

Nuclear Data Testing at AECL

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Outline

- $n + {}^{16}\text{O}$ at low neutron energy
-

- TSL ($S(\alpha, \beta)$) for H_2O , D_2O
-

Collaboration with

K. Kozier (retired), J.C. Chow (AECL),

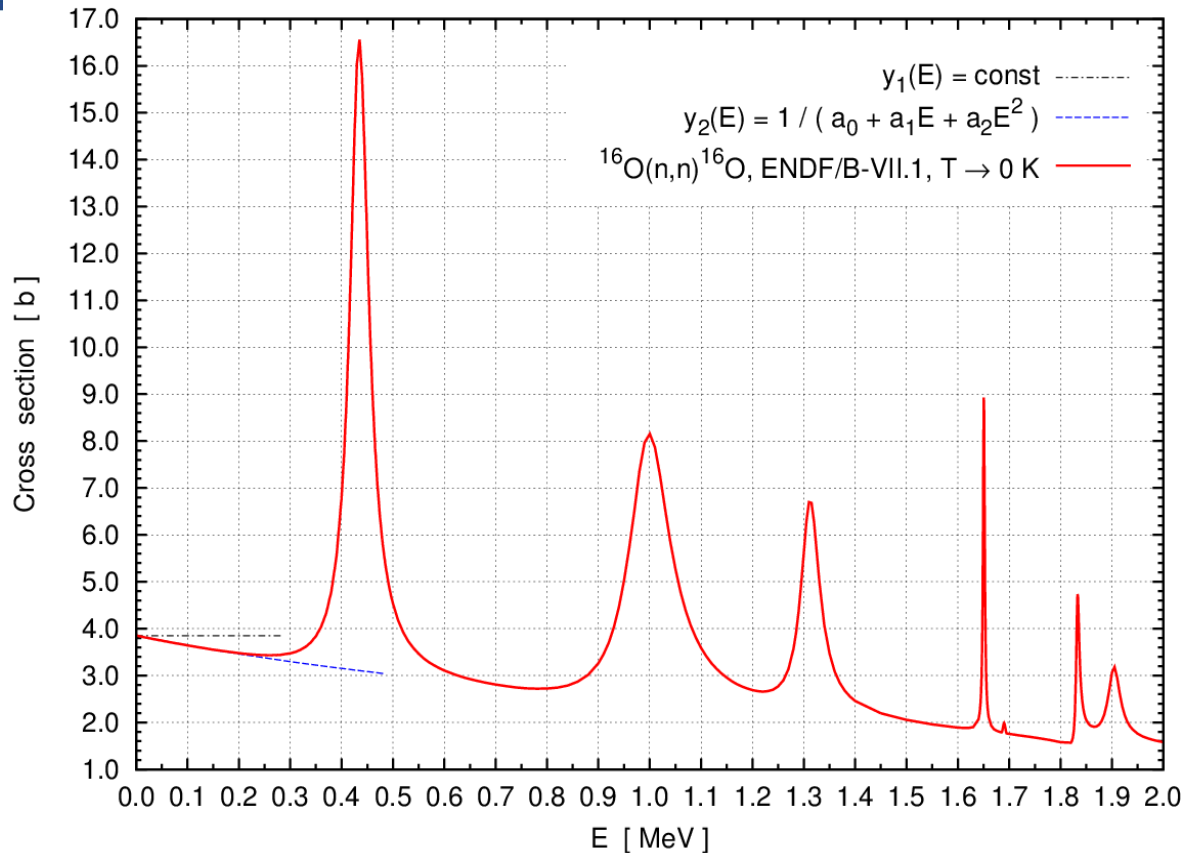
A. Plompen, S. Kopecky (IRMM, Belgium),

J.I. Márquez Dámian (Bariloche, Argentina),

J. Svenne (U of Manitoba, Canada)

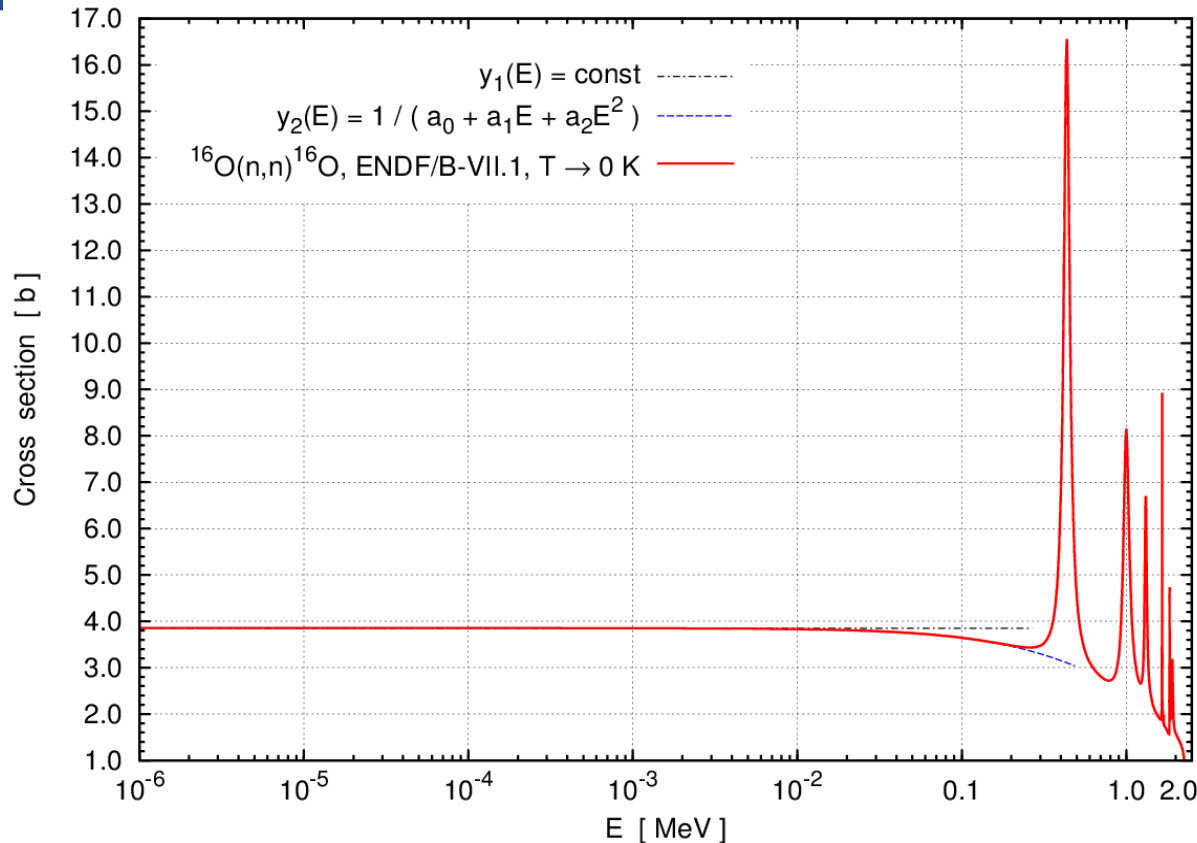
L. Canton (Istituto Nazionale di Fisica Nucleare, Italy)

Elastic neutron scattering cross sections of ^{16}O at low E (from **nuclear physics** standpoint)



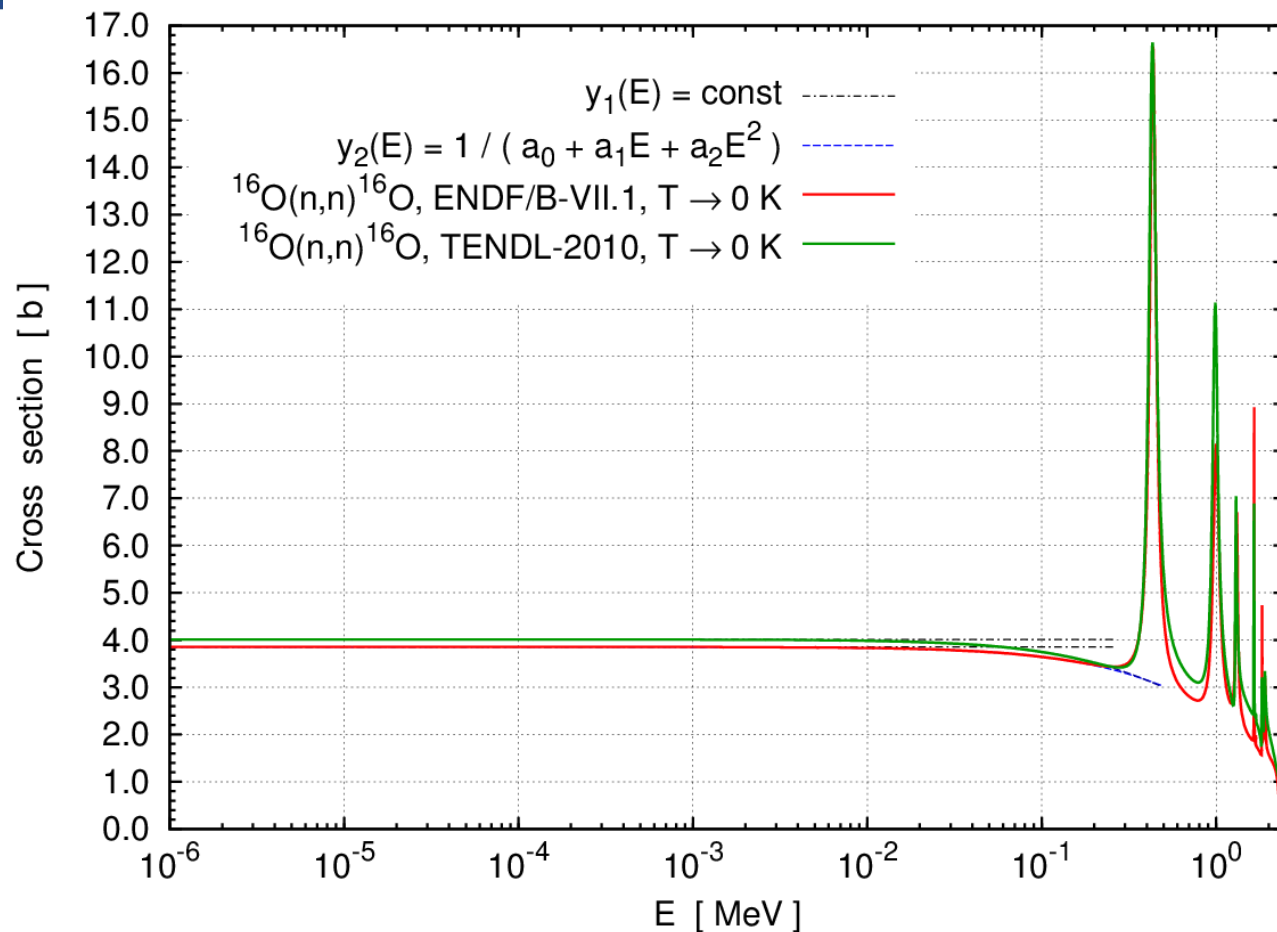
- In the limit of $E \rightarrow 0$ (better, $E \ll 0.1$ MeV),
 $\sigma_s(^{16}\text{O})$ vs. E approaches a constant (≈ 3.85 b in ENDF/B-VII.1)
This $E = 0$ limit is for neutron scattering x-sections at $T = 0$ K,
or n scattering on target-at-rest, free nuclide (MF3, MT2 in ENDF-6 file)

Elastic neutron scattering cross sections of ^{16}O at low E (for **Reactor Physics** applications)



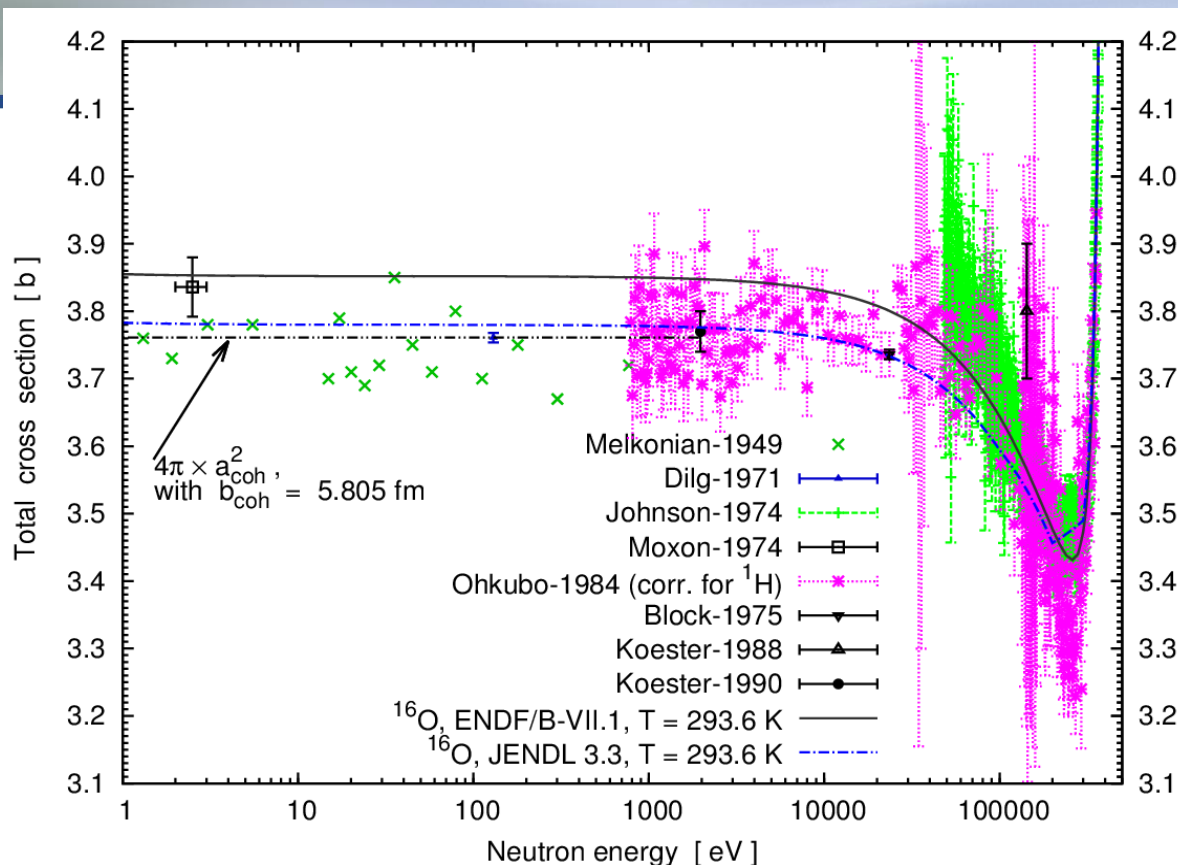
- At $E < 0.01 \text{ MeV}$, $\sigma_s(E) \approx \text{const}$ works well, and $\text{const} = \sigma_{s, \text{th}}$.
- For $E < 0.2 \text{ MeV}$, $\sigma_s(E) \approx 1 / (a_0 + a_1E + a_2E^2)$, (effective-range approx.).
- If $T \neq 0 \text{ K}$, Doppler broadening modifies $\sigma_s(E) \rightarrow \sigma_s(E; T)$ at $E < 1 - 10 \text{ eV}$; usually, use Free Gas Model, but also $^{16}\text{O-in-UO}_2$, $^{16}\text{O-in-D}_2\text{O}$, etc.

Elastic neutron scattering cross sections of ^{16}O at low E (for **Reactor Physics** applications)



- If $T \neq 0 \text{ K}$, Doppler broadening modifies $\sigma_s(E) \rightarrow \sigma_s(E; T)$ at $E < 1 - 10 \text{ eV}$; usually, use Free Gas Model, but need ^{16}O -in- UO_2 , ^{16}O -in- BeO , ^{16}O -in- D_2O , etc.
- TSL** needs $\sigma_{s, \text{th}} \pm \Delta\sigma_{s, \text{th}}$, so check $\sigma_{s, \text{th}}$ of ^{16}O in different evaluations ...

Measurements at low energy ($E < 0.3 - 0.4$ MeV)



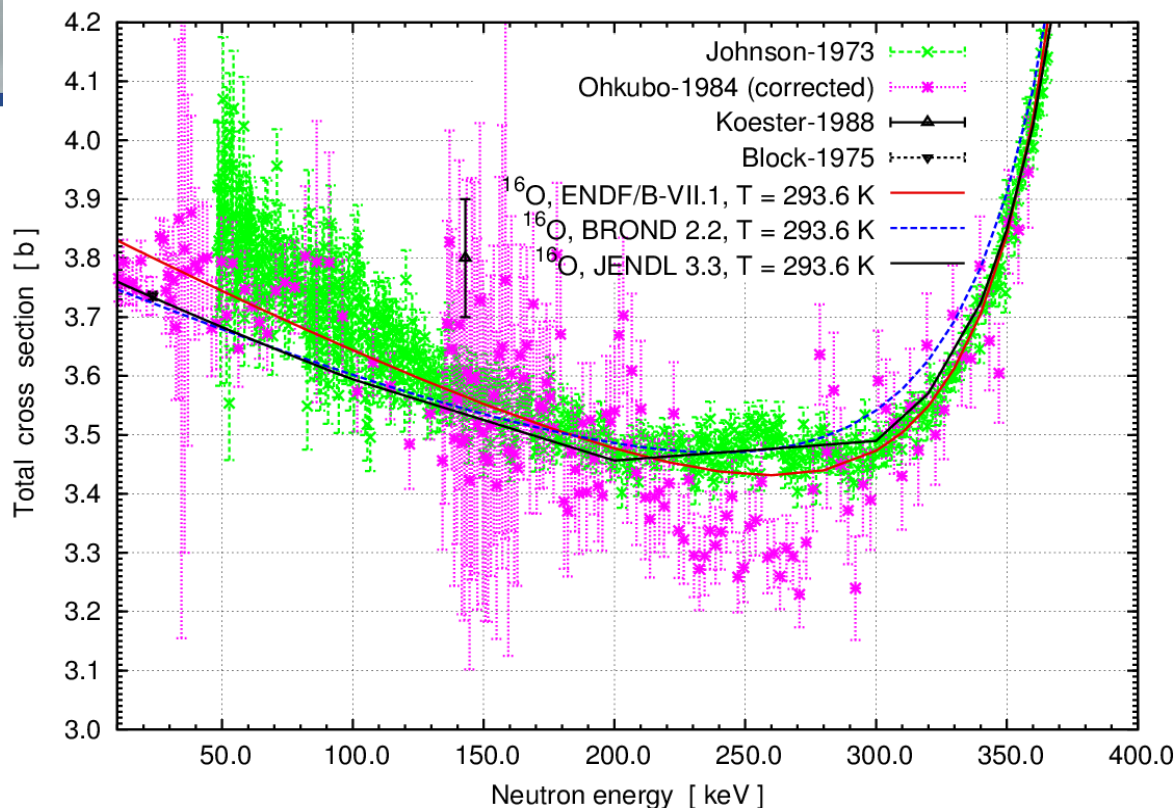
- **Johnson-1974:** unexpected behaviour at $E < 0.2$ MeV , σ_{tot} from **BeO** and **Be**, sample quality ?

C.H. Johnson *et al.*, "The O-16 + n total cross section: diagnostics and refinements," Report **ORNL-4937**, pp. 195-196 , (1974).

- **Ohkubo-1984:** σ_{tot} from **Al₂O₃** and **Al**; data corrected for **H** in Al₂O₃ (A. Plompen & S. Kopecky)

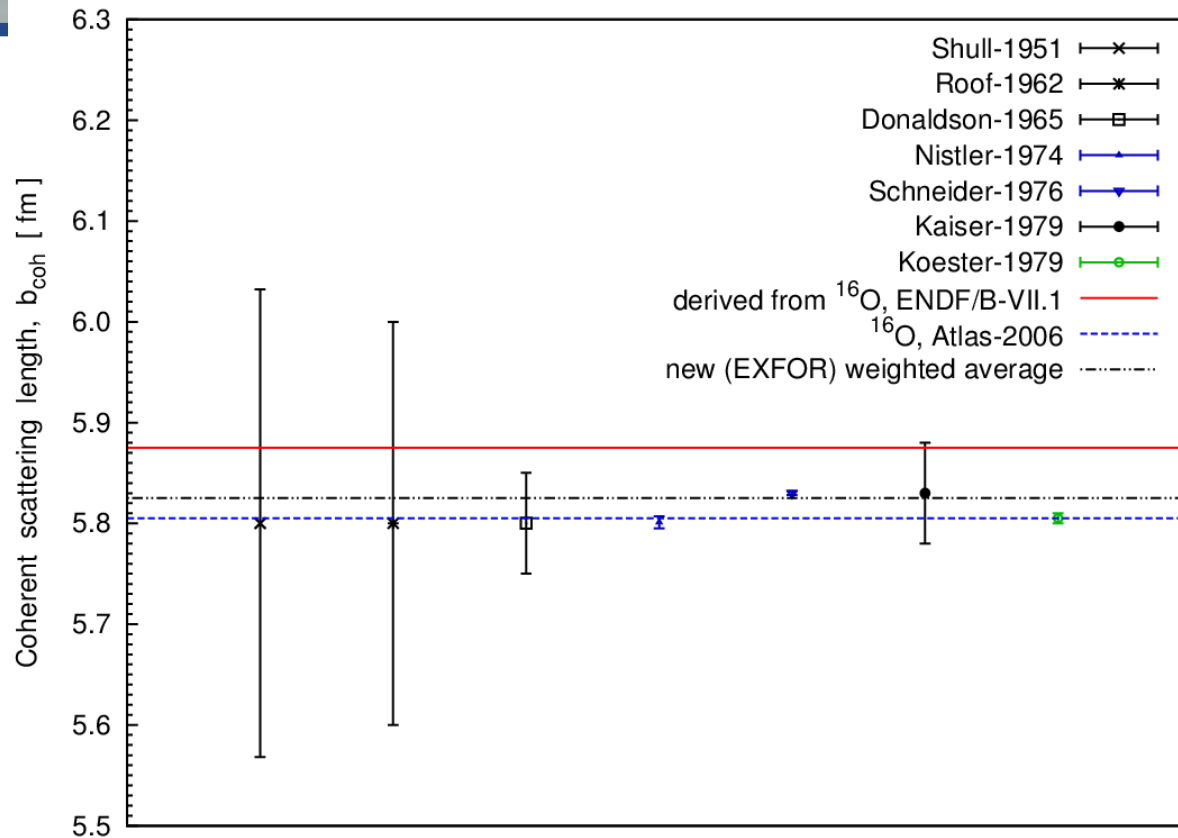
M. Ohkubo, "Neutron Total Cross Section Measurements on Oxygen, Aluminum and Carbon below 930 keV," Report **JAERI-M 86-193**, Japan Atomic Energy Research Institute (1987).

Measurements at low energy ($E < 0.3 - 0.4$ MeV)



- **Total cross-sections near a minimum at $E \approx 250$ keV ($E \sim 100 - 300$ keV):**
*NEW evaluation(s): we can estimate $\sigma_{\text{tot}}(E) \pm \Delta\sigma_{\text{tot}}(E)$ (or $\sigma_s(E) \pm \Delta\sigma_s(E)$), but can we compare it with **accurate** measurements ?*
*(e.g., we have **Block-1975**, $E = 23.5$ keV, $\sigma_{\text{tot}} = 3.736 \pm 0.007$ b ($\pm 0.19\%$), what else ?)*
 This could be a test for the accuracy of $R'(^{16}\text{O}) \sim 5$ fm (σ_{pot}) and **res. parameters**, E_j , Γ_n , Γ_γ that define σ_{tot} at low energies ~ 10 keV $< E < 300$ keV :
 local bound level(s), $E_0 \sim -3$ MeV (s-res., $\Gamma_n \sim |E_0|$) and $E_1 \approx 0.434$ MeV (p-res.)

Neutron Optics: b_{coh} [fm] of ^{16}O ($J = 0$)



- **New weighted average from EXFOR experimental data:**
 $b_{coh} = 5.824 \pm 0.002$ fm (A. Plompen & S. Kopecky)
- **Atlas-2006 estimate:** $b_{coh} = 5.805 \pm 0.005$ fm
- **Derived from ^{16}O , ENDF/B-VII.1:** $b_{coh} = 5.874 \pm 0.059$ fm

b_{coh} [fm] and $\sigma_{s, th} = \sigma_{coh}$ [barn] of ^{16}O

- **Atlas-2006** ($\sigma_{s, th} \leftrightarrow b_{coh}$ consistent):

$$\sigma_{s, th}(^{16}\text{O}) = 3.761 \pm 0.006 \text{ b } (\pm 0.16\%)$$

$$b_{coh}(^{16}\text{O}) = 5.805 \pm 0.005 \text{ fm } (\pm 0.09\%)$$

- **ENDF/B-VII.1 :**

$$\sigma_{s, th}(^{16}\text{O}) = 3.852 \pm 0.077 \text{ b } \rightarrow b_{coh}(^{16}\text{O}) = 5.874 \pm 0.059 \text{ fm}$$

- **JENDL-4.0:**

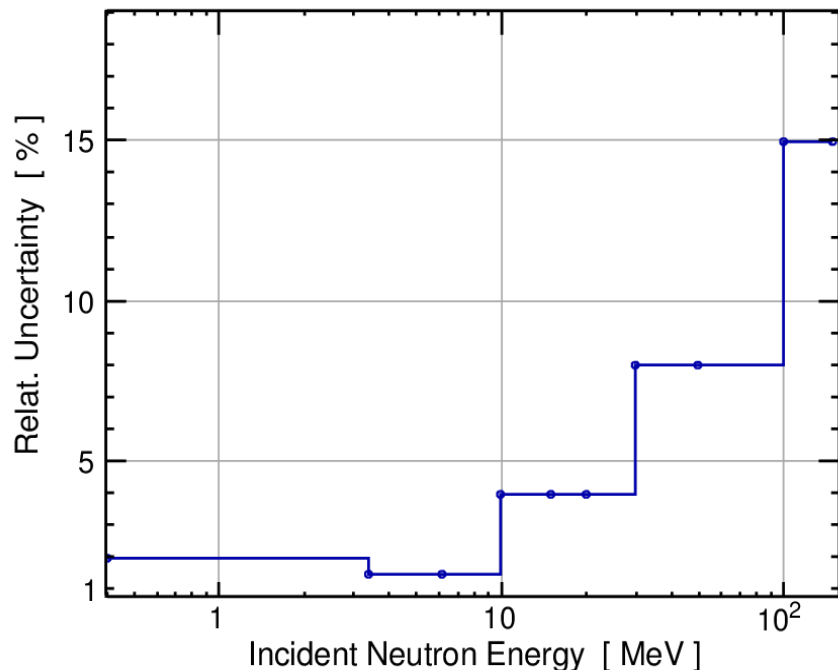
$$\sigma_{s, th}(^{16}\text{O}) = 3.841 \pm 0.038 \text{ b } \rightarrow b_{coh}(^{16}\text{O}) = 5.866 \pm 0.029 \text{ fm}$$

- **New (EXFOR-based) estimate:**

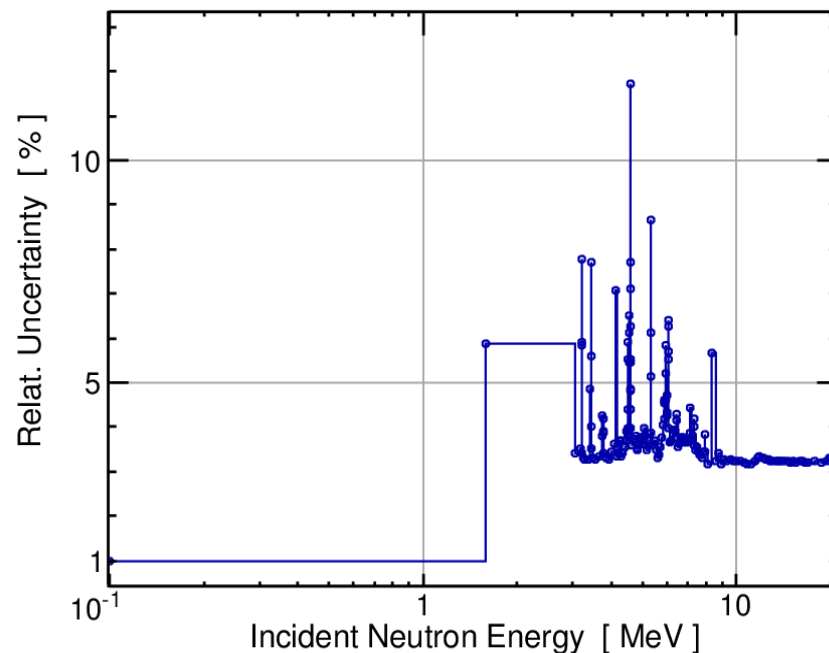
$$\sigma_{s, th}(^{16}\text{O}) = 3.786 \pm 0.003 \text{ b } \leftarrow b_{coh}(^{16}\text{O}) = 5.824 \pm 0.002 \text{ fm}$$

Uncertainty of $n + {}^{16}\text{O}$ at low neutron E

Cross Section Uncertainty
ENDF/B-VII.1: O-16(n,n)O-16

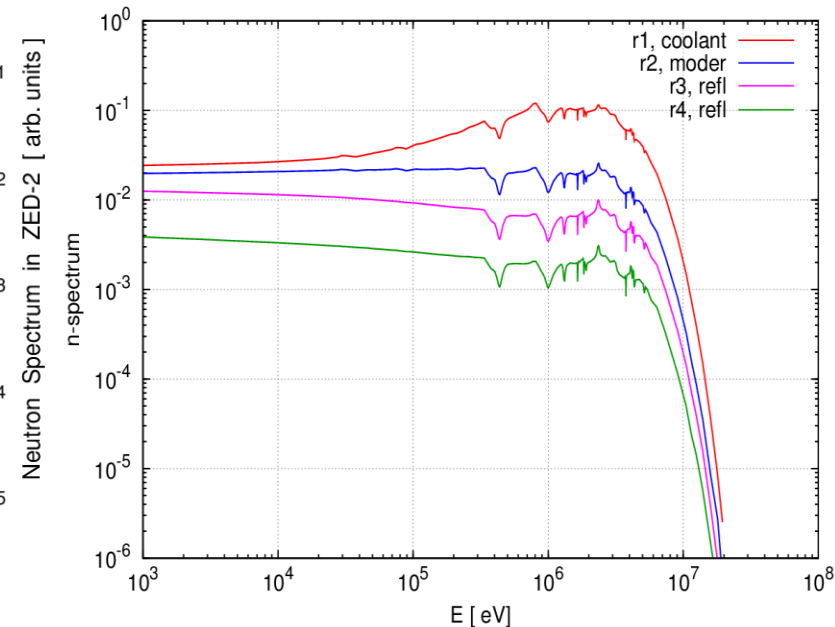
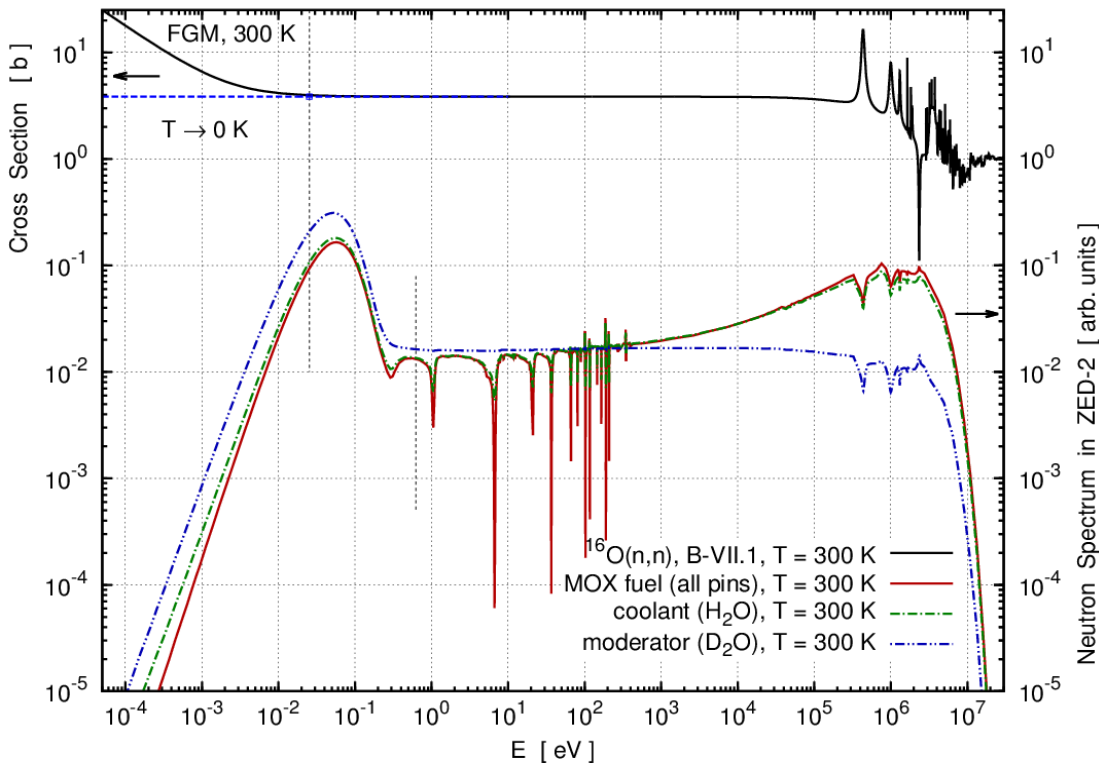


Cross Section Uncertainty
JENDL-4.0: O-16(n,tot)



- Relative uncertainty of $\sigma_{\text{tot}}(E)$ and $\sigma_s(E)$ calculated using ${}^{16}\text{O}$ covariance file (MF=33)
ENDF/B-VII.1: $\Delta\sigma_{\text{tot}}/\sigma_{\text{tot}} \approx \Delta\sigma_s/\sigma_s = \pm 2.0\%$ at $E < 3.4$ MeV.
 MF=33, MT=2, **cov_s(i, i')**: 10^{-5} eV $< E_1 < 0.4$ MeV, 0.4 MeV $< E_2 < 3.4$ MeV,
JENDL-4.0: $\Delta\sigma_{\text{tot}}/\sigma_{\text{tot}} \approx \Delta\sigma_s/\sigma_s = \pm 1.0\%$ at $E < 1.6$ MeV.
 MF=33, MT=1, **cov_{tot}(i, i')**: 10^{-5} eV $< E_1 < 0.1$ MeV, 0.1 MeV $< E_2 < 1.6$ MeV,

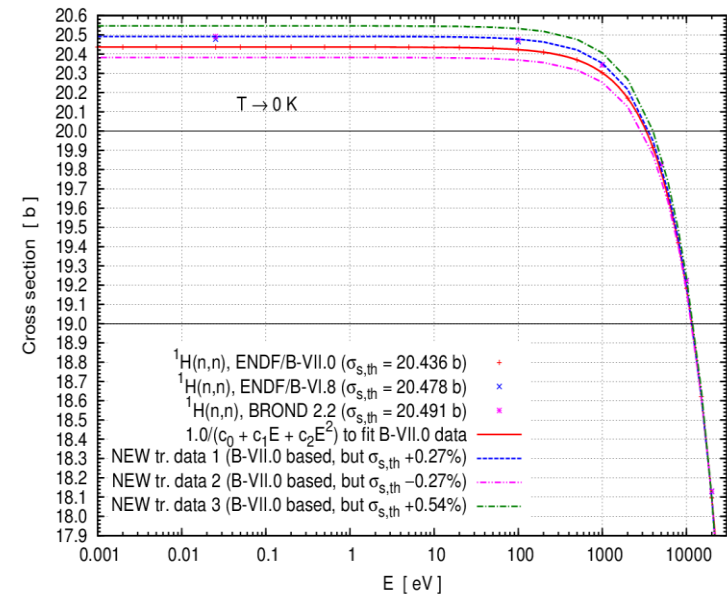
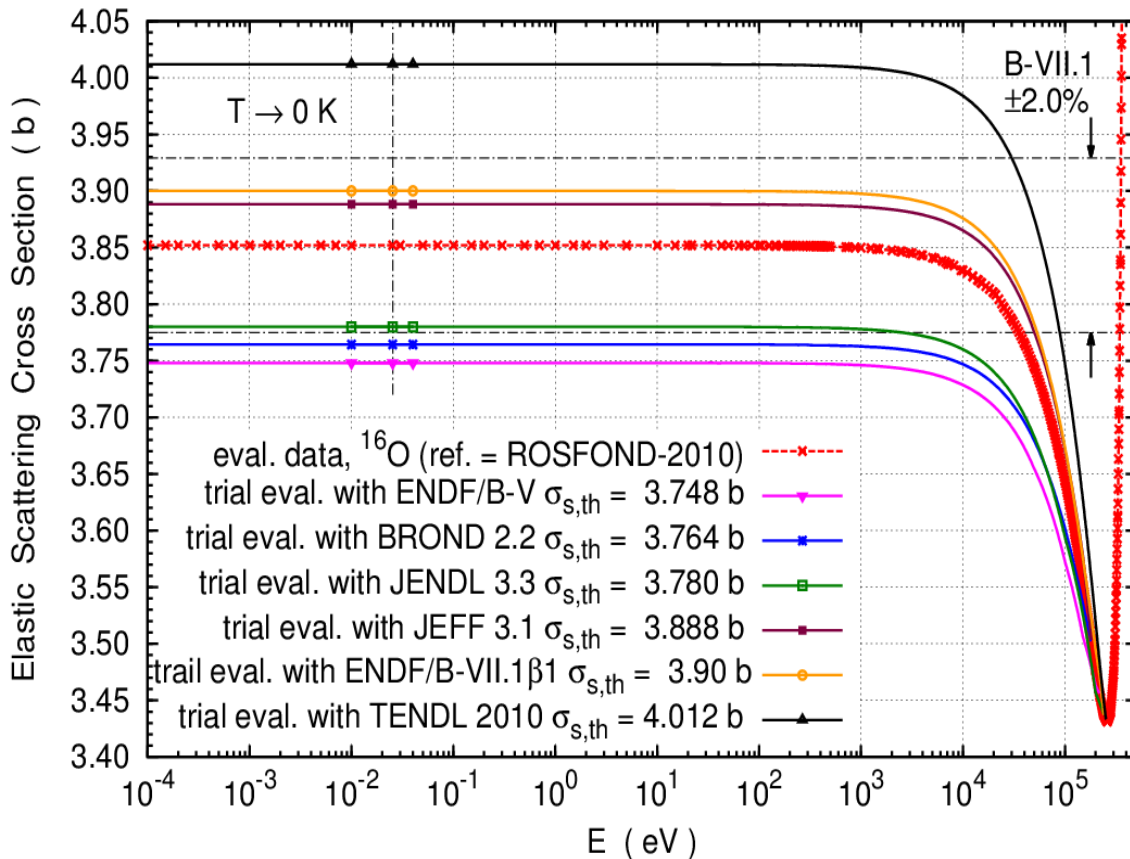
Questions to be discussed (n scattering)



- In new estimates of ^{16}O : $\sigma_{s, \text{th}} \pm \Delta\sigma_{s, \text{th}}$,
 what will it be ? (e.g., consistent with available **neutron optics data**, and
 σ_{tot} of **Dilg-1971** ($E = 130.0$ eV) & **Block-1975** ($E = 23.5$ keV) **OR** ...)
 Energy bin structure for MF33: not too coarse at **low neutron energies**, e.g.,
 a few bins at $E < 1.0$ MeV,
 $10^{-5} \text{ eV} < E_1 < 0.01 \text{ MeV}$, $0.01 \text{ MeV} < E_2 < 0.1 \text{ MeV}$, $0.1 \text{ MeV} < E_3 < 1.5 \text{ MeV}$...
 Then, **how accurately do we know $\sigma_s(E)$ and $\sigma_{\text{tot}}(E)$ at $E_1 < 0.01$ MeV: $\sim \pm 0.1\%$ **or** $\sim \pm 1\%$?**

Uncertainty propagation (thermal n scatt.)

Trial eval. for n scatt. cross sect. of ^{16}O ($\sigma_{s,\text{th}} = 3.852$ b is the ref. value)

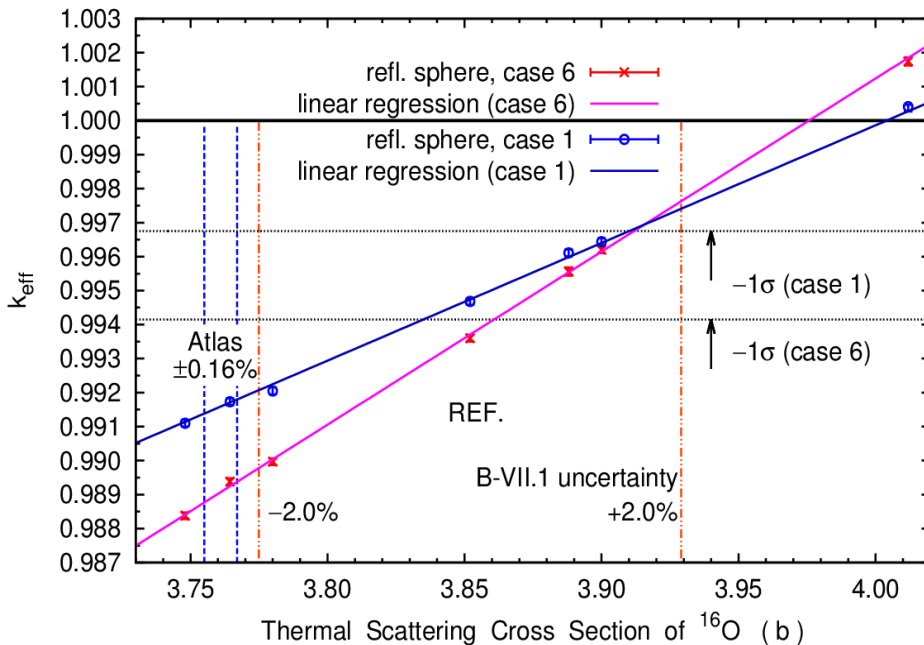


- We can answer the following question: for ^{16}O (as well as ^1H , ^2H) estimate the **uncertainty propagation** of $\sigma_{s,\text{th}} \pm \Delta\sigma_{s,\text{th}}$ (in MF3 and MF33 of an evaluation) to $k_{\text{eff}} \pm \Delta k_{\text{eff}}$ (of a critical benchmark) using **MCNP**, **NJOY**, and a linear regression:

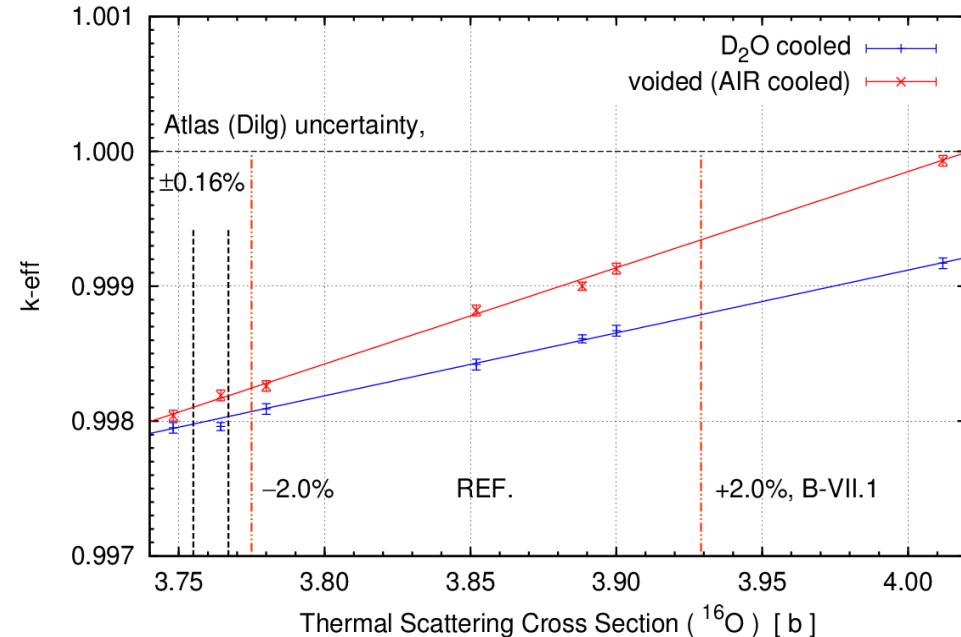
$$k_{\text{eff}}(\sigma_{s,\text{th}}) \approx b + a \times \sigma_{s,\text{th}}(^{16}\text{O}) + a' \times \sigma_{s,\text{th}}(^2\text{H}) + \dots$$

Using trial evaluations for $^{16}\text{O}(n,n)^{16}\text{O}$, we have

HEU-SOL-THERM-004, ref. ^2H and ^{16}O eval. based on ROSFOND-2010



28-el. NU ZED-2, T = 300 K, B-VII.0 lib. + ROSFOND ^{16}O (ref.)

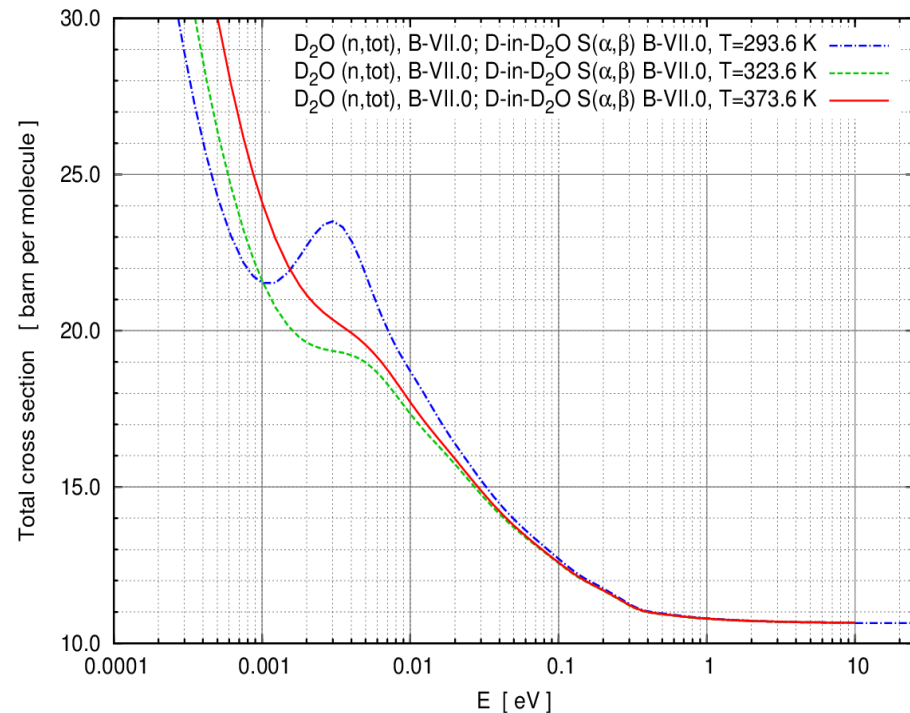
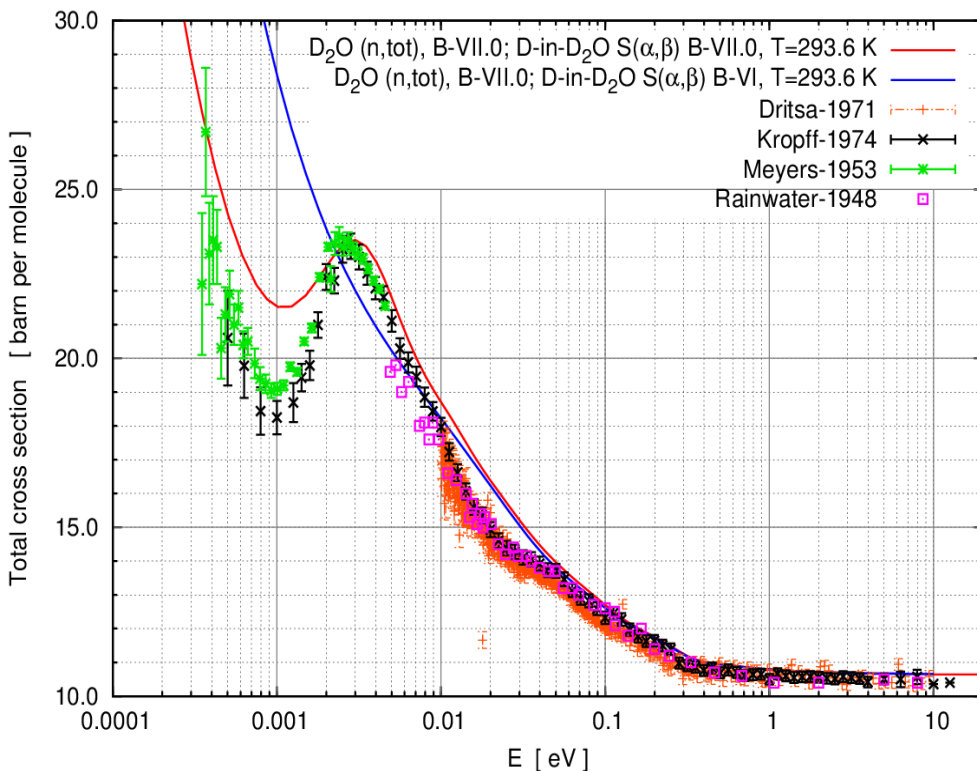


- $k_{\text{eff}}(\sigma_{s, \text{th}}) \approx b + a \times \sigma_{s, \text{th}}(^{16}\text{O})$, valid at $\Delta\sigma_{\text{sc}, \text{th}} \sim \pm 1\%$;
- $S_{s, \text{th}} \propto \partial k_{\text{eff}} / \partial \sigma_{s, \text{th}} = a$ (sensitivity coefficient).
We normalize it to be in **mk per %** (1 mk = 100 pcm)
- **Benchmark HST-04 (Case 6)**, $S_{s, \text{th}}(^{16}\text{O}) \approx 2.0$ mk per %, but $\Delta k_{\text{eff}} = \pm 5.85$ mk
- Typical **ZED-2** cores with NU fuel, $S_{s, \text{th}}(^{16}\text{O}) \approx 0.2$ mk per %, but $\Delta k_{\text{eff}} \approx \pm 3$ mk
compare with $S_{s, \text{th}}(^2\text{H}) \approx 1.2$ mk per %, $S_{s, \text{th}}(^1\text{H}) \approx 0.4 - 0.5$ mk per %.

References (^{16}O)

- A. Plompen, S. Kopecky, K. Kozier, D. Roubtsov,
“The status of low energy data for deuterium, oxygen and hydrogen,”
JEFF Document JEF/DOC-1488, Nuclear Energy Agency (NEA), Paris,
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- K. Kozier, D. Roubtsov, A. Plompen, S. Kopecky,
“Reactivity Impact of ^{16}O Thermal Elastic-Scattering Nuclear Data for Some Numerical and Critical Benchmark Systems,”
Nuclear Technology, Vol. 183, pp. 473-483, 2013 (September).
- K. Kozier, D. Roubtsov, J. Chow, A. Plompen, S. Kopecky, J. Svenne, and L. Canton,
“Reactivity Impact of ^2H and ^{16}O Elastic Scattering Nuclear Data on Critical Systems with Heavy Water,”
in Proceedings of ND-2013, Nuclear Data Sheets.

TSL: D₂O, and D₂O vs. H₂O



- $\sigma_{\text{tot}}(E)$ in barn per molecule for D₂O (²H₂¹⁶O) in heavy water at **RT** and (T **up** & **down**)
- Near $E_{\text{th}} = 0.0253$ eV, we have at **RT**
(Exp. – Calc.) / Calc. $\approx -8.4\%$ (using B-VII.0 S(α,β) for D-in-D₂O): ?

TSL: H₂O and D₂O

With **J.I. Márquez Dámian, J.R. Granada, *et al.***
(Centro Atómico Bariloche, Argentina),
the goal is

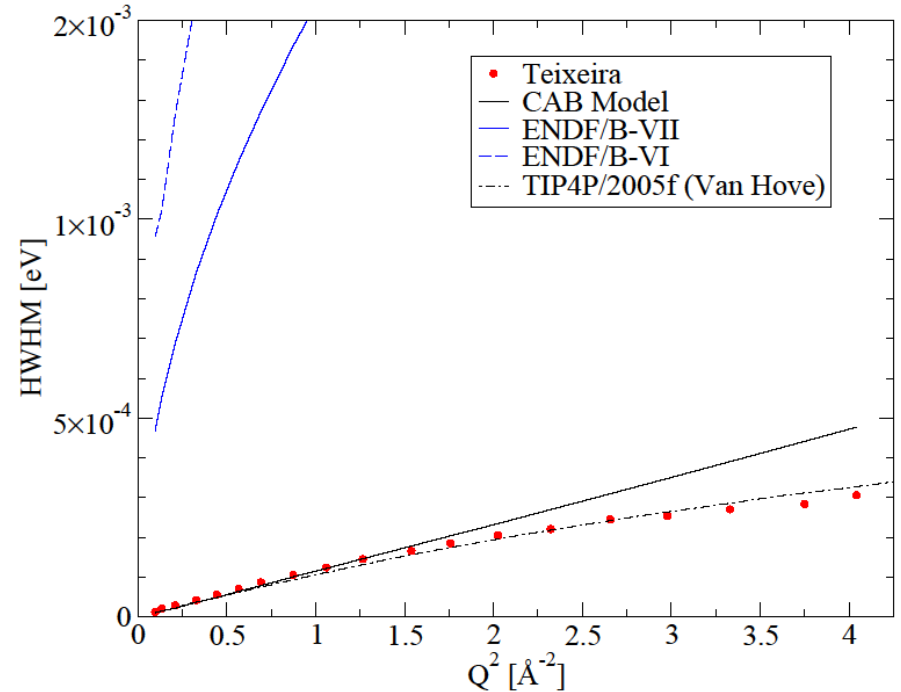
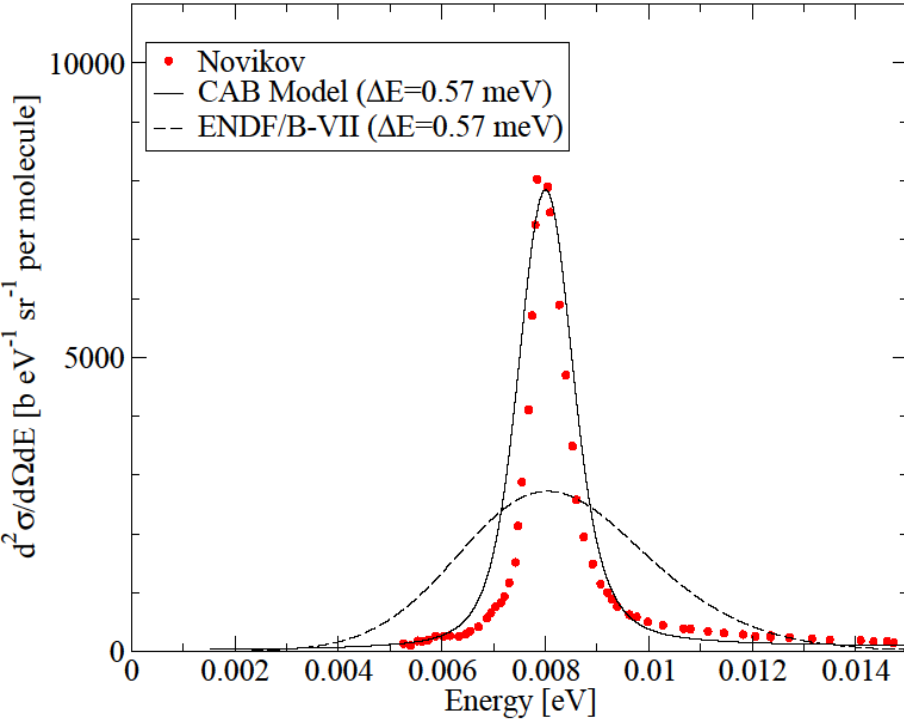
**A NEW EVALUATION OF
THERMAL SCATTERING LAW
FOR LIGHT AND HEAVY WATER
IN ENDF-6 FORMAT,
BASED ON EXPERIMENTAL DATA
AND MOLECULAR DYNAMICS**

**WITH MODERN SIMULATIONS OF WATER DYNAMIC AND STRUCTURE
we will have ¹⁶O (*new*), any (reasonable) *T* available,
*etc.***

$S(\alpha, \beta)$ for water: collaboration with Bariloche

- The Neutron Physics Department at *Centro Atómico Bariloche* in Argentina is working on an update of the thermal scattering libraries for light and heavy water. There are two researchers involved (J.R. Granada and J. Dawidowski), one former post-doc (A.D. Viñales), and one PhD student (J.I. Márquez Damián).
- Their approach is based on combining **molecular dynamics** simulations and experimental data, and the resulting models are implemented in **LEAPR** / NJOY.
- The **key points** for these models are:
 1. use of molecular diffusion for translational motion (instead of free gas approx.),
 2. continuous spectra computed from molecular dynamics simulation at a given thermodynamic state (instead of derived from neutron scattering experiments),
 3. Models for D and O in D₂O, with a more precise description of **the structure** (instead of the incoherent approximation used in ENDF/B-VI or the Lennard-Jones model for D-D structure used in ENDF/B-VII).
- The resulting cross sections are an improvement over existing evaluations: **they are compared with measurements** of double differential scattering cross sections, quasi-elastic neutron scattering measurements, angular distributions, average cosine of the scattering angle and total cross sections.

Results: light water TSL (1)

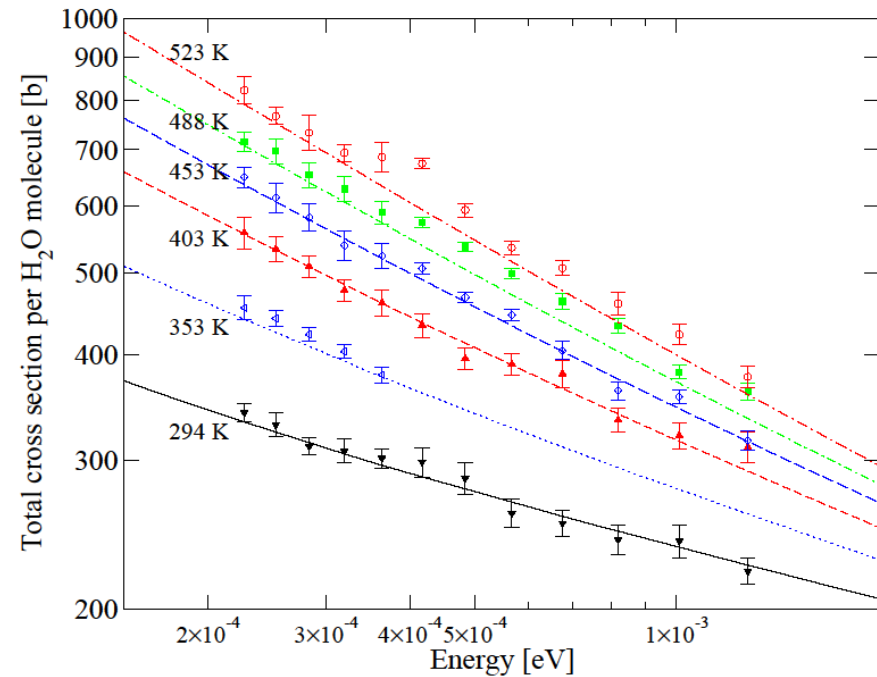
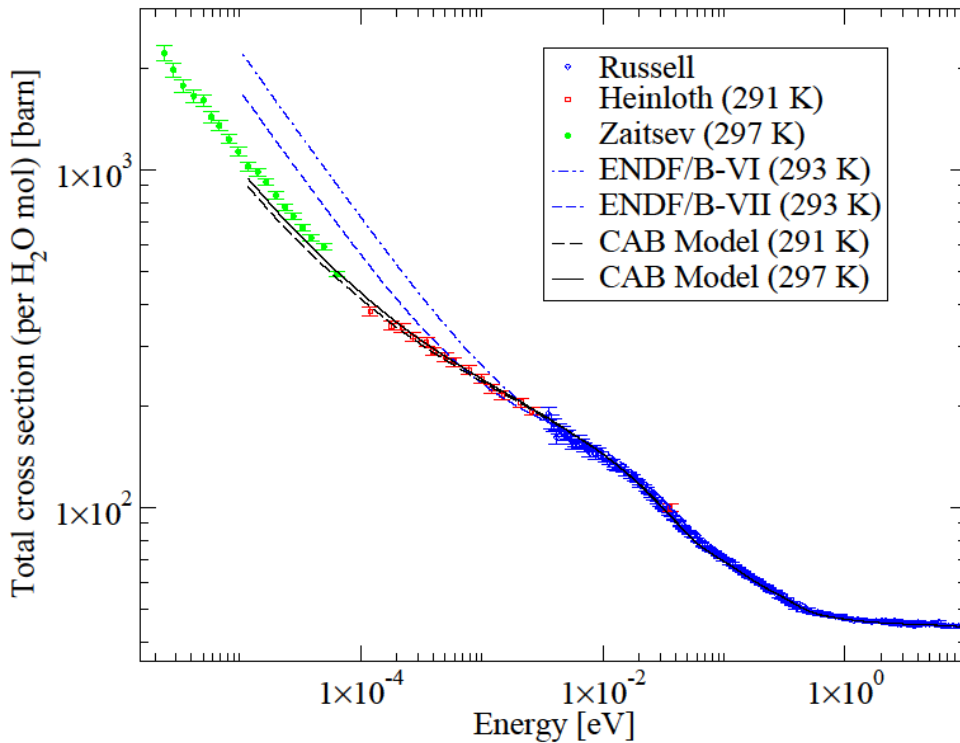


Double differential
scattering cross section
for light water,
 $E_0 = 8$ meV, $\theta = 37^\circ$.

Half-width of the quasi-elastic
peak for $E_0 = 3.15$ meV neutrons
in H₂O.

J.I. Márquez Damián *et al.*

Results: light water TSL (2)



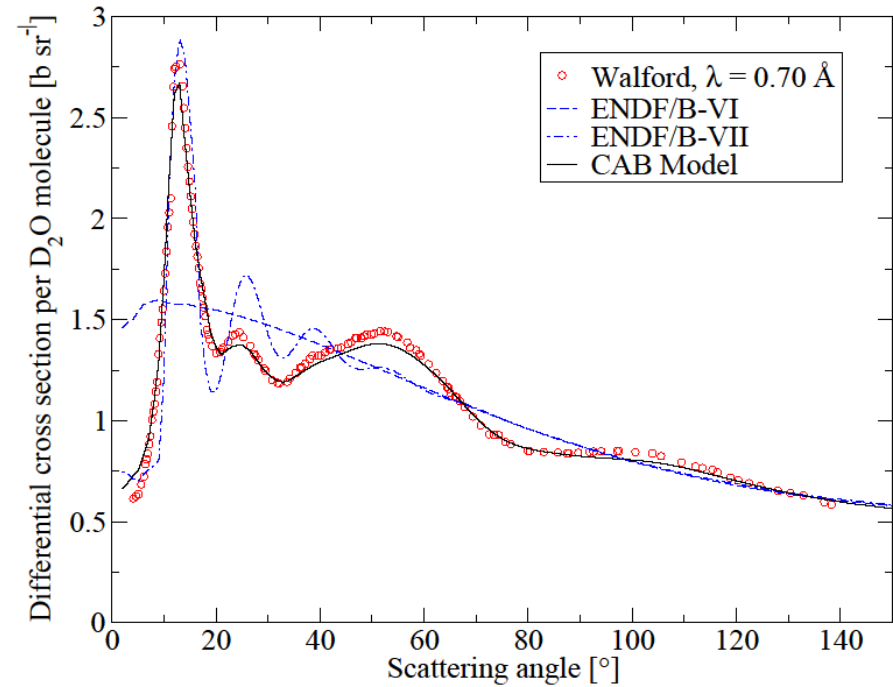
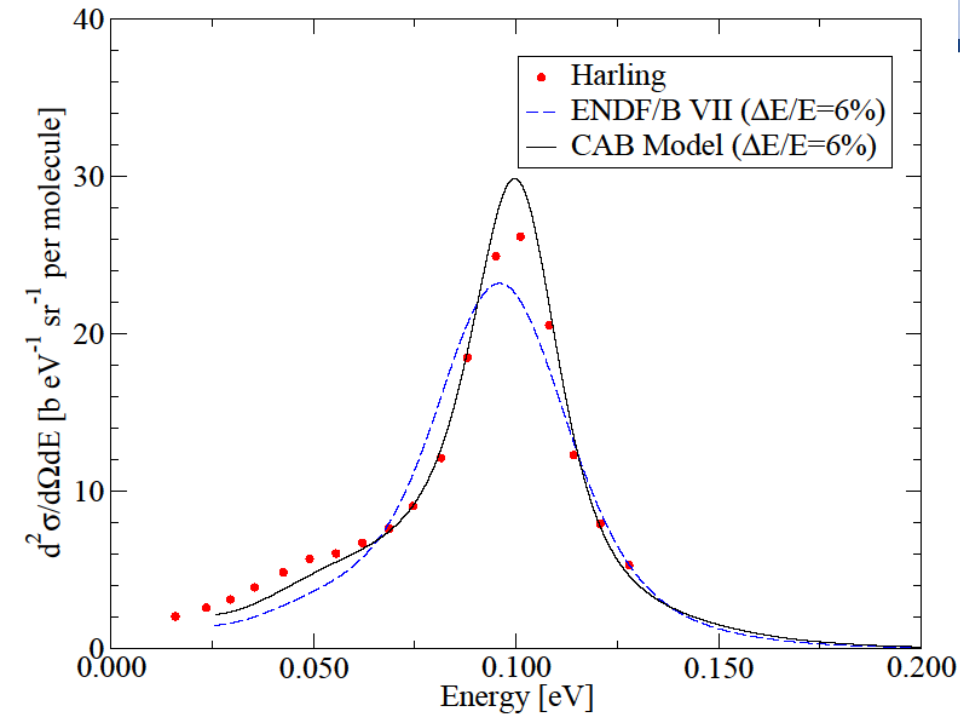
Total cross section
per H_2O molecule (RT).

Temperature dependence
of the total neutron cross section
for H_2O .

J.I. Márquez Damián *et al.*

UNRESTRICTED / ILLIMITÉ

Results: heavy water TSL (1)

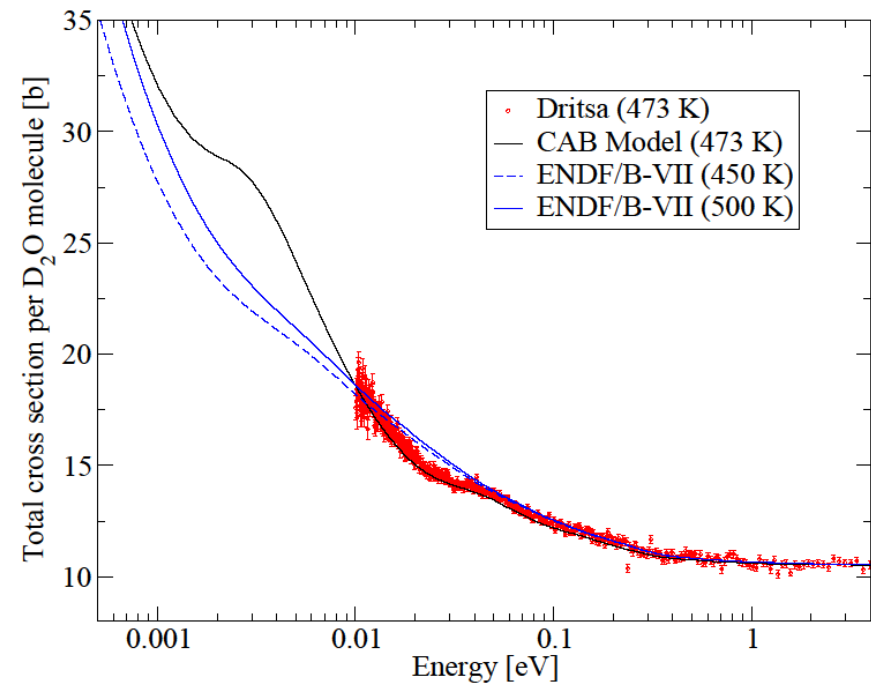
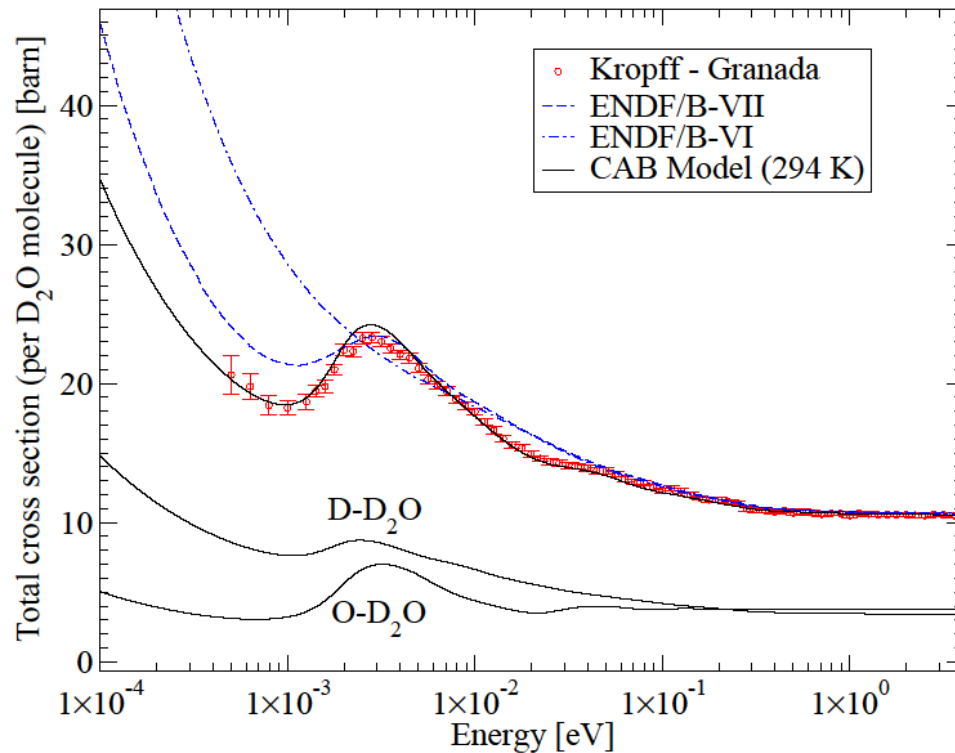


Double differential
scattering cross section
for heavy water,
 $E_0 = 101$ meV, $\theta = 60^\circ$.

Angular distribution for
 $E_0 = 170$ meV neutrons in D₂O.

J.I. Márquez Damián *et al.*

Results: heavy water (2)



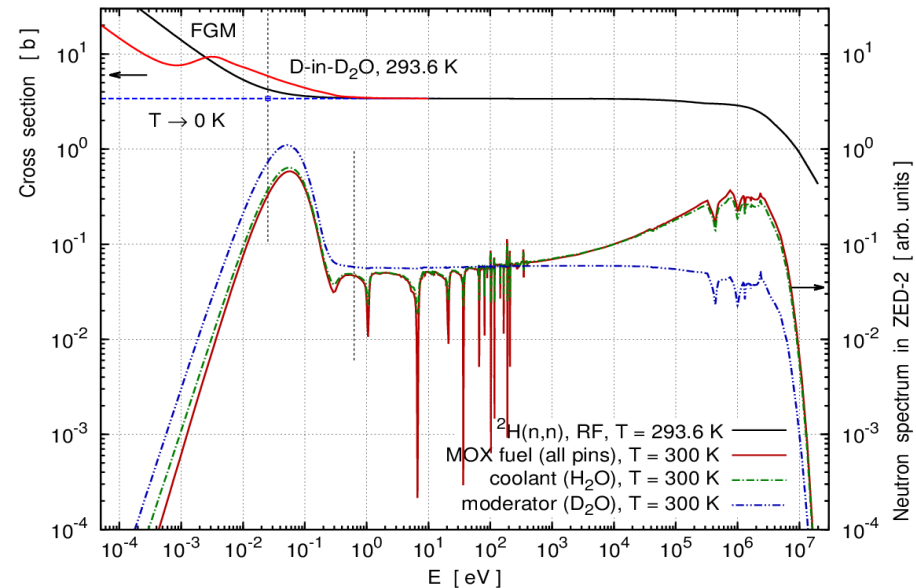
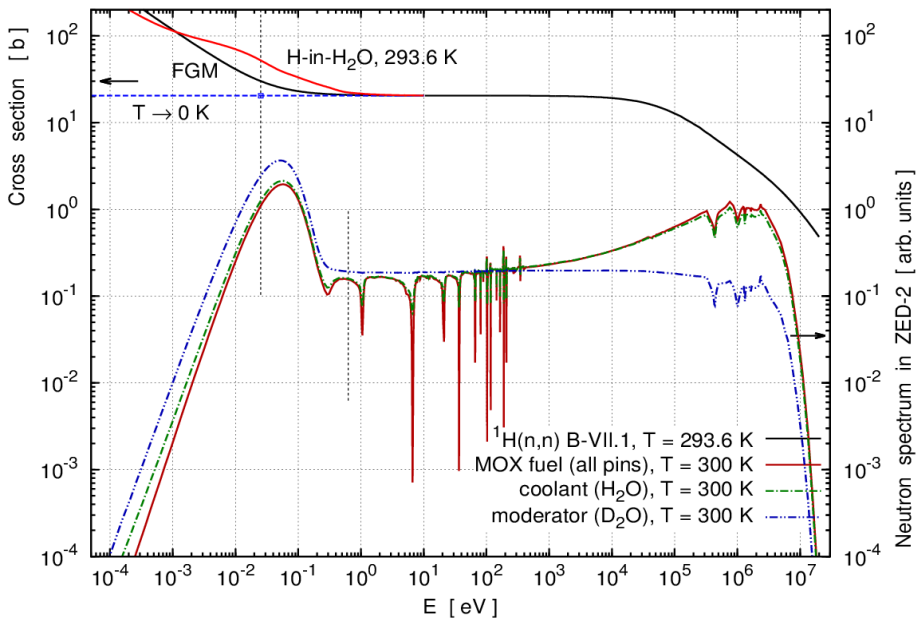
Total cross section
per D_2O molecule (at RT).

Total cross section
per D_2O molecule at $T = 473$ K.

J.I. Márquez Damián *et al.*

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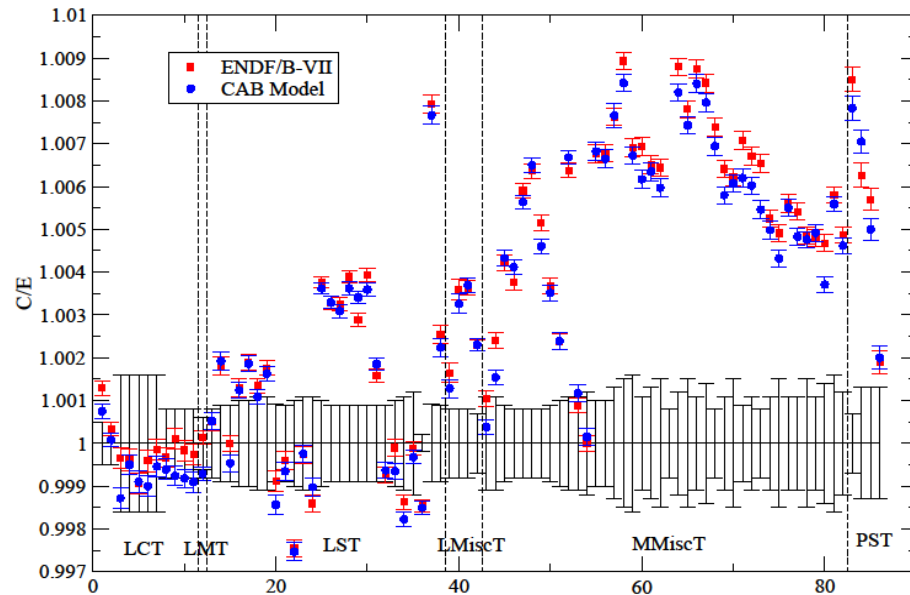
Testing New TSL (thermal ace + MCNP5)



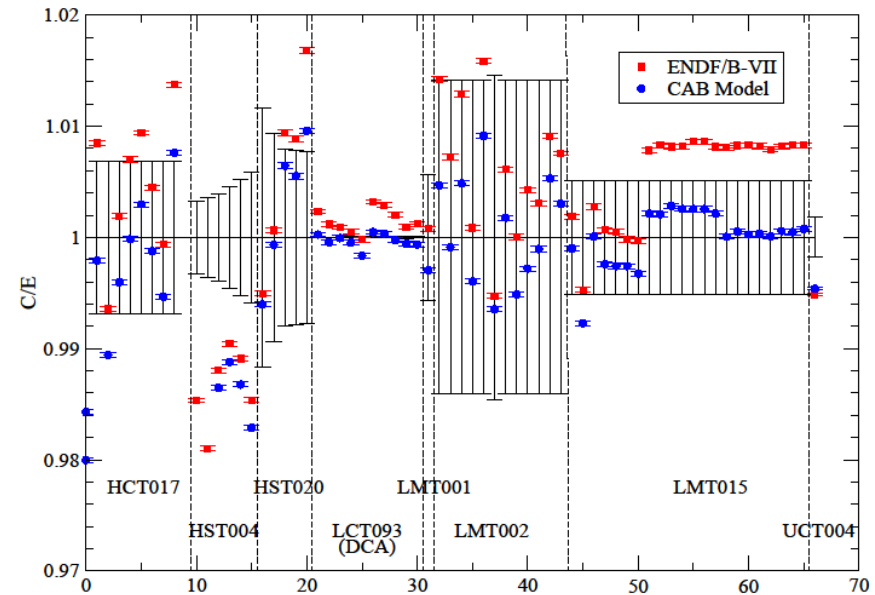
We create new thermal ace files (at room T) with NJOY99 and use MCNP5 for critical benchmarks with H₂O and D₂O ($k_{\text{eff}} \pm \Delta k_{\text{eff}}$)

Results: ICSBEP criticality benchmarks (C/E ratio)

Light water moderated critical experiments



Heavy water moderated critical experiments



ENDF/B-VII + ENDF/B-VII TSL vs.
ENDF/B-VII + CAB Model (H₂O)

- Impact is less than 100 pcm.
- No clear improvement over ENDF/B-VII TSL.
- Existing discrepancies caused by nuclear data not addressed.

ENDF/B-VII + ENDF/B-VII TSL vs.
ENDF/B-VII + CAB Model (D₂O)

- Differences up to 1000 pcm.
- 66% of benchmarks cases have a C/E ratio closer to 1.0 using the [new evaluation](#).
- 82% when the [new evaluation](#) and ²H (fast ace) from ROSFOND-2010 is used.

Summary for new evaluations of TSL (water)

- The **CAB Models for water** are a set of new models for thermal neutron scattering in light and heavy water, generated from molecular dynamics calculations and experimental data.
- The models result on a improvement over existing models for both light and heavy water for the calculation of differential and integral scattering quantities.
- The impact of the improvements in light water is not significant for criticality applications (main differences are in low energy, small angle interactions), but updating the library might be important for other users.
- In the case of heavy water, the inclusion of **O-in-D₂O** and a better representation of the structure improves the calculation of critical systems significantly.

- **REFERENCES**

J.I. Márquez Damián, J.R. Granada, D.C. Malaspina, Ann. of Nucl. En. (accepted), **65**, (2014).

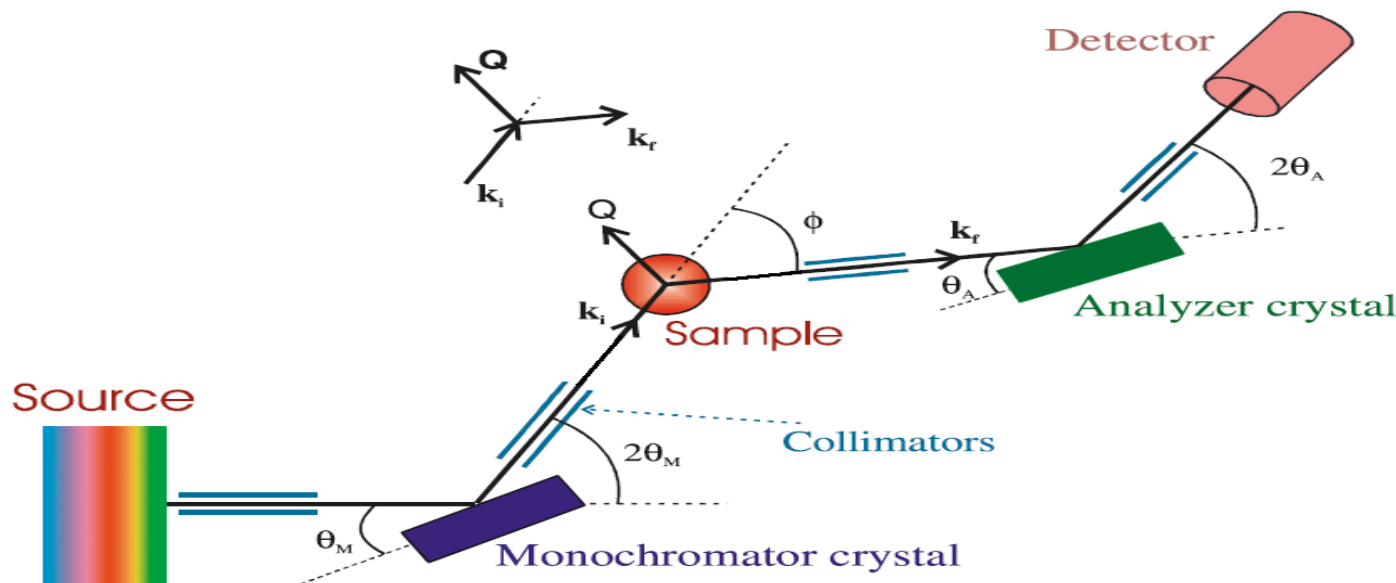
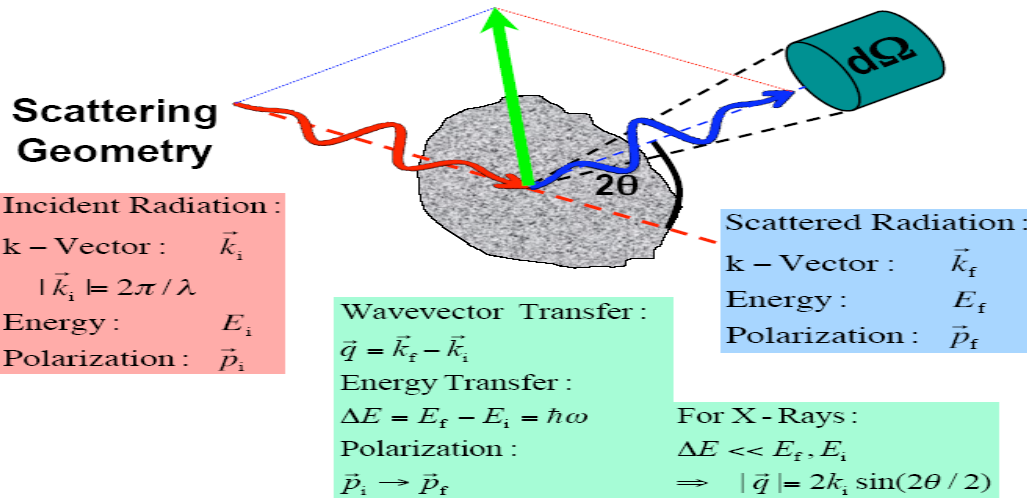
J.I. Márquez Damián, D.C. Malaspina, J.R. Granada, J. Chem. Phys., **139**, p. 024504 (2013).

A.D. Viñales, J. Dawidowski, J.I. Márquez Damián, Ann. of Nucl. En., **38**, p. 1687 (2011).

J.I. Márquez Damián, J.R. Granada, D.C. Malaspina, in Proceedings of **ND-2013**

AECL EACL

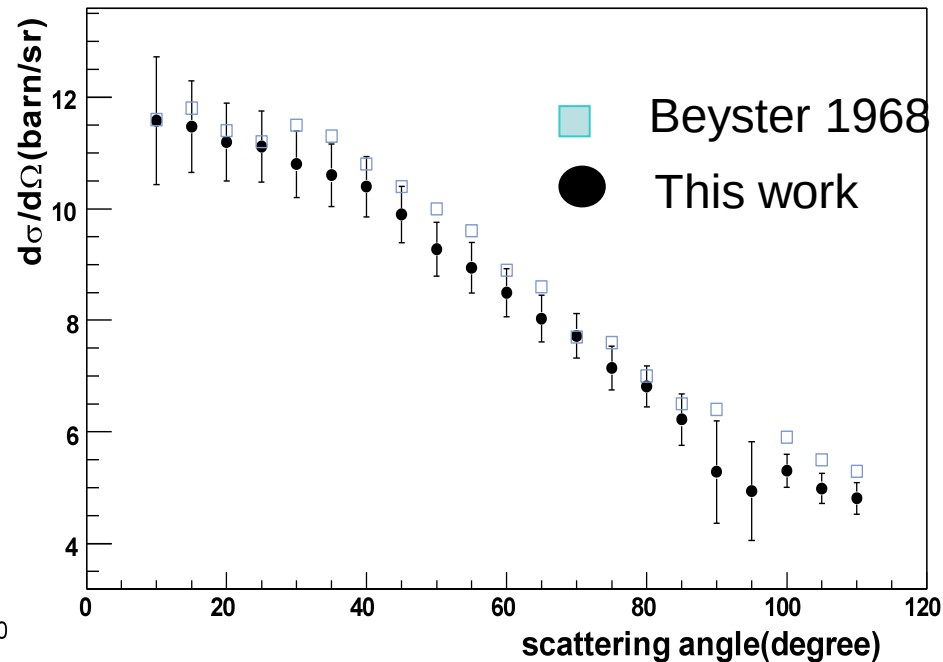
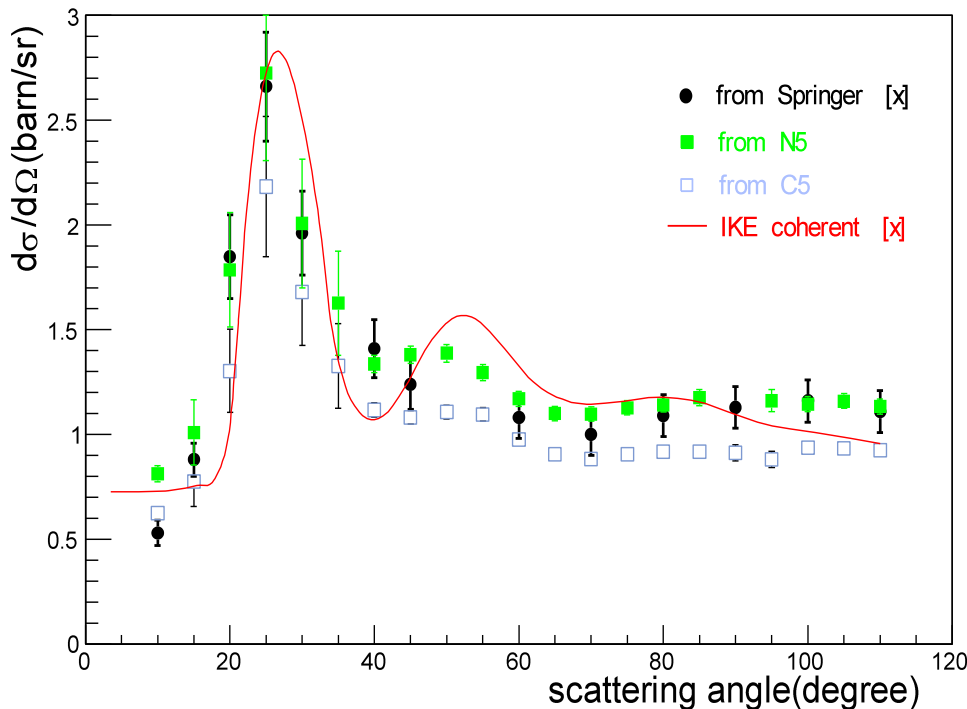
Neutron Scattering on Water using triple axis spectrometer at NRU reactor at CRL, AECL



Sample sizes:
0.1 mm to 3 mm,
at **RT**

**Triple axis
spectrometer**

G. Bentoumi, G. Li, B. Sur, and Z. Tun, (AECL and Canadian Neutron Beam Centre)



Differential scattering cross section of D_2O .
Beam energy is 44 meV
(except for that the result from C5: it is at
 $E_0 = 41.44$ meV).

Absolute differential cross
section (in barn/sr)
for **Light water**,
at $E_0 = 41$ meV,
Beyster's data: $\pm 5\%$.

