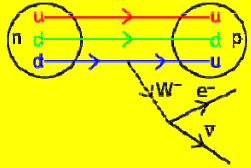


I.N.Borzov \*

## Beta-decay data from microscopic models

Joint Institute of Heavy Ion Research, ORNL



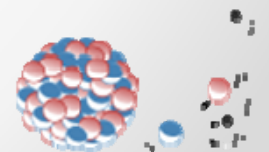
### Self-consistent approach to nuclear beta-decay based on DFT

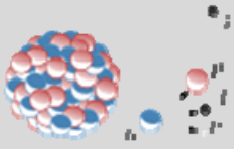
- UNEDF PROGRAM: [www.unedf.org](http://www.unedf.org)  
A quest for universal nuclear density functional.

#### Aim

- describe existing beta-decay data with well quantified uncertainties;
- provide reliable extrapolation to unknowns,
- large-scale calculations of beta-decay data for applications.

\*) NDC IPPE, Obninsk and BLTP JINR, Dubna





# Applications:

## **RIB experiments**

*T1/2 and Pn-s predictions for recent RIB experiments in ORNL, GSI, IPN.  
Nuclear structure models are guided by RIB experiments on short-lived nuclei.  
(New data vs. existing global approaches: DFT, FRDM+RPA, Gr. theory.)*

## **Beta-decay data for astrophysics**

*(Collaborations with ULB and GSI).  
Beta-strength functions  $\rightarrow$ TALYS  $\rightarrow$ T1/2, Pn, bn-spectra  $\rightarrow$ R-process abundances.*

## **Reactor applications**

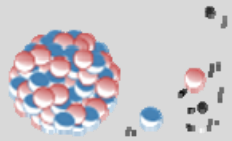
*NDC IPPE, Obninsk*

*Theoretical nuclear data:  $Q_b$ ,  $S_n$ , T1/2, Pn .*

*Table for fission products and r-process nuclei (I. Spherical nuclei).*

*Re-evaluation of  $v_D$  for actinides.*

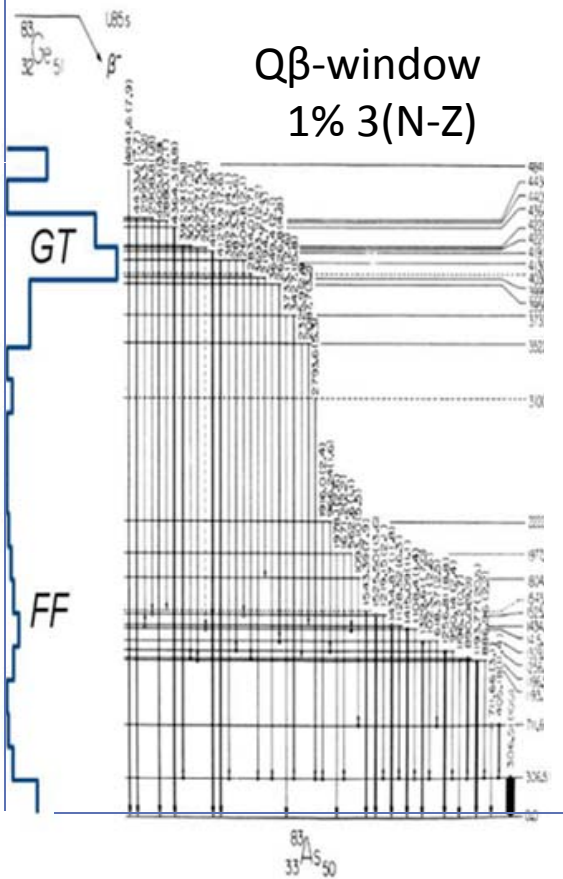




# Beta decay of very neutron-rich nuclei



GT Resonance  
99%  $3(N-Z)$



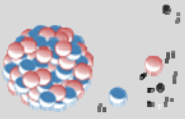
## Beta-decay rates for the r-process

The most unreliable data-base.  
Experimental data are incomplete.  
Theoretical predictions are complicated .

- 1-2% of the GT sum rule within the  $Q\beta$ -window .  
Energy distribution of this tiny strength defines the total half-life;
- sensitivity to nuclear g.s. properties: high;
- sensitivity to effective NN-interaction: high;  
(repulsion vs. attraction; finite-range vs. contact)
- competition from the FF decays: complicates theoretical analysis;
- Temperature dependence: rather low ( Kajino et al. , 2009). 😊

Different approaches give deviating extrapolations far from stability.

Comparing them one has to clearly realize the main assumptions and restrictions of the models.



# Gamow-Teller (GT) vs. first-forbidden (ff). New effects predicted near the closed shells

The ff decays are suppressed cf. GT  
 $M_{ff}^2 \sim (1/qR \times L) M_{GT}^2$   
 (if the same phase-space is assumed).

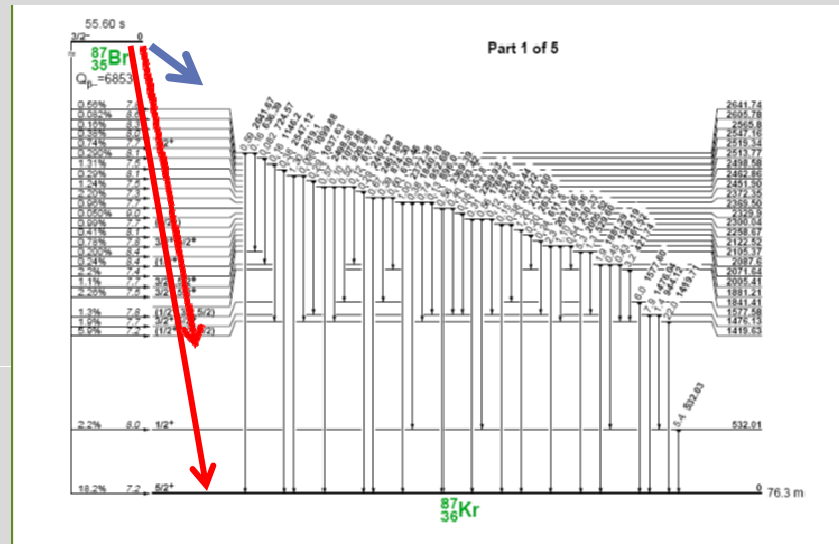
\* \* \*

Below and above  
 the shell closures  $N_{mag}=50,82$ :

a)  $N < N_{mag}$        $Q_{ff} \leq Q_{GT}$

b)  $N > N_{mag}$        $Q_{ff} \gg Q_{GT}$

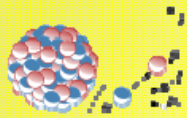
The impact of high-energy ff-decays  
 on  $S_{JLS}(Q)$ ,  $T_{1/2}$ ,  $P_n$ -s  
 depends on detail of the shell-sequence



$N > 50$  High-energy FF decay and low-energy GT

## SHELL EFFECTS FAR FROM STABILITY:

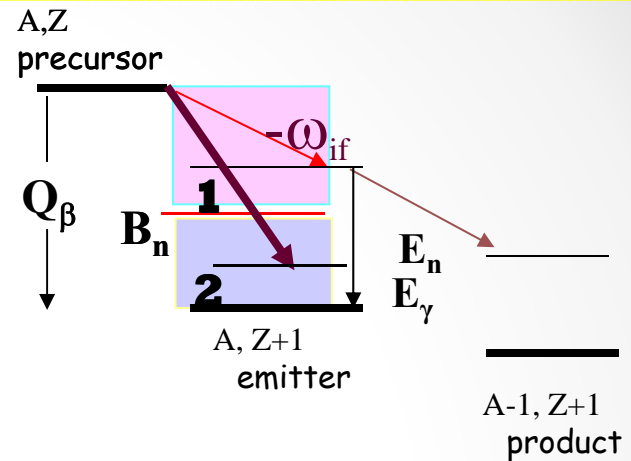
- *Crossing the major  $N=50,82,126$  shells .  
 High-energy ff transitions reduce the half lives and  $P_n$ -branchings.*
- *Near  $Z \sim 28, N \sim 50$ .  
 Sensitivity of the beta-decay rates to the  $J/\pi$  of the g.s.  
 Stabilization of the half-lives near new emerging subshell at  $N=58$ .*



# Half-life, P<sub>n</sub>-value

Key ingredient is the **beta-strength function**  $S_{JLS}(\omega)$ :  
spectral distribution of beta-decay matrix elements.  
Its resonance character reflects non-statistical nature  
of beta-decay.

(See e.g. I.N. Izosimov, PEPAN 30(2),131,1999.)



$$T_{1/2} = \frac{D}{\left(\frac{G_A}{G_V}\right)^2 \int_0^{Q\beta} S_L(\omega) f_0(Z, \omega) d\omega}$$

$S_L(\omega)$  –  $\beta$  – strength function

$$D = 2\pi^3 \ln 2 / G_V^2 m_e^5 = 6163s$$

$$G_A / G_V = 1.26$$

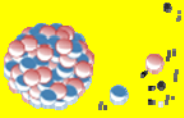
$$f_0(Z, A, \omega) = \int_0^\omega F(Z, A, \omega) pW (\omega - W)^2 dW$$

$f_0(Z, \omega) \sim \omega^5$  – amplifies the  
high – energy tail of  $S_\beta(\omega)$ !

$$P_n = \frac{\int_0^{Q\beta} S_L(\omega) f_0(Z, \omega) P_{if}(j_{if}, E_n) d\omega}{B_n(Z+1) \int_0^{Q\beta} S_L(\omega) f_0(Z, \omega) d\omega}$$

$$P_{if} = \Gamma_n / (\Gamma_n + \Gamma_\gamma),$$

$$\Gamma_\gamma \ll \Gamma_n \Rightarrow P_{if} \approx 1$$



# Beta-strength function

## Finite Fermi system theory (FFST):

Beta-decay strength function can be defined through polarization operator of 2-component superfluid Fermi system

Migdal, A.B., *Theory of Finite Fermi Systems*,  
Moscow: Nauka, 1983, 2nd ed. (in Russian)

$$-i\chi = \text{---} \left( \text{---} \right)_{\tau} \text{---} + \text{---} \left( \text{---} \right)_{\tau^h} \text{---} + \text{---} \left( \text{---} \right)_{\tau^{(1)}} \text{---} + \text{---} \left( \text{---} \right)_{\tau^{(2)}} \text{---} \dots$$

To find the strength function  
in nuclei with pairing one has to

1. constrain the ground state:

self-consistent HFB based on DFT  
(to find  $Q_b$  and single-quasiparticle basis).

2. solve the QRPA-like eqns.:

FFST eqns.  
(to find effective fields  $\sim \tau_i$ ).

An approach is equivalent to HFB + pnQRPA

# Ground State properties : DFT

An upper limit of exact  $E_{total}$ :

$$E[\rho, \nu] = \text{Tr} \left( \frac{p^2}{2M} \rho \right) + E_{\text{int}}[\rho, \nu]$$

Kohn – Sham quasiparticle local EDF,  $M^* = 1$

$$E_{\text{int}} = \sum_{\text{main, Coul, sl}} \varepsilon_n[\rho] + \frac{1}{2} \nu^* F^\xi[\rho] \nu$$

$F^\xi$  – volume + surface

$$H = \begin{pmatrix} h - \mu & -\Delta \\ -\Delta & \mu - h \end{pmatrix}$$

$$h = \frac{p^2}{2m} + \frac{\delta E}{\delta \rho} \sim \rho$$

$$\Delta = \frac{\delta E_{\text{int}}}{\delta \nu}$$

HFB – like iterative procedure

$$\rho_0, \nu_0 \Rightarrow h_0, \Delta_0 \Rightarrow \rho_1, \nu_1 \Rightarrow h_1, \Delta_1$$

## DF3 functional by S.A. Fayans et al.

S.A. Fayans, S.V. Tolokonnikov, E. Trykov, D. Zawischa, Nucl. Phys. A676 (2000) 49.  
I.N. Borzov, S.A. Fayans, E. Kromer, D. Zawischa Z. Phys. A335(1996) 117

Fitted to the masses and (as  $M^*=1$ ) it was specially fitted to s.p energies of very neutron-rich doubly-magic  $^{132}\text{Sn}$

**NEW:**

DF3a with better spin-orbit splitting; blocking the odd- $p$  in  $Z$  and  $Z+1$  isobars



# Excited states: CQRPA based on the self-consistent g.s

$$F_{\tau\tau}^{\omega} = \frac{\delta^2 E}{\delta\rho^{\tau} \delta\rho^{\tau}} \quad F_{\tau\tau}^{\xi} = \frac{\delta^2 E}{\delta\nu^{\tau} \delta\nu^{\tau}}$$

An impact of spin-dependent terms on nuclear masses is of order of 100KeV.  
(J. Margueron et al. J.Phys.G 36(2009) 125103)

## **Approximation:**

The spin-isospin (time odd) parts of the effective NN-interaction are defined independently of the scalar (time-even) parts.

## **DF+CQRPA**

- Universal (the same for all A) effective NN-interaction
- Non-truncated (ph,pp,hh) QRPA matrix.  
(full ph basis Continuum QRPA)
- Gamow-Teller and first-forbidden decays



# Spin-isospin NN-interaction

$$ph: F_{\sigma\tau}^{\omega} = 4N_0^{-1} \left[ g'_0 \vec{\sigma}_1 \cdot \vec{\sigma}_2 + g_{\pi} e_{q\pi}^2 \frac{(\vec{\sigma}_1 \cdot \vec{k})(\vec{\sigma}_2 \cdot \vec{k})}{k^2 + m_{\pi}^2 + P_{\Delta}(k^2)} + g_{\rho} e_{q\rho}^2 \frac{[\vec{\sigma}_1 \vec{k}][\vec{\sigma}_2 \vec{k}]}{k^2 + m_{\rho}^2} \right] \tau_1 \cdot \tau_2 .$$

$$2N_0^{-1} = C_0 = 300 \text{MeV fm}^3, \text{ with } C_0 = 2\varepsilon_F/3\rho_0, \text{ and } \rho_0 = 0.0859 \text{ fm}^{-3}$$

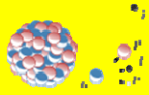
$g' > 0$  is fixed from GTR position (shifts GT strength to higher Ex , as  $g'_{\pi,\rho} < 0$  shift it downward) 

Here,  $g_{\pi} = -2\pi/N_0 (f_{\pi}^2/m_{\pi}^2)$ ,  $g_{\rho} = -2\pi/N_0 (f_{\rho}^2/m_{\rho}^2)$ , where  $m_{\pi}(m_{\rho})$  and  $f_{\pi}(f_{\rho})$  are the bare pion ( $\rho$ -meson) mass and the  $\pi NN(\rho NN)$  coupling constants, respectively. The pion irreducible polarization operator in the nuclear medium  $P_{\Delta}(k^2)$  takes care of the virtual  $\Delta$  isobar-nucleon hole excitations. The contact part of the effective spin-isospin interaction Eq. (14) is governed by the Landau-Migdal constant  $g'_0$ . The operator  $e_{q\pi}^2 = Q = e_q[\sigma\tau]^2$  is assumed to describe the quenching of the pion-nucleon vertex [18]. The operator  $e_{q\rho}^2$  is defined from the condition that the  $\rho NN$  coupling

$$pp: F\sigma\tau^{\xi}(\mathbf{r}_{ij}) = -4N_0^{-1}(g'_{\xi} + h^{\xi}x^q)\delta(\mathbf{r}_{ij}), \quad (J^{\pi} = 0^{-}, 1^{+}, \dots) .$$

$g'_{\xi} < 0$  is fixed from (p,n) and (n,p) spectra ( shifts the GT strength downward) 

An increase of  $g'_{\xi}$  leads to shorter  $\beta^{-}$ -decay halflives and softer (p,n) spectra



# GT and FF beta-decay driving operators

## Gamow-Teller decay

(simple operator)

$$e_q [V_0]_{J=1, L=0, S=1} = 2\sqrt{\pi} (1 - 2\zeta_s) \vec{\sigma} \vec{r}$$

$\zeta_s = 0.05 - 0.075$  from Ward's identity

$$e_q [\sigma\tau]^2 = (1 - 2\zeta_s)^2 = \left( \frac{g_A}{G_A} \right)^2 = 0.9^2$$

*eq - GT quenching operator*

Migdal, A.B., Theory of Finite Fermi Systems,

Moscow: Nauka, 1983, 2nd ed. (in Russian)

(1st ed. New York: Interscience, 1967).

## CQRPA

$$P_{ph}(\omega) = -1/\pi \text{Im}(e_q V_0 G_\tau G_\tau V)$$

*... + Ppp*

## First-forbidden decay

(complex operators: contain velocity dependence and interference terms)

$$V_0 = 2\sqrt{\pi} e_q [V_0]_{J, L=1, S} \tau_-$$

$$V_0_{0,1,1} = (1 - 2\zeta_s) \vec{\sigma}^* \vec{r} - e_{q5} \vec{\sigma}^* \vec{P} / 2M$$

$$V_0_{1,1,0} = \frac{1}{\sqrt{3}} (i\vec{r} - \vec{P} / 2M)$$

$$V_0_{1,1,1} = (1 - 2\zeta_s) \sqrt{2} [\vec{\sigma} \vec{r}]^{(J=1)}$$

$$V_0_{2,1,1} = (1 - 2\zeta_s) \frac{2}{\sqrt{3}} [\vec{\sigma} \vec{r}]^{(J=2)}$$

Warburton, E.K., Phys. Rev. C, 1991, vol. 44, p. 233.

*eq5 - FF (J=0) amplification operator*

$$\vec{P} \Rightarrow i\vec{r}, \quad \vec{\sigma}^* \vec{P} \Rightarrow i\vec{\sigma}^* \vec{r}$$

*CVC, PCAC reduction*

I. N. Borzov, Phys. Rev. C 67, 025802 (2003).

# Continuum QRPA

Linear eqs. to be solved in coordinate-space

Each super-matrix has a dimension  $N*N$ , where  $N \sim 4R_{nuc}/\text{mesh size}$

$$\hat{[I - \begin{pmatrix} \underline{F^\xi} & -F^\xi & F^{\omega\xi} & F^{\xi\omega} \\ -F^\xi & \underline{F^\omega} & F^{\xi\omega} & F^{\omega\xi} \\ F^{\omega\xi} & F^{\xi\omega} & F^\xi & -\underline{F^\omega} \\ F^{\xi\omega} & F^{\omega\xi} & -\underline{F^\xi} & \underline{F^\omega} \end{pmatrix} \begin{pmatrix} \underline{L(\omega)} & M(\omega) & N^1(\omega) & N^2(\omega) \\ M(\omega) & L(-\omega) & N^2(-\omega) & N^1(-\omega) \\ N^1(\omega) & N^2(-\omega) & K(\omega) & -M(\omega) \\ N^2(\omega) & N^1(-\omega) & -M(\omega) & K(-\omega) \end{pmatrix} \begin{pmatrix} \underline{V} \\ \underline{V^h} \\ d^{(1)} \\ d^{(2)} \end{pmatrix} = \begin{pmatrix} e_q V_0 \\ 0 \\ 0 \\ 0 \end{pmatrix}]$$

$F^\xi, F^\omega$  - effective NN-interactions in ph and pp channels.

$L, M, N_i, K$  - ph, pp, hh - charge changing propagators  $p(n) \rightarrow n(p)$

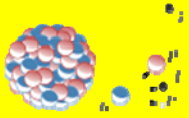
**FRDM:  
RPA**

The  $T=1$  ph-propagator with exact account for continuum and pairing

$$L(r, r'; \omega) = -i \langle r, r'; \omega \rangle + \Sigma \left[ L_{ph} - \frac{1}{\omega} \left| \begin{matrix} \varphi & \varphi & \varphi & \varphi \end{matrix} \right. \right]$$

I.N.Borzov, and E.L.Trykov, Sov. J. Nucl. Phys. 52, 52 (1990).

I.N.Borzov, E.L.Trykov, and S.A. Fayans, Sov. J. Nucl. Phys. 52, 627 (1990).



# Beta-decay half-life

$$S_{\beta}^{JLS}(\omega, \gamma) = \frac{(2J+1)}{4\pi} (e_q^{JLS})^2 \int \underline{\hat{V}_0^{JLS}(r)} \underline{\hat{\rho}^{JLS}(r; \omega, \gamma)} r^2 dr ,$$

$$1/t_{1/2} = D^{-1} (G_A/G_V)^2 \int_{m_e c^2}^{W_{max}} C_{\beta}(W) F(Z, W) p W (W_{max} - W)^2 dW,$$

$$1/T_{1/2} = D^{-1} (G_A/G_V)^2 \int_0^{Q_{\beta}} d\omega \underline{f_0(Z, \omega)} \sum_{n=1,4} \langle \kappa_J \rangle \underline{S_n(\omega, \gamma)}$$

Coulomb ( $\xi$ ) approximation  $E_{Coul} = 6/5 \xi \gg \omega$        $\xi = Ze^2/2Rm_e c^2$

$$C_{\beta} = \sum_{J=0,1} B(J) = \sum_{J=0,1} \left| \frac{\sum_{S=0,1} \langle f | M_{JLS} | i \rangle}{2J+1} \right|^2$$

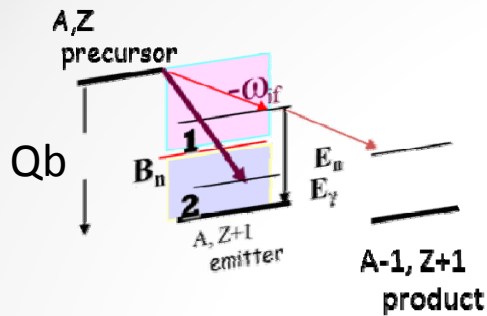
GT  $S=1, J=1, L=0$  and FF (non-unique)  $S, J=0,1; L=1$

# *Near the $N=50,82$ shells*

*Beta-decay properties of isotopes near the  $^{78}\text{Ni}$ ,  $^{132}\text{Sn}$   
are sensitive to the:*

- A) competition of high transition energy FF beta-decays and low-energy GT decays at  $N > N_{\text{mag}}$ .*
- B) interaction induced ground state  $J-\pi$  inversion effects;*
- C) Stabilization of the half-lives near new emerging subshell at  $N=58$ .*

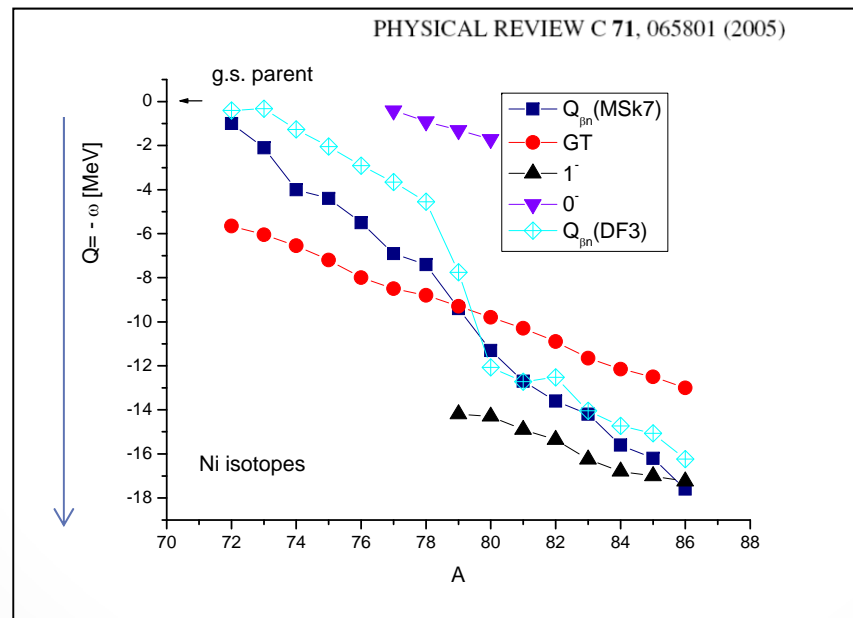
# Reduction of Pn-values in Ni isotopes



$$P_n = \frac{\int_0^{Q_\beta} |S_L(\omega) f_0(Z, \omega) P_\gamma(J_\gamma, E_\gamma) d\omega}{\int_0^{Q_\beta} |S_L(\omega) f_0(Z, \omega) d\omega}$$

$$R_\gamma = \Gamma_n / (\Gamma_n + \Gamma_\gamma)$$

$$\Gamma_\gamma \ll \Gamma_n \Rightarrow R_\gamma \approx 1$$



At  $N > 50$ , the main **GT-decays** undergo to the states located **within the  $Q_{\beta n}$ -window**.

At  $^{79}\text{Ni}$  ( $N=50+1$ ), new channel opens: **high energy FF beta-decay** with  $Q \sim Q_\beta$  undergo **outside the  $Q_{\beta n}$ -window!**

# Reduction of $P_n$ -values in Ni isotopes

**For neutron excess bigger than a major shell  
 $T_{1/2}$  and  $P_n$ -values  
are reduced compared to pure GT approximation.**

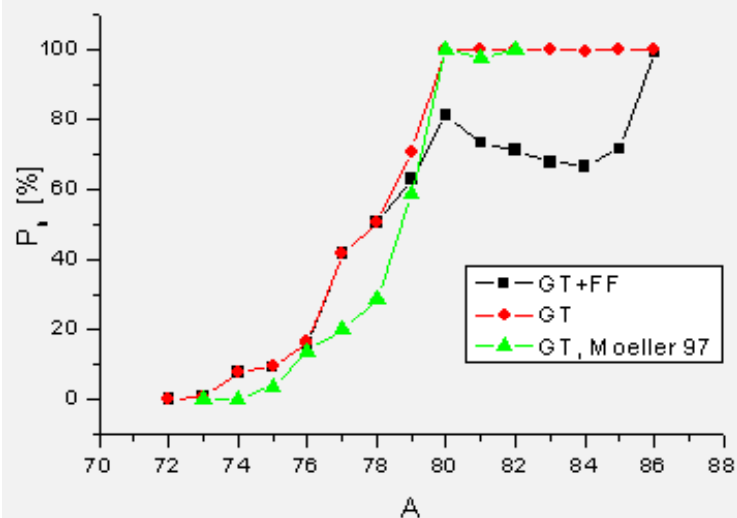
**Reason: the high-energy  $ff$  decays to the states  
outside the  $Q_{\beta}$ - $S_n$  window.**

*I.N. Borzov Phys.Rev. C71(2005)065801*

*New experiments at ORNL, 2011.  
Isobaric purified beams.  
For  $^{82,83}\text{Zn}$   $P_n < 100\%$*

**"GT-only" case :  $P_n$  tends to 100%.**

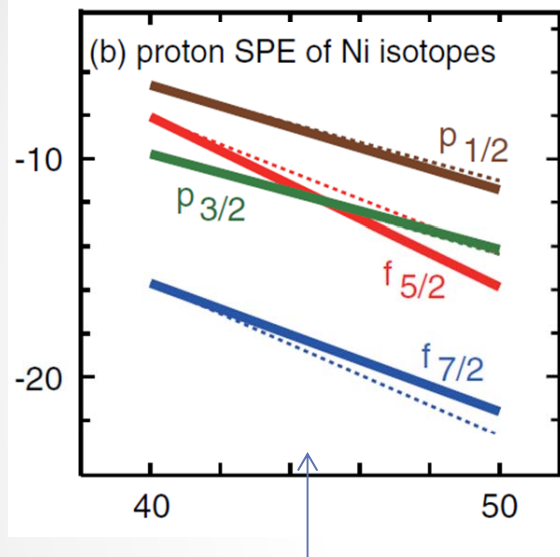
**GT+ff : reduction of  $P_n$ -values !**





Large  $\beta$ -Delayed Neutron Emission Probabilities in the  $^{78}\text{Ni}$  Region

J. A. Winger,<sup>1,\*</sup> S. V. Ilyushkin,<sup>1</sup> K. P. Rykaczewski,<sup>2</sup> C. J. Gross,<sup>2</sup> J. C. Batchelder,<sup>3</sup> C. Goodin,<sup>4</sup> R. Grzywacz,<sup>5,2</sup>  
 J. H. Hamilton,<sup>4</sup> A. Korgul,<sup>6,5,4,7</sup> W. Królas,<sup>8,7</sup> S. N. Liddick,<sup>3,5</sup> C. Mazzocchi,<sup>5,9</sup> S. Padgett,<sup>5</sup> A. Piechaczek,<sup>10</sup>  
 M. M. Rajabali,<sup>5</sup> D. Shapira,<sup>2</sup> E. F. Zganjar,<sup>10</sup> and I. N. Borzov<sup>11</sup>

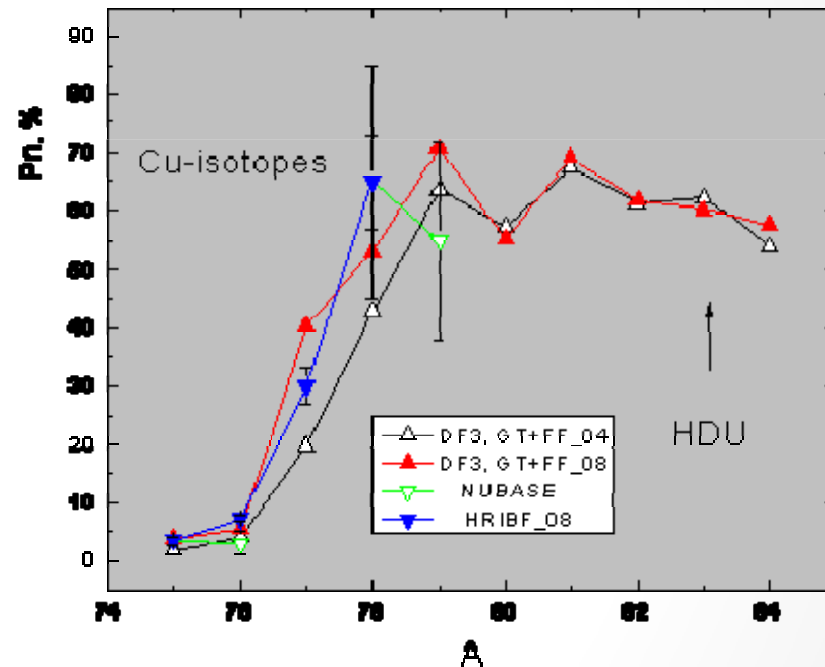


T. Otsuka et al. PRL 104, 012501 (2010)

**SM: inversion at  $A=73$ .**

**SkP, DF3: at  $A \sim 79$ .**

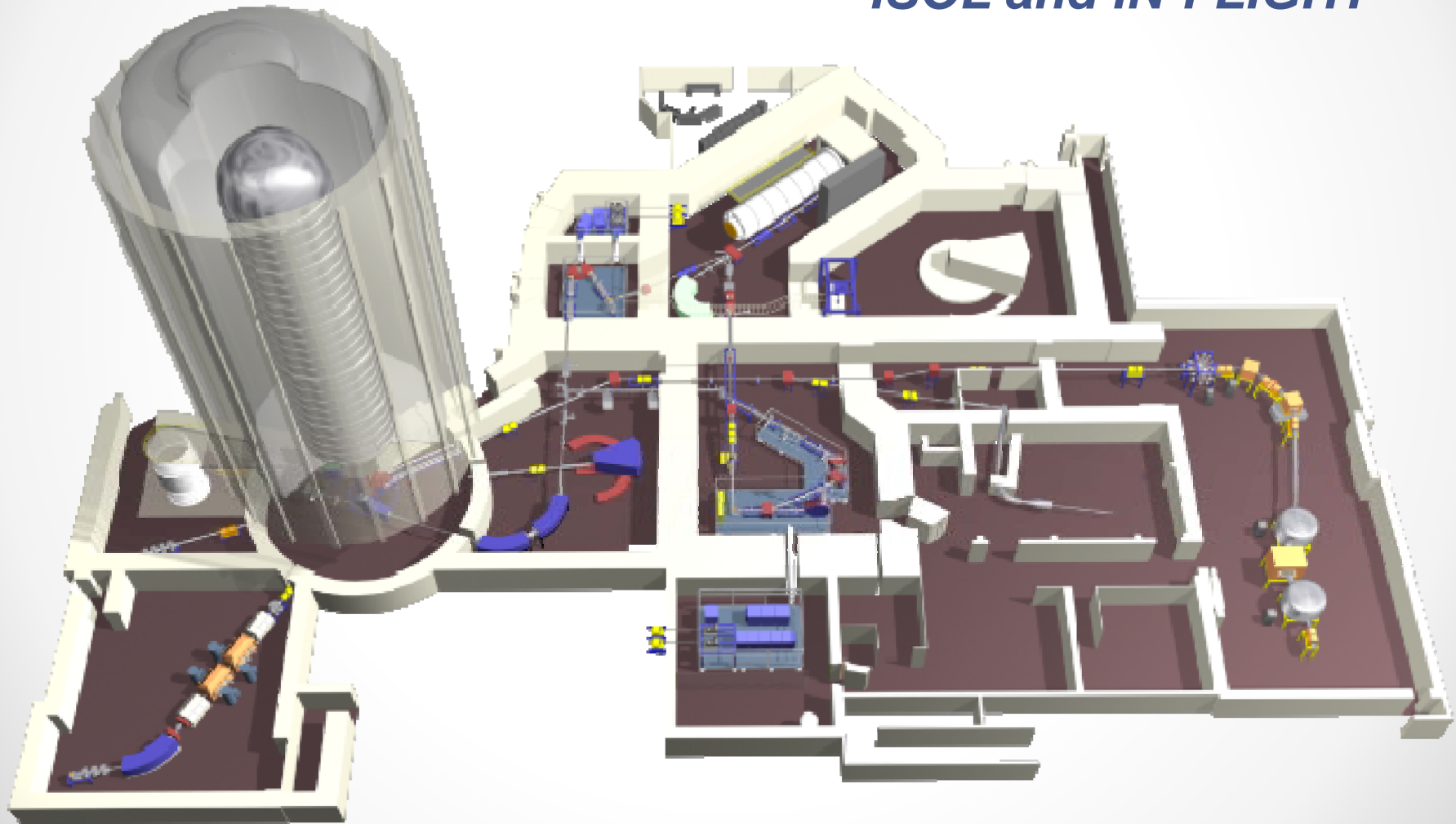
Magnetic moments measurements:  
 in Cu isotopes  $\pi 2p_{3/2} \rightarrow \pi 1f_{5/2}$  at  $A > 75$ .  
 K. Flanagan et al PRL 103(2010)142501



**DF3 with fixing the odd proton  
 at  $1\pi f_{5/2}$  in  $A > 75$  (blocking).  
 Pn-S shift in a right direction.**

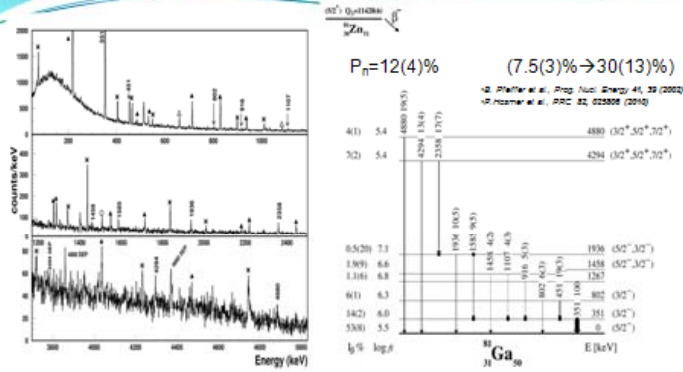
# *Holifield Radioactive Ion Beam Facility accelerators and separators*

***ISOL and IN-FLIGHT***



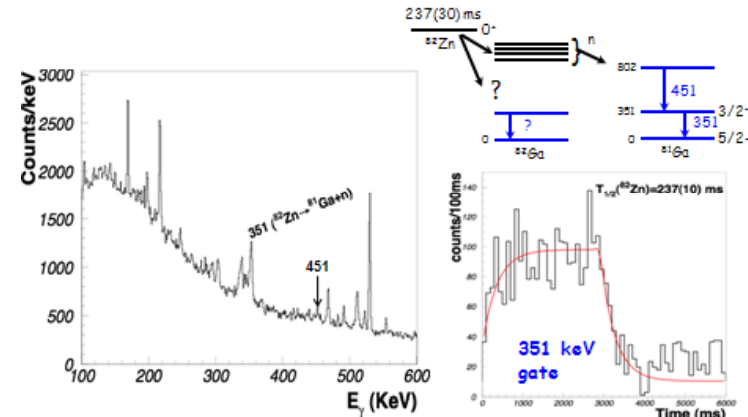
# Zn isotopes A=81-83

## Summary of $^{81}\text{Zn}$ results



- >11 gamma transitions observed, 9 new ones.
- >All placed in level scheme → 5 new states
- >Pure  $^{81}\text{Zn}$  beam
- >2008  $^{81}\text{Zn}$  rate: 30 pps → 2011: ~300 pps

## Decay spectroscopy of $^{82}\text{Zn}$



S. Padgett et al. PRC 82, 064314, 2010

“We consider only exp.data for our evaluation not to be **contaminated** by any theory data...”



- Isobarically purified beam (no isobaric contamination)
- Tandem post-acceleration (optional)
- LeRIBSS: mass & isobaric separation  $\beta$ ,  $\beta_n$ ,  $\beta_Y$ ,  $\beta_n Y$

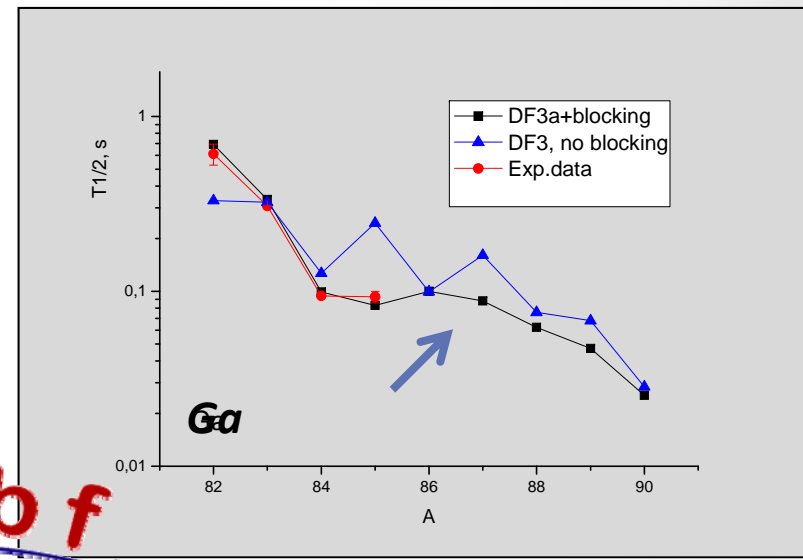
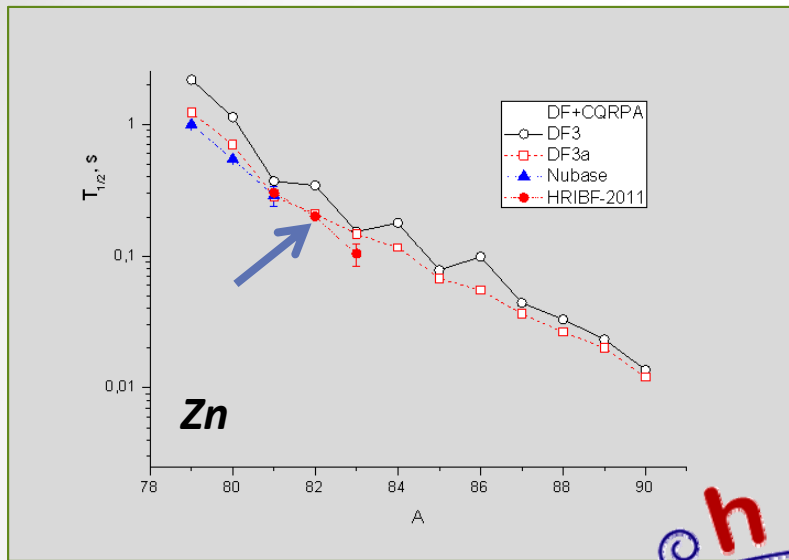
OAK RIDGE NATIONAL LABORATORY  
MANAGED BY UT-BATTELLE FOR THE DEPARTMENT OF ENERGY

## Newly measured half-lives of extremely exotic Zn and Ga isotopes alter calculated isotope abundances

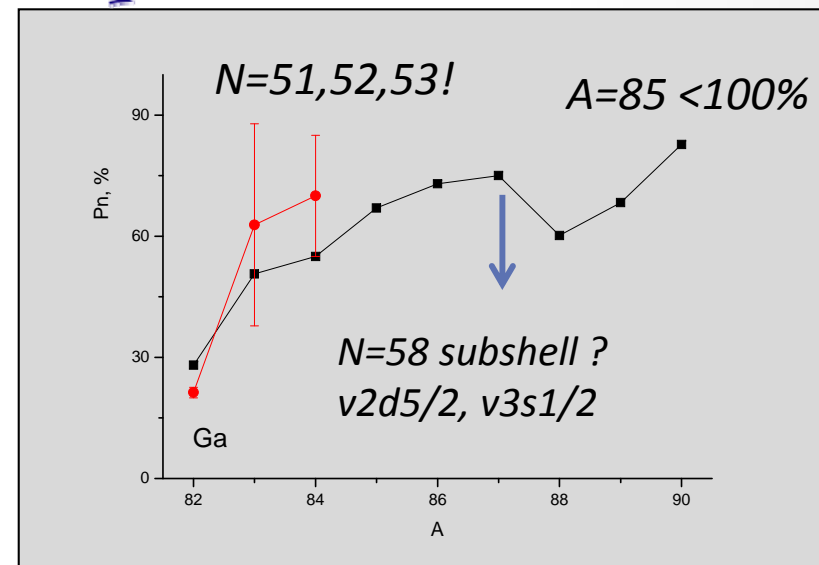
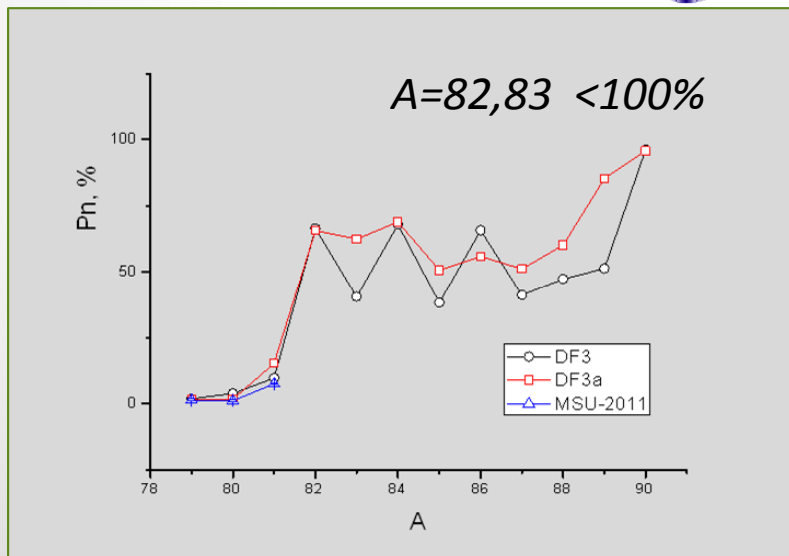
Researchers have, for the first time, identified the  $\beta$  decay of the extremely neutron-rich isotopes  $^{82}\text{Zn}$ ,  $T_{1/2}=202(7)$  ms, and  $^{83}\text{Zn}$ ,  $T_{1/2}=104(20)$  ms, and measured the  $\beta$ -decay half-life of  $^{85}\text{Ga}$  to be 86(5) ms [Madurga2011]. Neutron-rich isotopes occur in environments such as type II supernova explosions believed to be a site of the rapid neutron-capture process and in nuclear reactor fuel. New data contribute to the input for large network calculations leading to better understanding of the abundances of isotopes created in these extreme environments.

The Holifield Radioactive Ion Beam Facility (HRIBF) produces very neutron-rich nuclei using proton-induced fission of  $^{238}\text{U}$  and is able to produce radioactive samples with enhanced isotopic purity. Zinc-82 is among “r-process waiting-point” isotopes, where  $\beta$ -decay is more likely to occur than neutron-capture. Zinc-83 and  $^{85}\text{Ga}$  are now the most neutron-rich Zn and Ga isotopes with known  $\beta$ -decay properties, see Fig. 1. The measured half-lives indicate  $\beta$ -decay probability larger than estimated earlier. The half-life and nuclear structure information obtained from HRIBF experiments have been used to refine the theoretical modeling of the  $\beta$ -decay process within the continuum quasi-particle random phase approximation [Borzov2005, Winger2009]. The experimental half-lives and resulting changes in theoretical extrapolations have been used to re-analyze the post r-process isobaric distribution [Surman2011], see Fig. 1. This new analysis includes accelerated r-process decay rates and shows a redistribution of isotopic abundances for heavy nuclei.

# DF-CQRPA vs. ORNL HRIBF 2011 measurements in Zn and Ga



*hrifb*



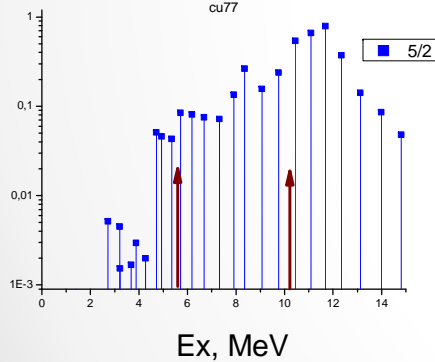
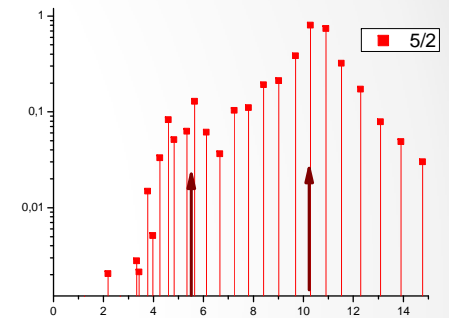
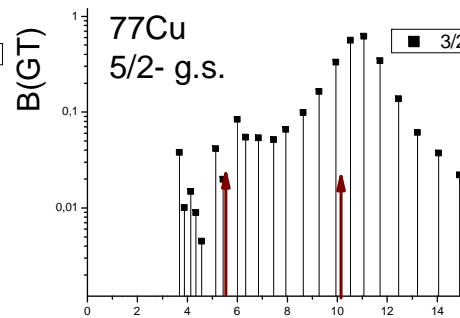
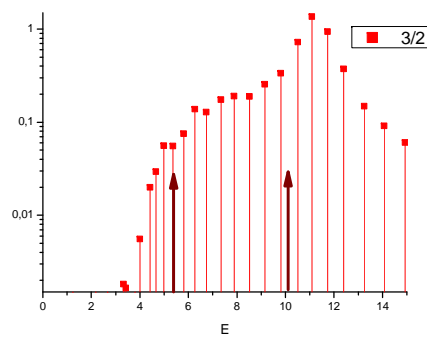
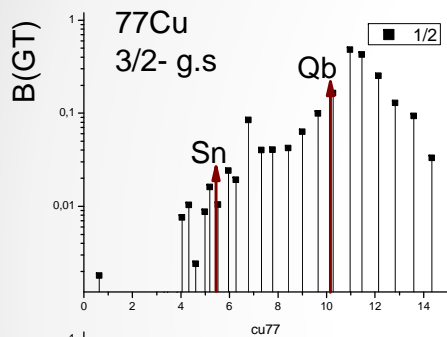
S. Padget et al. PRC 82, 064314, 2010

J. Winger et al. PRC 81, 044303, 2010  
M. Madurga et al., to be published 2011

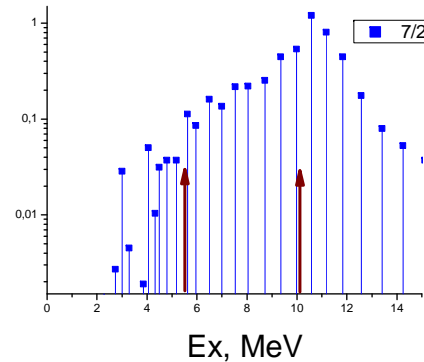
# Partial beta-strength functions. (K. Sieja, F. Novacki, 2010, p.c.)

~~Parent 3/2<sup>-</sup> g.s.~~

Parent 5/2<sup>-</sup> g.s.



K.Sieja, F.Novacki, 2011

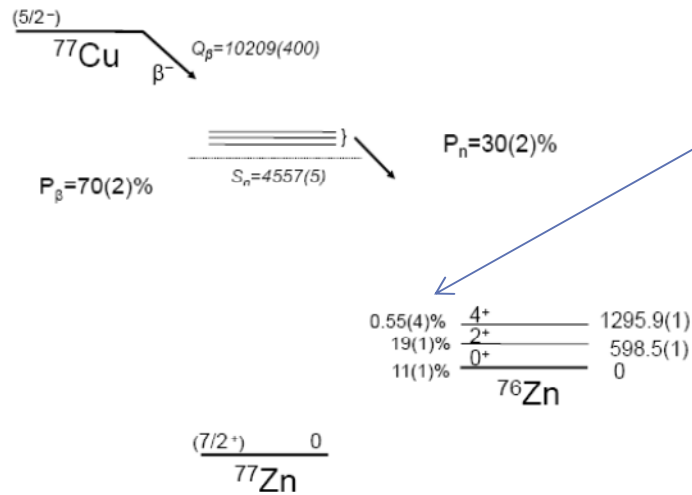


K.Sieja, F.Novacki, 2011

Sensitivity to the  $^{77}\text{Cu}$  g.s.  $J/\pi$   
At least GT-distributions  
for  $j_f=1/2$  and  $7/2$  differ.

CD-Bonn potential.  
48Ca core.  
p:  $f7/2, f5/2, p3/2, p1/2$   
n:  $f5/2, p3/2, p1/2, g9/2$   
→ fp / up to 8p8h  
N=40 / 7\*10(8)

# Fine structure of delayed neutron Pn-s.



A. Korgul et al. , to be published 2011

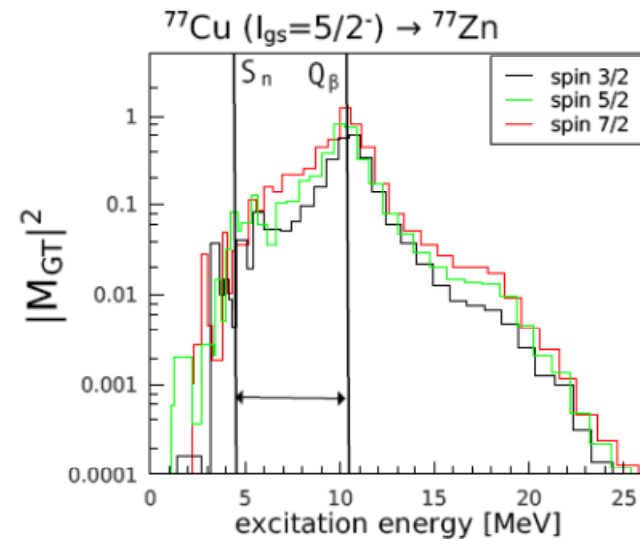


FIG. 6. Partial decay schemes of  $^{77}\text{Cu}$  and  $^{77}\text{Zn}$ . Partial and total branching ratios for  $\beta n$  emission are shown as well as the branching ratios for  $\beta$ -decay. The values for branching ratio of  $^{77}\text{Cu}$  and  $^{79}\text{Cu}$  are deduced from data published in [8], [14] and our work. Excited states in  $^{76,78}\text{Zn}$  are not in energy scale. All energies are in keV. The values of  $Q_\beta$  and  $S_n$  energies are taken from [33, 34]. See text for more details.

## $^{77}\text{Cu} - \beta n \rightarrow ^{76}\text{Zn}$ (HRIBF)

0.55(4)%	4+	
19(1)%	2+	(5, 7/2- + $l_n=1$ )
11(1)%	0+	(3/2- + $l_n=1$ )

**Fine structure of  $P_n(E_n)$  in  $(Z+1, N-2)$  products is affected by distribution of the partial GT strengths near  $S_n$  and  $l_n$  ; structure of the wave functions of GT de-excitations in  $^{77}\text{Zn}$  (different 1qp and 3qp decay rates to the g.s. and excited states).**



# Newly measured half-lives of extremely exotic Zn and Ga alter calculated isotope abundances

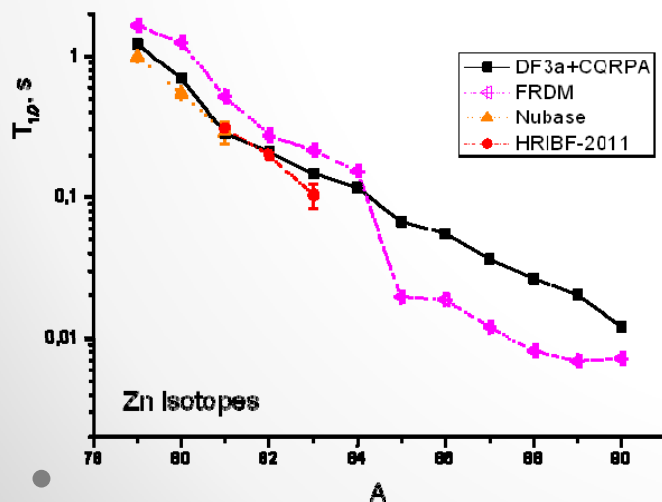
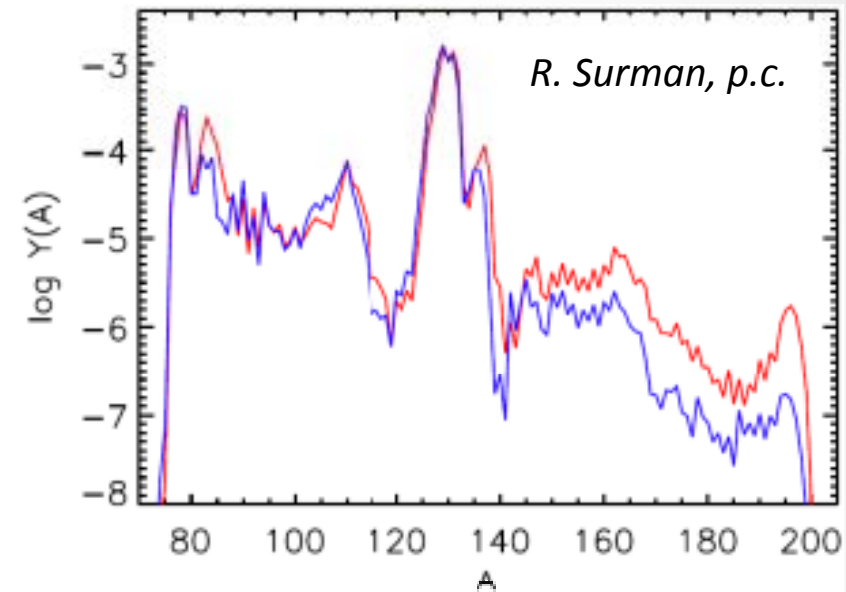
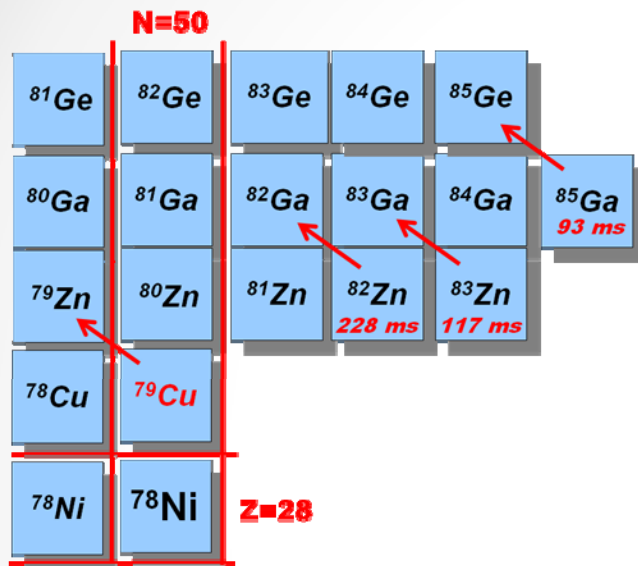


Fig. 1. (left) Section of the chart of nuclei near doubly magic  $^{78}\text{Ni}$  is shown. Marked isotopes above  $^{78}\text{Ni}$  are among the nuclei studied at the HRIBF [Winger2010, Padgett2010]. Newly measured half-lives for  $^{82}\text{Zn}$ ,  $^{83}\text{Zn}$  and  $^{85}\text{Ga}$  isotopes are given in red. (right) The r-process abundances (note logarithmic scale) **calculated using new experimental and theoretical half-lives (red curve)** are compared to previous simulations (**blue curve**).

M. Madurga et al., to be published 2011



# *How good are “first-principle” nuclear structure models in extrapolating beta-decay data?*

*Theoretical models give deviating extrapolations far from stability.  
DF+CQRPA extrapolation is supported by recent data for WF-nuclei.*

**NB!** *T<sub>1/2</sub>, P<sub>n</sub>-s are functionals of Gamow-Teller strength distribution.  
Different beta-strength functions may result in close T<sub>1/2</sub>, P<sub>n</sub>-s.*



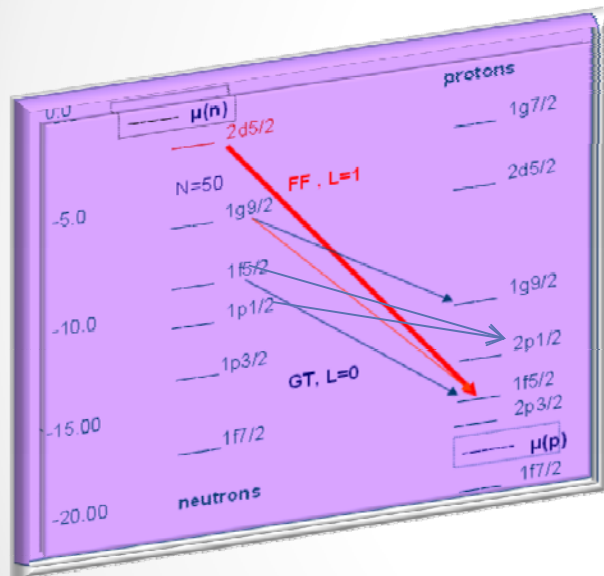
Георгий (George) А. Гамов (Gamow)



Teller (Edward) Ede

*As FF decays across the major shell are not expected at  $N < 50$ , DF+CQRPA gives no impact of FF decays for  $N=50,82$  isotones*

*A comparison with quantum-statistical description of FRDM:  
RPA for GT + Gr.Th. for FF decays ... gives a  
strong impact of the FF decays: see the last two columns of Table.*



DF3+CQRPA

FRDM

Nucleus	Expt.	GT [22]	GT + FF [22]	GT [14]	GT + FF [15]
$^{78}\text{Ni}$	$0.110^{+0.100}_{-0.060}$ [26]	0.102	0.102	0.477	0.224
$^{79}\text{Cu}$	$0.257^{+0.29}_{-0.26}$ [26]	0.266	0.257	0.430	0.157
$^{80}\text{Zn}$	$0.188 \pm 0.25$	$0.865$	$0.839$	$3.068$	$1.259$
$^{129}\text{Ag}$	$0.578 \pm 0.21$ [26]	0.061	0.056	0.047	0.0317
$^{130}\text{Cd}$	$0.545 \pm 0.16$	0.15	0.14	1.123	0.502
$^{131}\text{In}$	$0.280 \pm 0.030$	0.35	0.34	0.147	0.139

ЯДЕРНАЯ ФИЗИКА, 2011, том 74, № 10, с. 1-11

ЯДРА

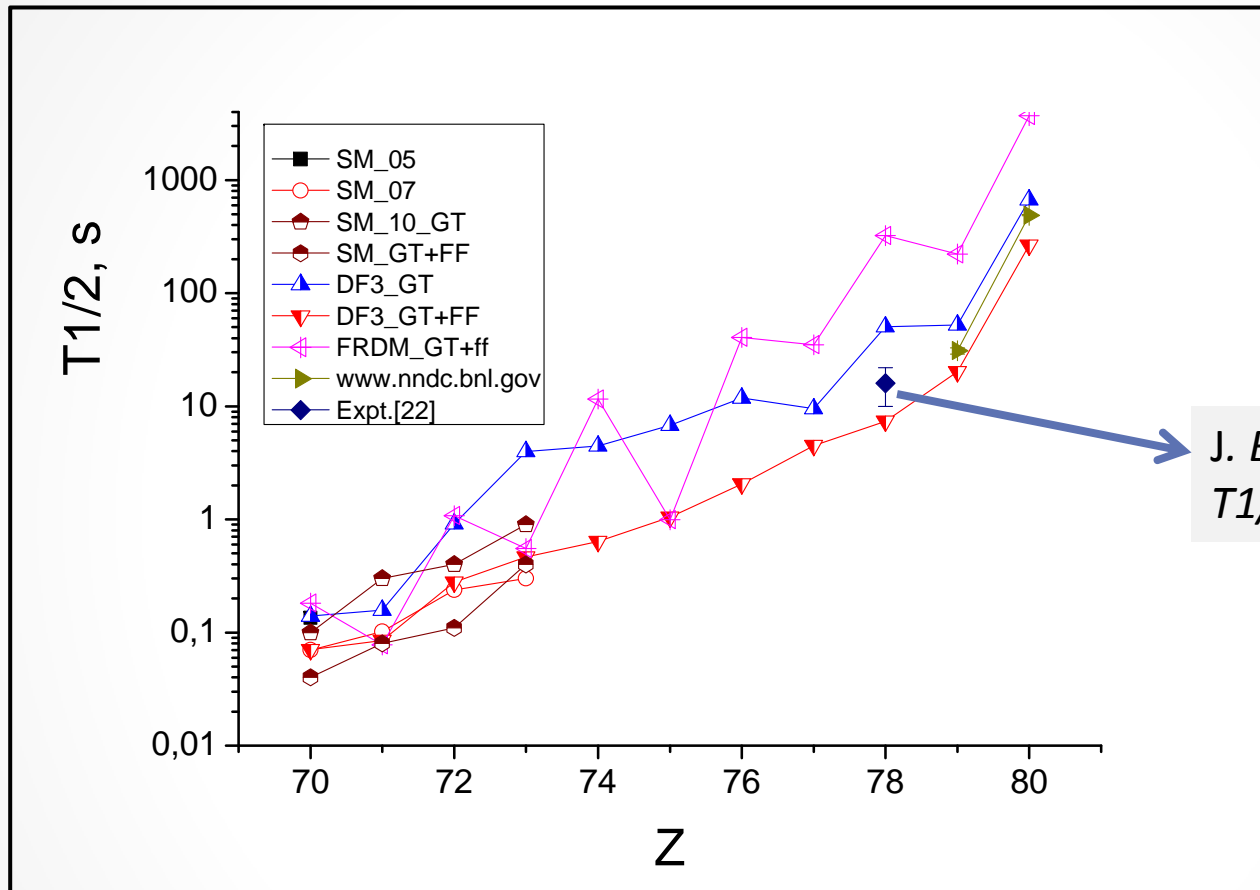
BETA-DECAY OF NUCLEI NEAR THE NEUTRON SHELL  $N = 126$

© 2011 I. N. Borzov\*

Joint Institute of Heavy Ion Research, Oak Ridge, USA  
Received December 23, 2010; in final form, April 26, 2011

*In DF+CQRPA  
fast decays at  $N=50,82$   
are due to GT transitions*

# *N=126 isotones: FF decays are important*



J. Benliure e a. 2010,  
 $T_{1/2}(204\text{Pt}) = 16 + 6 - 5 \text{ s}$

*Taking off the  $T=0$  pp-effective NN-interaction leads to  $SO(8)$ -symmetry violation of QRPA. An odd-even effect in FRDM at  $N=126$  is not supported by the existing data.*

*SM10 (GT+FF)  
 T. Suzuki et al.  
 Non-standard  $J=0$  operator*

# *Near the $N=126$ shell*

*Recent experiments GSI, USC ...*

*2007-2010*

*K.-H. Schmidt, J. Benlliure et al.*

*2011*

*S410*

*I. Dillmann et al.*

*The  $Q_{\beta}$ -values of reachable isotopes south-west of  $^{208}\text{Pb}$  are relatively low. Nevertheless, their  $\beta$ -decay properties reflect a competition of high transition energy FF  $\beta$ -decays and low-energy GT decays at  $N \sim N_{\text{mag}}$ .*

# GSI, Darmstadt



The experiment, which aimed at measuring the  $\beta$  half-lives of heavy neutron-rich nuclei close to the neutron closed shell  $N = 126$  was performed at the fragment separator FRS [9] at the Gesellschaft für Schwerionenforschung (GSI) in Darmstadt, Germany. A  $^{208}\text{Pb}$  primary beam of 1 A GeV, delivered by the SIS18 heavy-ion synchrotron, was directed to a beryllium target at the entrance of the FRS. The reaction residues were identified by determining both their atomic number  $Z$  and their mass-over-charge ratio  $A/Z$  by means of the measurements of the energy loss, the magnetic rigidities, and the time of flight (ToF).



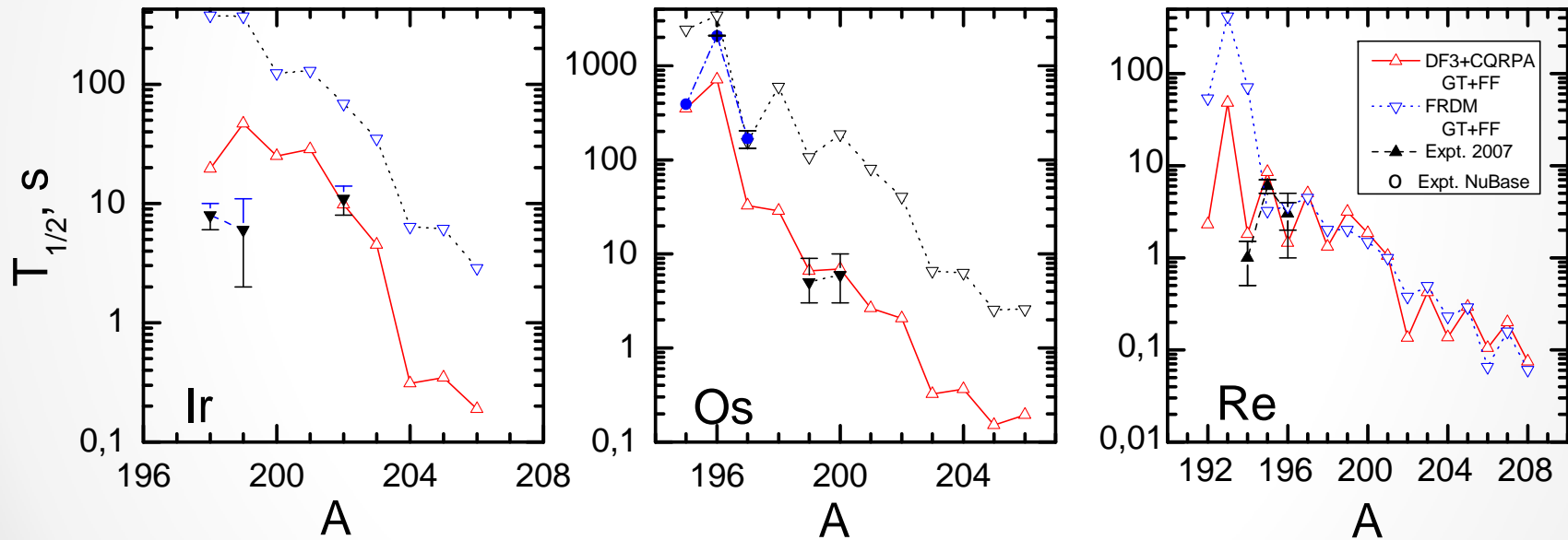


# First access to $\beta$ -decay half-lives approaching the r-process path near $N=126$

T. Kurtukian-Nieto<sup>a,1</sup>, J. Benlliure<sup>a</sup>, K.-H. Schmidt<sup>b</sup>, L. Audouin<sup>c</sup>, F. Becker<sup>b</sup>, B. Blank<sup>d</sup>, I.N. Borzov<sup>b,2</sup>, E. Casarejos<sup>a</sup>, M. Fernández-Ordóñez<sup>a,3</sup>, J. Giovinazzo<sup>d</sup>, D. Henzlova<sup>b,4</sup>, B. Jurado<sup>d</sup>, K. Langanke<sup>b,e</sup>, G. Martínez-Pinedo<sup>b</sup>, J. Pereira<sup>a,4</sup>, F. Rejmund<sup>f</sup>, O. Yordanov<sup>b,5</sup>

*GSI FRS- Collaboration 2007*

*T.Kurtukian-Nieto et al. nucl-ex.0711.0101v1, 2007;  
Nucl.Instr.Meth. A589,472,2008.  
Nucl. Phys. A 589,472c, 2008.*

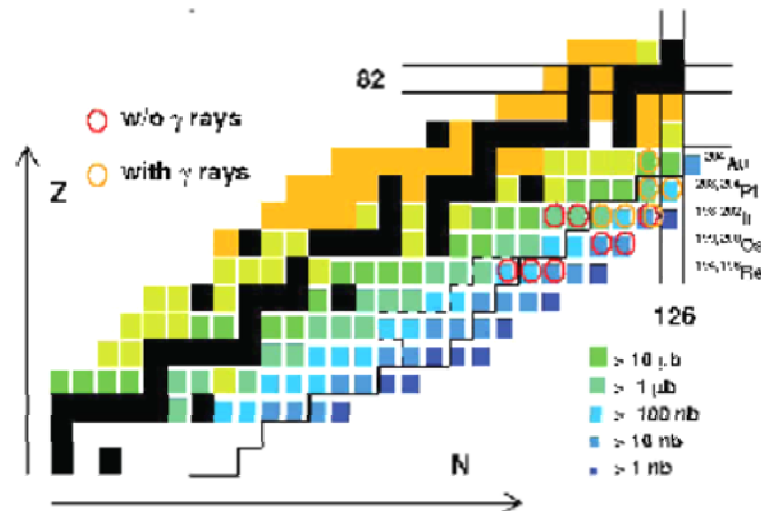


*From a theory side global predictions based on self-consistent microscopic models may facilitate the choice of appropriate experimental conditions.*

*The prospects for extending this experimental approach to more neutron-rich isotopes of elements below lead are very promising, in particular when higher beam intensities will become available in new-generation in-flight secondary-beam facilities, like FAIR at GSI, the RI Beam Factory of RIKEN, FRIB at MSU or HRIBF at ORNL.*

# $\beta$ half lives

## Results



The  $\beta$  half lives of 13 heavy neutron-rich nuclei have been determined, 11 of them for the first time.

Nuclei	w/o $\gamma$	with $\gamma$	other works	FRDM+ QRPA <sup>[1]</sup>	DF3+ QRPA <sup>[2]</sup>
<sup>204</sup> Au		$37 \pm 0.8$ s	$39.8 \pm 0.9$ s		
<sup>204</sup> Pt		$16_{-5}^{+6}$ s		321.8 s	7.4 s
<sup>203</sup> Pt		$22 \pm 4$ s		654.0 s	12.7 s
<sup>202</sup> Ir	$11 \pm 3$ s	$15 \pm 3$ s		68.4 s	9.8 s
<sup>201</sup> Ir		$21 \pm 5$ s		130.0 s	28.4 s
<sup>200</sup> Ir		$43_{-3}^{+6}$ s		124.1 s	25.0 s
<sup>199</sup> Ir	$6_{-4}^{+5}$ s			370.6 s	46.7 s
<sup>198</sup> Ir	$8 \pm 2$ s		$8 \pm 1$ s	377.1 s	19.1 s
<sup>200</sup> Os	$6_{-3}^{+4}$ s			187.1 s	6.9 s
<sup>199</sup> Os	$5_{-2}^{+4}$ s			106.8 s	6.6 s
<sup>196</sup> Re	$3_{-2}^{+1}$ s			3.6 s	1.4 s
<sup>195</sup> Re	$6 \pm 1$ s			3.3 s	8.5 s
<sup>194</sup> Re	$1 \pm 0.5$ s			70.8 s	2.1 s

[1] P. Möller, et al. PRC 67, 055802 (2003)

[2] I. N. Borzov PRC 67, 025802 (2003)



# Systematic study of $Q_\beta$ – values in $Z=70-80$ , $N=126$ region.

Accurate description of the  $Q_\beta$ -values is crucial for beta-decay studies.

$Q_\beta$  is correlated with the  $qp$ -energies, as both are obtained from the same DF framework.

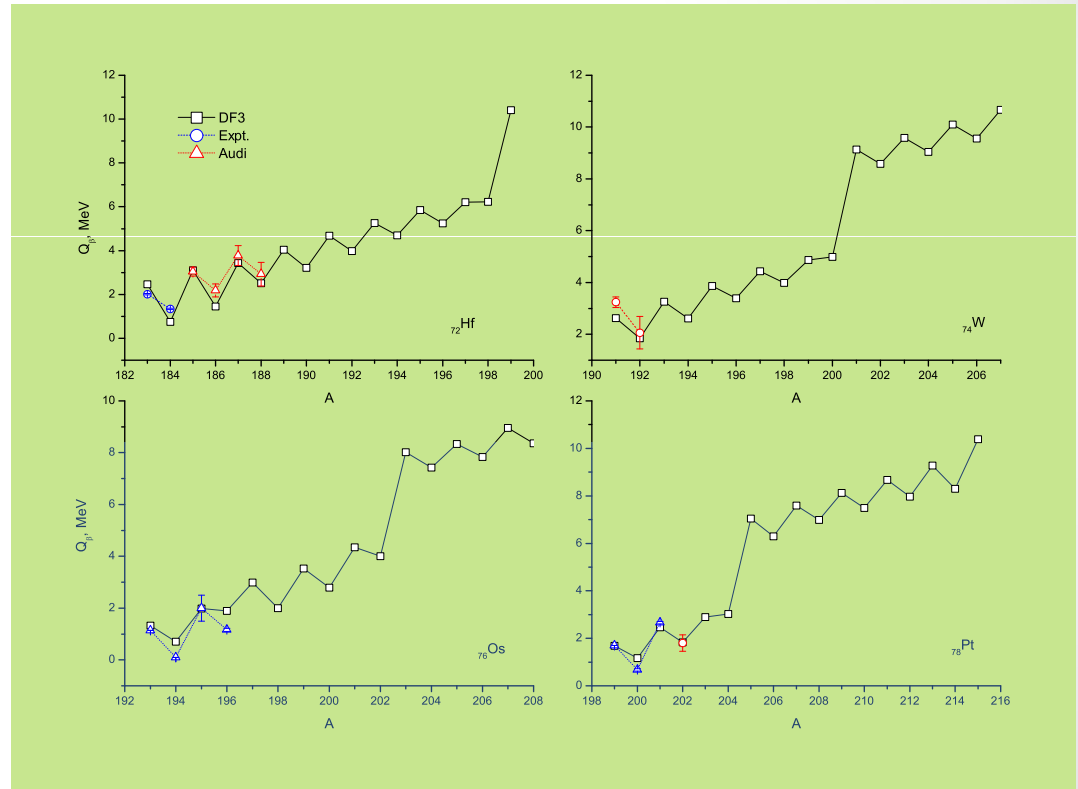
DFs with  $m^*/M \sim 1$  reproduce  $Q_\beta$ -values well enough :

**For  $N=50, 82$ :**

Typical deviation from the data is 0.5 - 1.5 MeV

**For  $N \sim 126$ :**

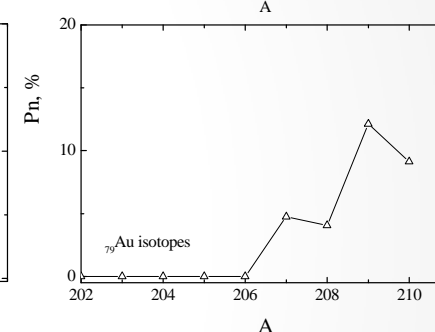
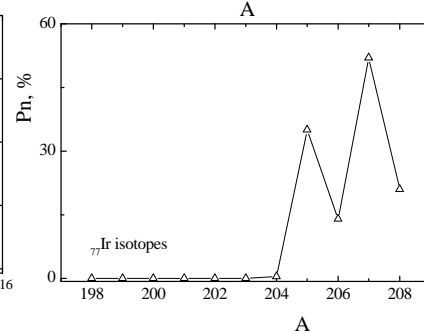
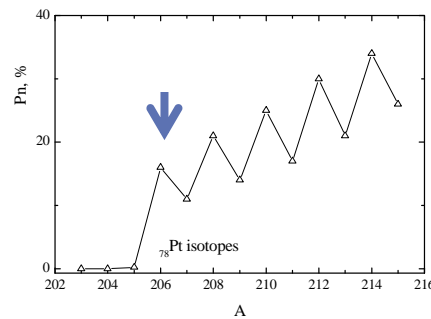
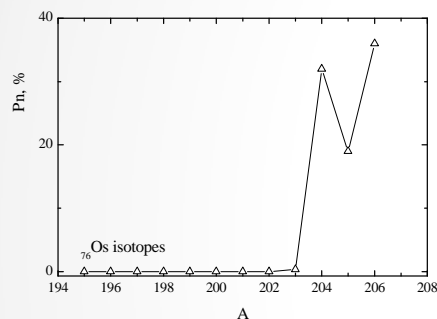
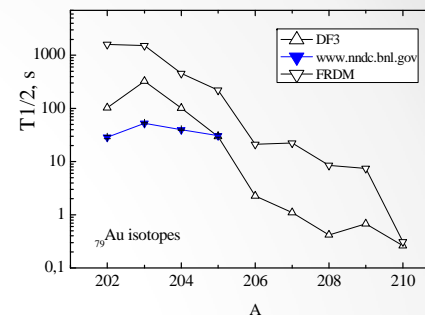
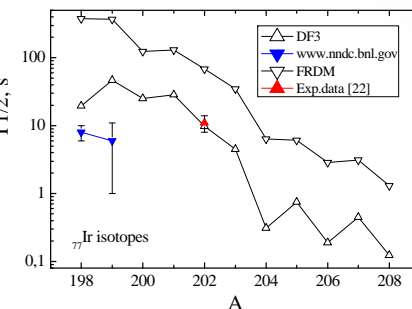
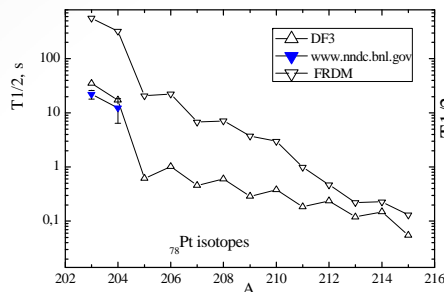
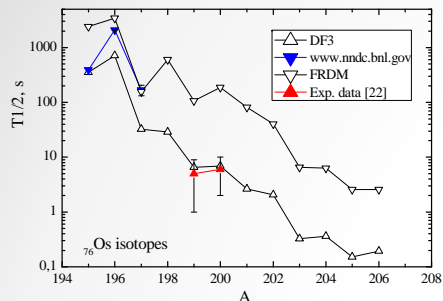
Higher accuracy, as deviation  $\sim 1/A$   
0.5 - 0.8 MeV



**NB!** Approaching  $N=126$  : further from stability , larger is  $N-Z$ , closer we are to the  $r$ -process paths.  $Q_\beta$ -values increase, as well as relative probability of the FF transitions. Favorable conditions for competition of the GT & FF decays...

- (The usual nomenclature of  $\log(ft)$ -values should not be taken too literally in this case.)

# Systematic study of half-lives and Pn-s in Z=70-80, N=126 region

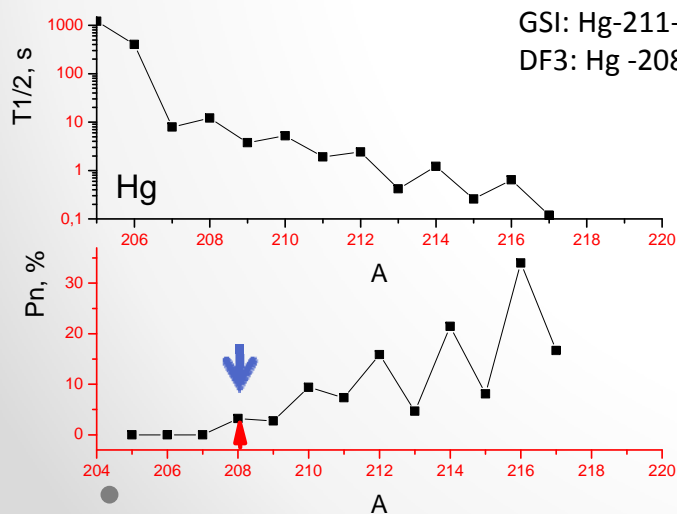


*I.N.B. Phys.At.Nucl.74,2011, 1435.*

*GSI S410 (September, 2011)*

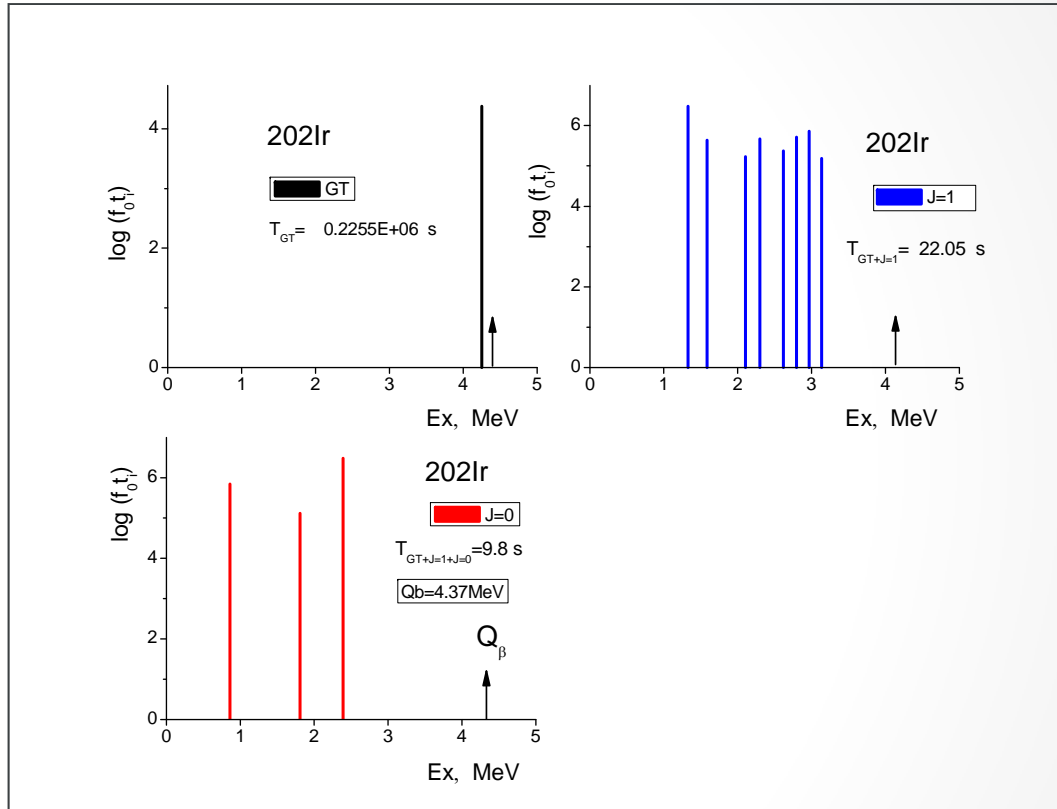
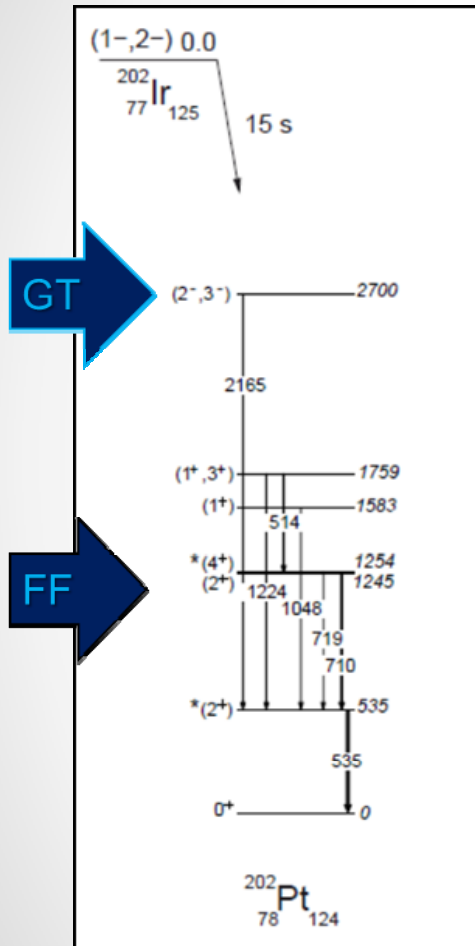
*... isotopes with Pn-s to be measured are  
Ir-204-206 Pt-208-209, Au-207-211  
Hg-211-213 Tl-213-216.*

*(From calculations already Pt-206 and 207  
could be measured!)*



# Microscopic origin of accelerated beta-decays at $N=126$ . Beta-strength functions: GT vs. $J=0$ , $J=1$ .

I.N.B Phys.At.Nucl .74 (2011) 1435

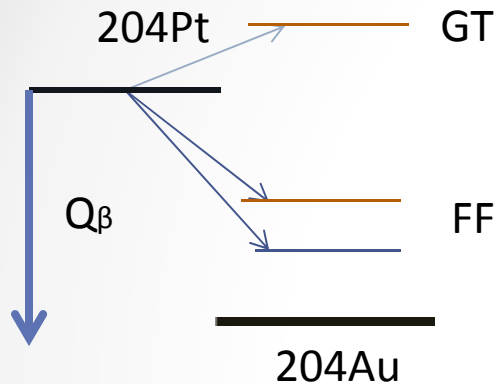


Very low transition energy (high-excitation energy) GT:  
 $n1h9/2 \rightarrow p1h11/2$  : retarded by low phase-space factor  $f(Qb-Ex)$  and high occupancy factor of proton orbital  $u^2(p1h11/2)$ .

A. Morales, USC thesis, 2010

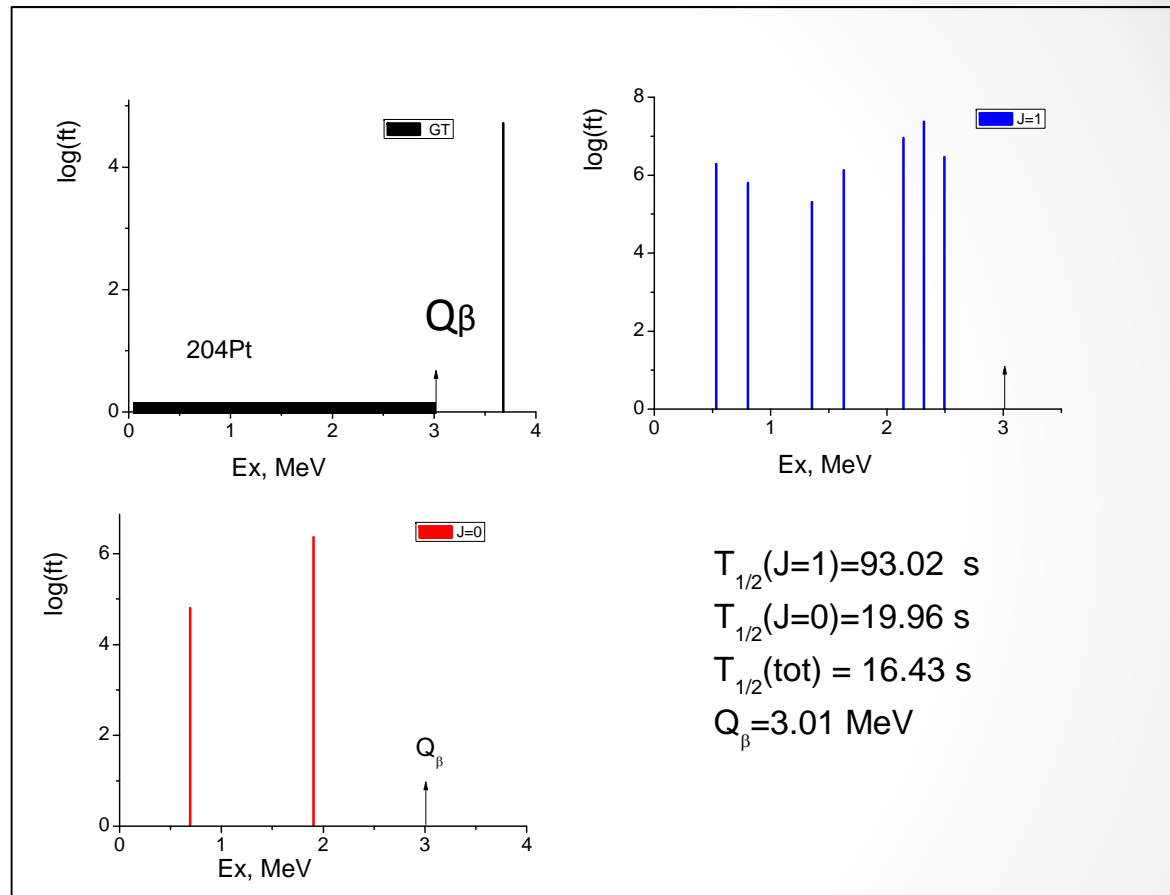
A bunch of higher transition energy FF-s "built" on  $n1i13/2 \rightarrow p1h11/2$  reduce the half-life **drastically**:  $T_{1/2}(GT)=0.23(+06)s \rightarrow T_{1/2}(tot)=9.8s!$

# $N=126$ waiting-point nucleus $^{204}\text{Pt}$



$$T_{1/2_{\text{exp}}} = 16+6-5 \text{ s}$$

J. Benlliure,  
Talk at NIC-XI, 2010

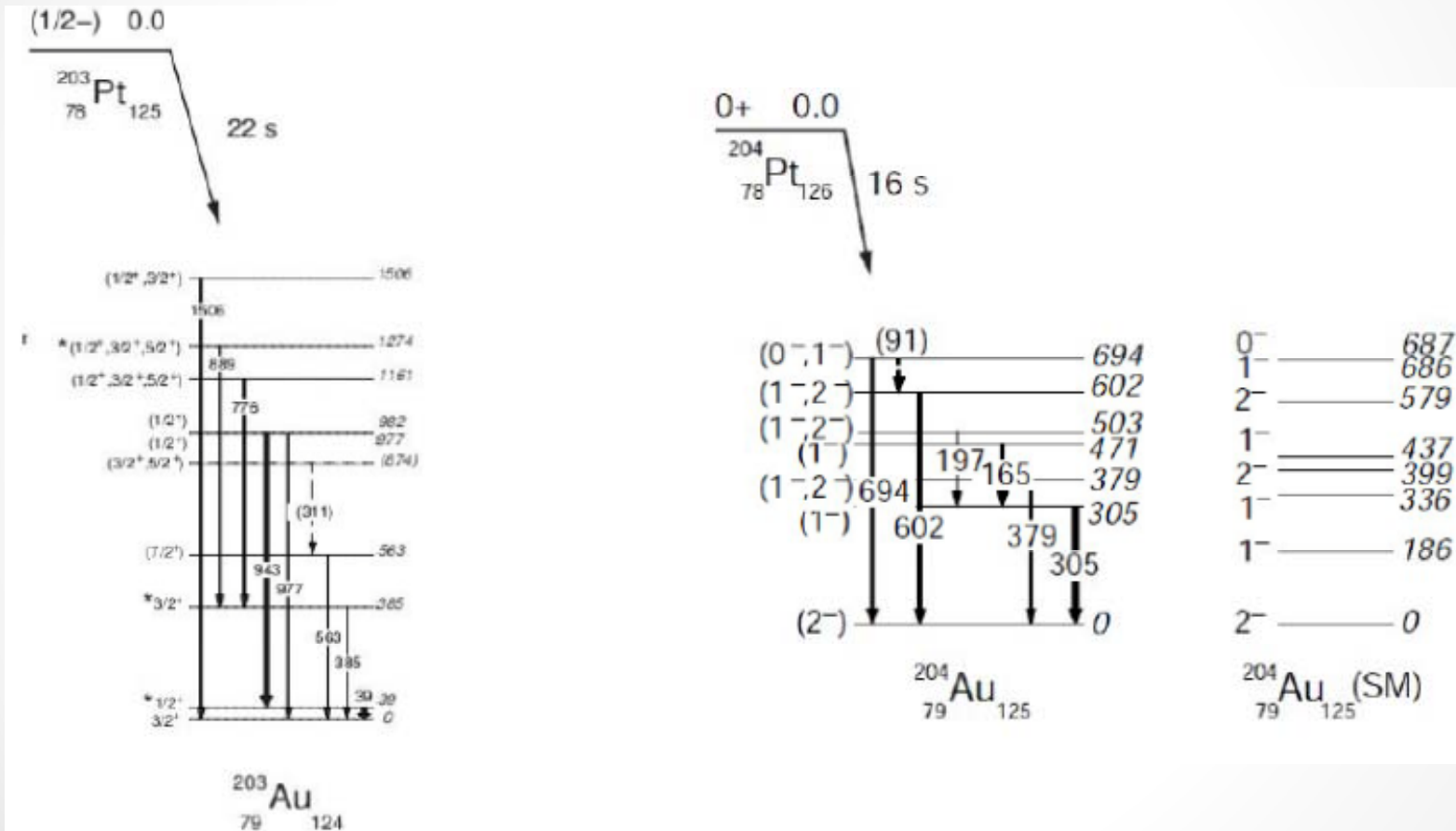


- **No GT-states within (rather small) Q-window according to our 1ph-QRPA prediction.**
- **Interesting case: total half-life is solely due to the FF-decays!**

*I.N.B. Phys.At.Nucl.74,2011, 1435.*

# Recent USC experiment in 203,204Pt:

*evidence for high-energy FF transitions*

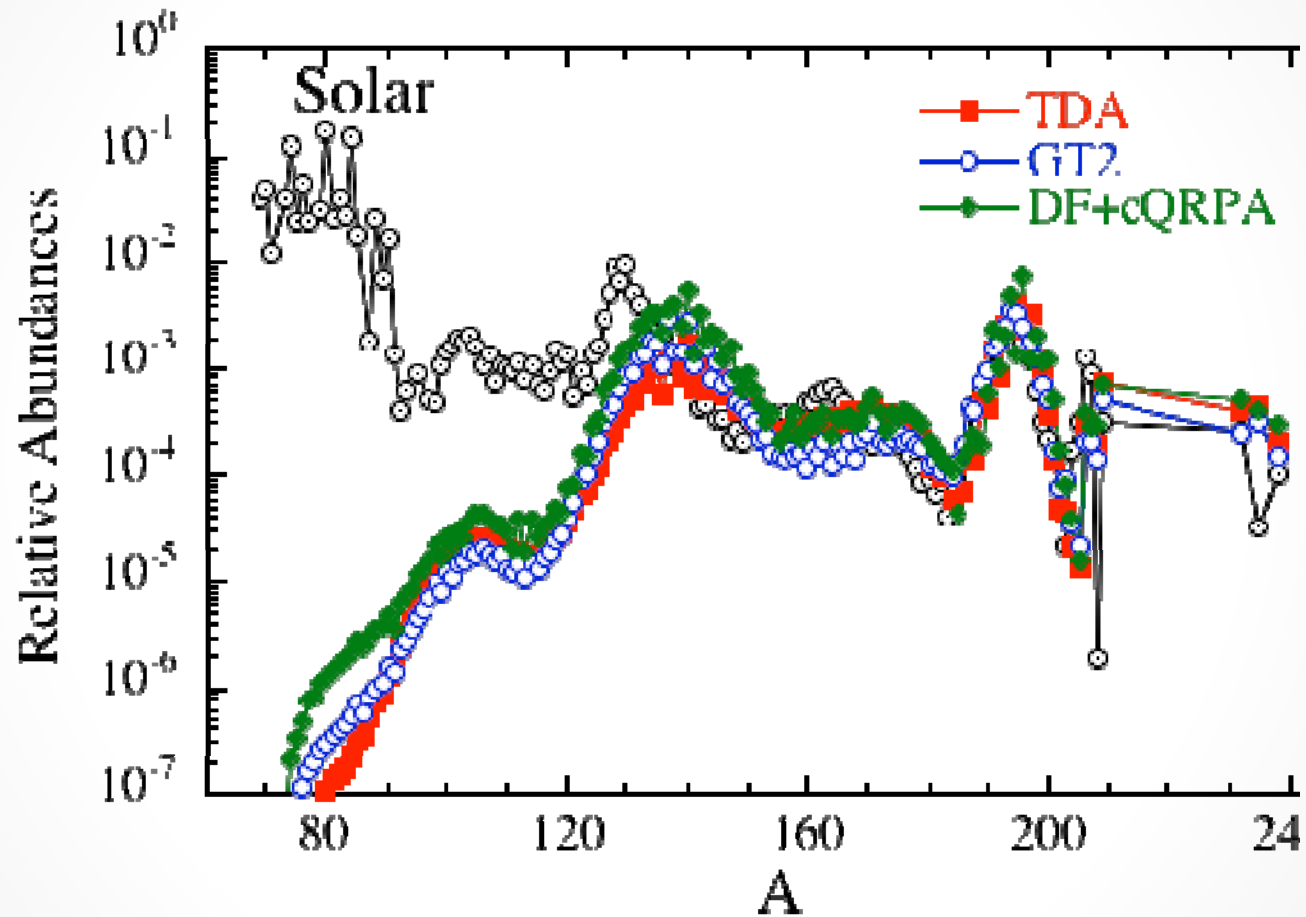


A. Morales, USC thesis, 2010

**Waiting for S-410 GSI results !**

# Astrophysical *r*-process nucleosynthesis

Abundances with DF3 beta-rates for  $Z > 24$  up to  $Z = 84$



TDA- H.-V.Klapdor-Kleingrothaus et al.  
GT2- T.Tachibana et al.

INB, S. Goriely, preliminary, June-011.



*“We will consider only experimental data ...  
for our evaluation not to be **contaminated** by any theoretical data...”*

1. *“...in most cases, the  $\beta$ n-measurements were performed with radioactive beams **containing more than one isotopes**. However the  $P_n$ -values can be determined reliably with an **isobarically purified beam** of  $\beta$ n-precursor of known intensity and subsequent measurements of  $\gamma$ -radiation properties along the mass  $A$  and  $A-1$  chains with efficiency calibrated  $\gamma$ -detectors.” (HRIBF ORNL report, 2011)*
2. *Theoretical extrapolation is unavoidable!  
The best observable to compare with data is **beta-decay strength function**.  
Constrains the theoretical model especially if taken together with other quantities :*
  - *$J/\pi$  g.s., charge-density, single  $-$ particle levels, magnetic moments, radii... .* ●



## Data for Beta-delayed neutron precursors selected as “Standards”

Balraj Singh (McMaster University) and Daniel Abriola (IAEA-NDS), Nov 10, 2011.

At the IAEA Consultants’ meeting Oct 10-12, 2011, the following beta-delayed neutron precursors were selected as “standards” for the purpose of data evaluation and measurements:

Precursor	$J\pi$ (g.s.)	<b>Half-life (s)</b>	<b>%P(n)</b>	$Q(\beta^-)$ (keV)	$S(n)$ (keV)	$Q(\beta-n)$ (keV)
Li-9	3/2-	0.1783(4) s	50.8(2)	13606.47(11)	1664.55(8)	11941.92(9)
N-17	1/2-	4.173(4) s	95.1(7)	8679(15)	4143.08(01)	4536(15)
Br-87	(5/2-) *	55.65(13) s	2.60(4)	6818(3)	5515.17(25)	1303(3)
Br-88	(2-)	16.29(6) s	6.58(18)	8975(4)	7053.1(26)	1922(3)
Rb-94	3(-)	2.702(15) s	10.5(4)	10281(8)	6828(10)	3453(8)
Rb-95	5/2-	0.3777(8) s	8.73(20)	9229(20)	4352(9)	4877(21)
I-137	(7/2+)	24.5(2) s	7.14(23)	5877(27)	4025.53(11)	1851(27)
I-138	(2-)	6.23(3) s	5.56(22)	8070(100)SY	5663(3)	2410(100) SY

	DF3		NuBase				FRDM+GrTh		
Br87	47,7	<b>0,15</b>	/55,65	0,13	/ 0,2	0,04/	7.34507	<b>0.9975</b>	0.0025
Br88	16,55	<b>2,9</b>	/16,36	0,07	/ 6,72	0,27/	4.92517	<b>0.9864</b>	0.0136
I-137	29.28	<b>11.85</b>	/24.13	0.12	/ 7.14	0.23/	18.12382	<b>0.9734</b>	0.0266

# Conclusions

❑ *Microscopic self-consistent DF3+CQRPA approach is capable to reliably predicts beta-decay half-lives and Pn-branchings for important fission products and r-process nuclei near the closed shells.*

❑ **RESULTS :**

1. *Above the N=50, (82,126) closed shells DF+CQRPA predicts reduction of the T1/2 and Pn-values.*

2. *Sensitivity of the T1/2 and Pn-s to the g.s. J/ $\pi$  inversion.*

***Agree with recent ORNL and GSI-USC experiments for new short-lived nuclides.***

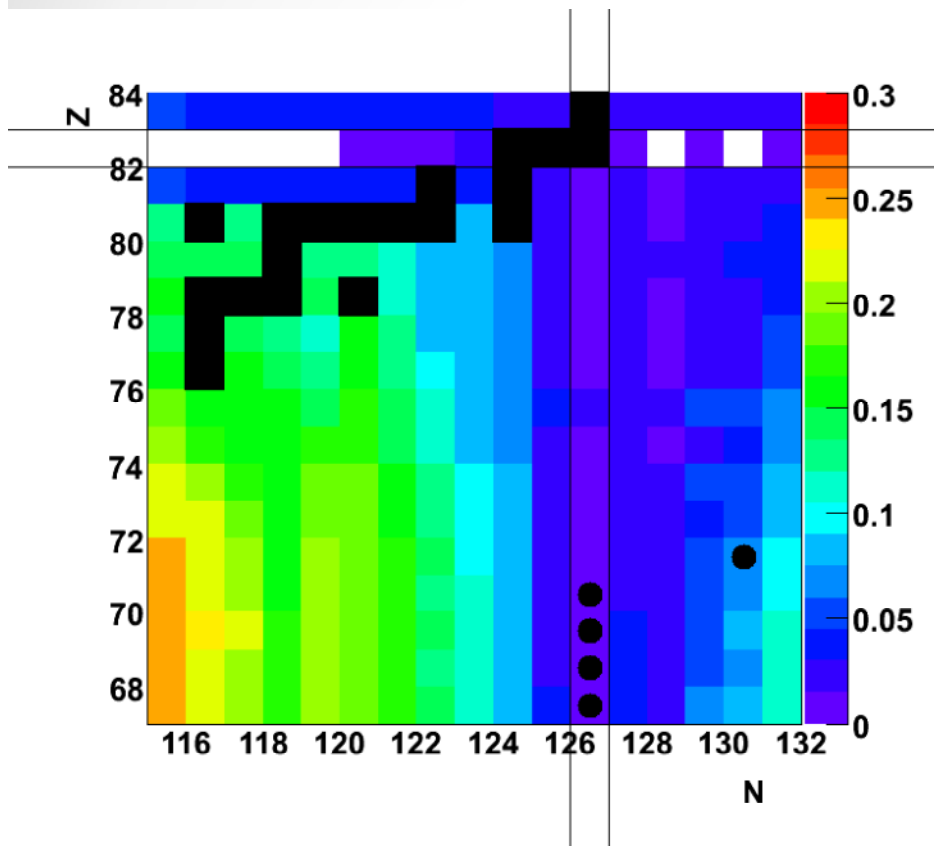
***These robust effects have to be taken care of in evaluations of beta-decay data.***

❑ *The DFT based approaches to beta-decay strength function are valuable alternative to empirical and semi-microscopical schemes.*



# Outlook

## FRDM deformation near $N=126$



- **1. Systematical calculations of the g.s. deformation and pairing properties in  $Z\sim 28$ ,  $N\sim 50$  region:**  
• **Include DF3, DF3a within HFBTHO**  
*M.V. Stoitsov, J. Dobaczewski, W. Nazarewicz, P. Ring*  
*Computer Physics Communications*  
Vol. 167, 2005, 43-63. ↓  
*Deformation effects at  $N=40-50-58$*
- **2. Detailed study of the g.s. deformation and pairing properties above  $N=126$ .** ↓  
*Deformation effects at  $N>126$*
- **3. A challenge:**  
*FAM for pnQRPA in deformed nuclei*  
*P. Avogadro, T. Nakatsukasa PRC 84,014314 (2011)*

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***New mass and beta-decay data in a wider region near @  $N \sim 50, 82, 126$   
are very important for further elaborating  
the universal nuclear energy-density functional.***