAL REFERENCE CROSS-SECTION= 17.9500
NRZ=100
NUCLEAR SPIN= 0.0
INITIAL THICKNESS IN ATOM/BARN= 0.0100
COMPENSATION CROSS SECTION= 1.2050
1 2 2
UNRESOLVED RESONANCE PARAMETERS
L J D AGNO AMUN AGO
1 0.5000E 00 0.2000E 02 0.2100E-02 1.0 0.2350E-01
2 0.5000E 00 0.2000E 02 0.1549E-02 1.0 0.2350E-01
3 0.1500E 01 0.1000E 02 0.7745E-03 1.0 0.2350E-01
4 0.1500E 01 0.1000E 02 0.2500E-02 1.0 0.2350E-01
5 0.2500E 01 0.6667E 01 0.1667E-02 1.0 0.2350E-01
    
```

B. Listing of Output

```

PROBABILITY TABLE
UPPER LIMIT PROBABILITY ERROR TOTAL-X=S ERROR CAPTURE X=S ERROR
2.00000 0.0 0.0 0.0 0.0 0.0 0.0
2.48189 0.3000E-03 0.2216E-03 0.2238E 01 0.7436E-02 0.2221E 00 0.7498E-02
3.07990 0.1000E-03 0.9950E-04 0.3059E 01 0.2184E-03 0.1830E 00 0.1057E-04
3.62199 0.3000E-03 0.1706E-03 0.3653E 01 0.9800E-02 0.4123E 00 0.2021E-01
4.74288 0.1500E-02 0.3841E-03 0.4418E 01 0.2470E-01 0.2762E 00 0.2420E-01
5.88568 0.1900E-02 0.4170E-03 0.5378E 01 0.2818E-01 0.1774E 00 0.1134E-01
7.30379 0.1098E-01 0.1069E-02 0.6718E 01 0.2721E-01 0.2223E 00 0.1491E-01
9.06362 0.6000E-01 0.2130E-02 0.8358E 01 0.2668E-01 0.2423E 00 0.1491E-01
11.24746 0.2302E 00 0.6509E-02 0.1040E 02 0.1161E-01 0.2847E 00 0.3374E-02
13.98750 0.3264E 00 0.7131E-02 0.1237E 02 0.1456E-01 0.4371E 00 0.9793E-02
17.32051 0.1317E 00 0.3493E-02 0.1830E 02 0.2721E-01 0.9953E 00 0.2289E-01
21.49382 0.7170E-01 0.2446E-02 0.1918E 02 0.4826E-01 0.1574E 01 0.3526E-01
26.67268 0.4910E-01 0.2112E-02 0.2393E 02 0.6248E-01 0.2066E 01 0.4113E-01
33.09937 0.3940E-01 0.1948E-02 0.2956E 02 0.9742E-01 0.2337E 01 0.5431E-01
41.07459 0.2560E-01 0.1567E-02 0.3877E 02 0.1319E 00 0.2641E 01 0.6433E-01
50.92731 0.2200E-01 0.1489E-02 0.4859E 02 0.1748E 00 0.2777E 01 0.8828E-01
63.97269 0.1490E-01 0.1247E-02 0.5899E 02 0.2354E 00 0.3040E 01 0.9321E-01
78.49319 0.1170E-01 0.1068E-02 0.7008E 02 0.3187E 00 0.3258E 01 0.9218E-01
97.40785 0.8000E-02 0.7724E-03 0.8740E 02 0.4394E 00 0.3304E 01 0.9894E-01
120.87846 0.4300E-02 0.6420E-03 0.1075E 03 0.5194E 00 0.4132E 01 0.9501E-01
150.00000 0.1400E-02 0.4470E-03 0.1314E 03 0.8188E 00 0.3137E 01 0.5669E-01
1000.00000 0.1000E-02 0.3000E-03 0.1742E 03 0.2632E 01 0.3118E 01 0.5849E-01
AVERAGE-TOT-CSS= 18.0719 ERROR 0.1887 AVERAGE-GAMMA-CSS 0.9332 ERROR 0.0103
BONDARENKO GROUP CROSS SECTIONS
    
```

```

AWPT AVERAGE WEIGHTED FLUX TOTAL X-SECTION AWCT AVERAGE WEIGHTED CURRENT TOTAL X-SECTION
DILUTION CAPTURE X-SECTION ERROR AWPT X-SECTION ERROR AWCT X-SECTION ERROR
1.0 0.6399 0.0047 13.7304 0.0491 11.9915 0.0810
10.0 0.7095 0.0073 14.4894 0.0823 12.9935 0.0879
100.0 0.8566 0.0091 16.4882 0.1344 18.4380 0.1122
1000.0 0.9223 0.0101 17.8477 0.1799 17.6360 0.4688
BONDARENKO SELF-SHIELDING FACTORS
    
```

```

BFF BONDARENKO WEIGHTED FLUX SELF SHIELDING FACTOR
BFC BONDARENKO WEIGHTED CURRENT SELF SHIELDING FACTOR
    
```

```

DILUTION CAPTURE FACTOR ERROR BFF FACTOR ERROR BFC FACTOR ERROR
1.0 0.68579 0.01045 0.98619 0.00831 0.75988 0.00881
10.0 0.76040 0.01152 0.72146 0.00823 0.80629 0.00957
100.0 0.91897 0.01407 0.86878 0.01104 0.92666 0.01223
1000.0 0.98846 0.01541 0.97978 0.02767 0.98771 0.01432
AVERAGE TRANSMISSION ATR TRANSMISSION FACTOR TSSF
AVERAGE SELF INDICATION HATIO SIR AND SELF INDICATION SELF SHIELDING FACTOR SIRSS
    
```

```

ATOM/BARN AT ERR TSSF ERROR SIR ERROR SIRSS ERROR
0.0200 0.72104 0.0046 1.0325 0.0039 0.5927 0.0089 0.7920 0.0081
0.0300 0.62230 0.0033 1.0663 0.0056 0.4740 0.0070 0.7610 0.0052
0.0400 0.54045 0.0036 1.1061 0.0075 0.3888 0.0057 0.7438 0.0072
0.0500 0.47153 0.0038 1.1569 0.0093 0.3216 0.0048 0.7362 0.0073
0.0600 0.41206 0.0038 1.2121 0.0112 0.2686 0.0041 0.7359 0.0078
0.0700 0.36252 0.0037 1.2736 0.0130 0.2261 0.0036 0.7413 0.0084
0.0800 0.31906 0.0035 1.3413 0.0149 0.1915 0.0033 0.7514 0.0097
0.0900 0.28137 0.0033 1.4154 0.0168 0.1631 0.0029 0.7658 0.0109
0.1000 0.24856 0.0031 1.4962 0.0186 0.1396 0.0027 0.7840 0.0123
0.1100 0.21991 0.0029 1.5840 0.0205 0.1199 0.0024 0.8057 0.0137
    
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