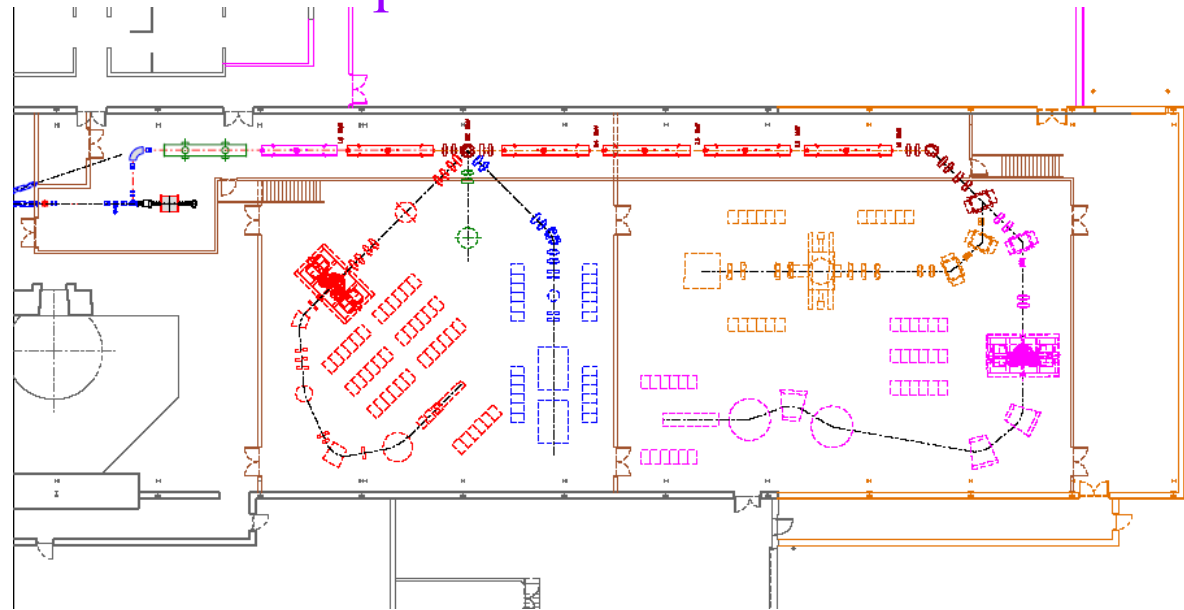




# Extracting spectroscopic factors from 40 years of (p,d) and (d,p) data



Proposed reaccelerated RI beam



USNDP  
Annual Meeting  
Nov 7-9, 2006

*Betty Tsang*

The National Superconducting  
Cyclotron Laboratory  
@Michigan State University



# The National Superconducting Cyclotron Laboratory

Michigan State University

**A national user facility for rare isotope research and education in nuclear science, astro-nuclear physics, accelerator physics, and societal applications**

**282 employees, incl. 51 undergraduate and 50 graduate students, 24 faculty**

(as of March 05)

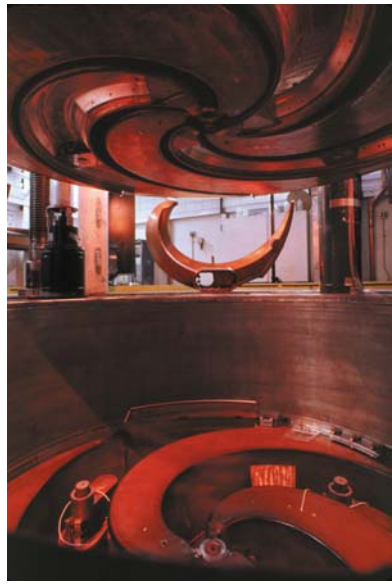
**User group of over 600 CCF users**





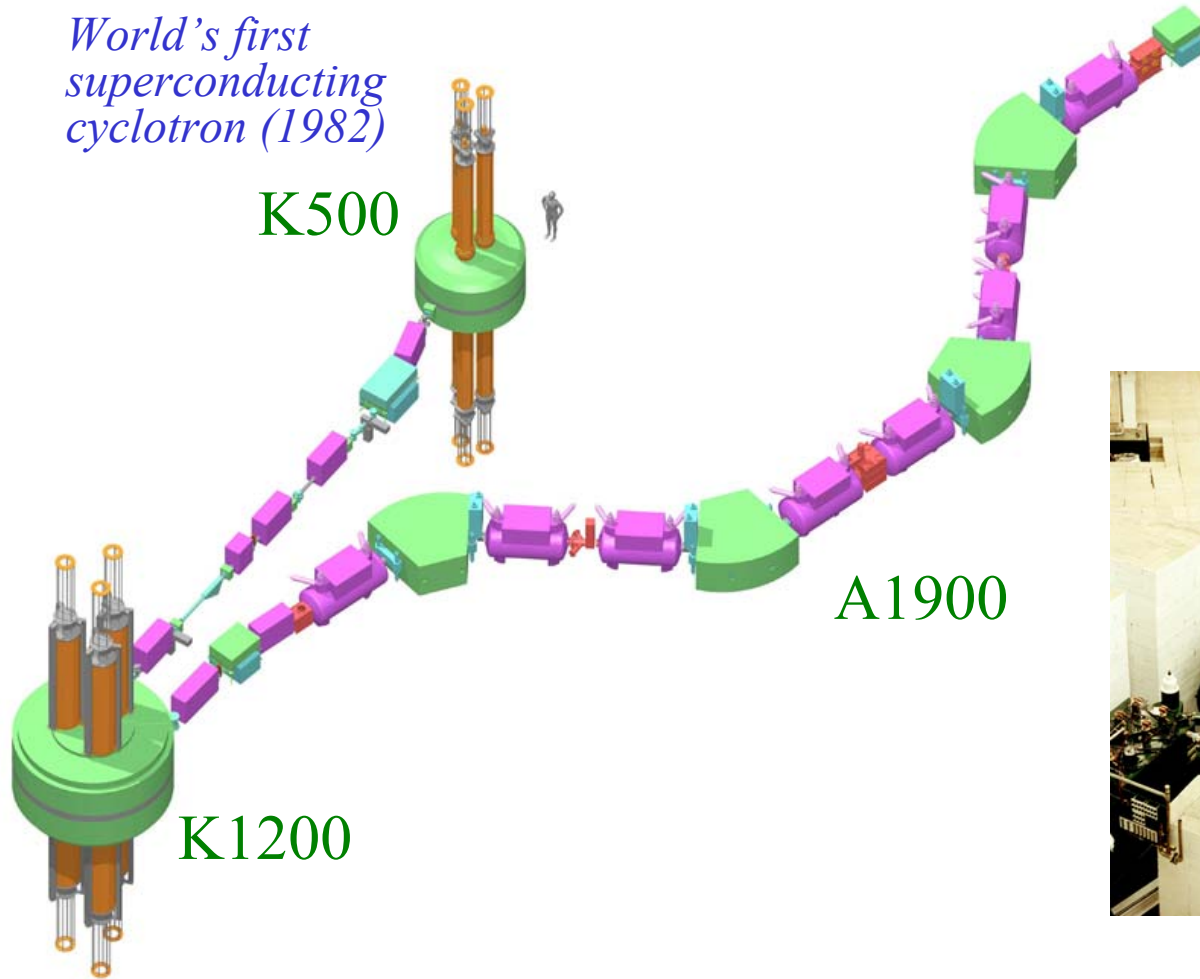
National Superconducting Cyclotron Laboratory

# Coupled Cyclotron Facility (2000)



*World's first  
superconducting  
cyclotron (1982)*

K500



A1900

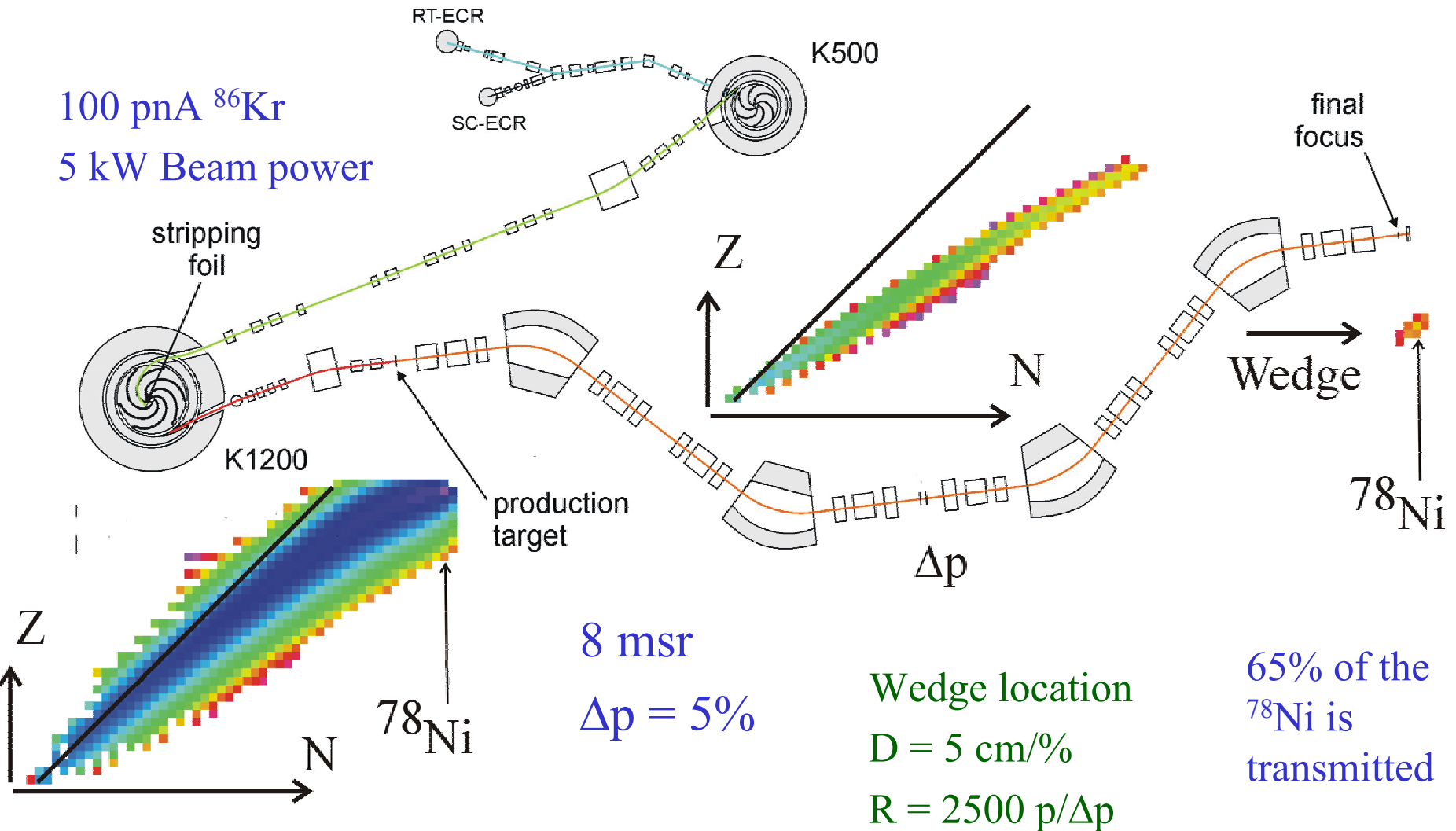
K1200

*World's most  
powerful  
superconducting  
cyclotron (1989)*



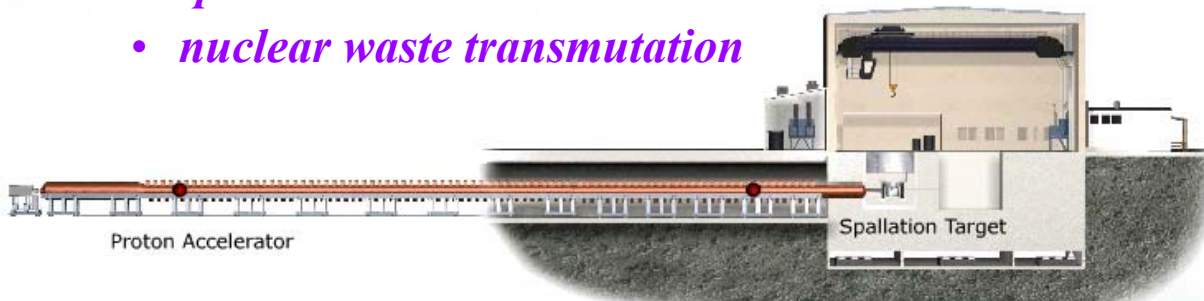
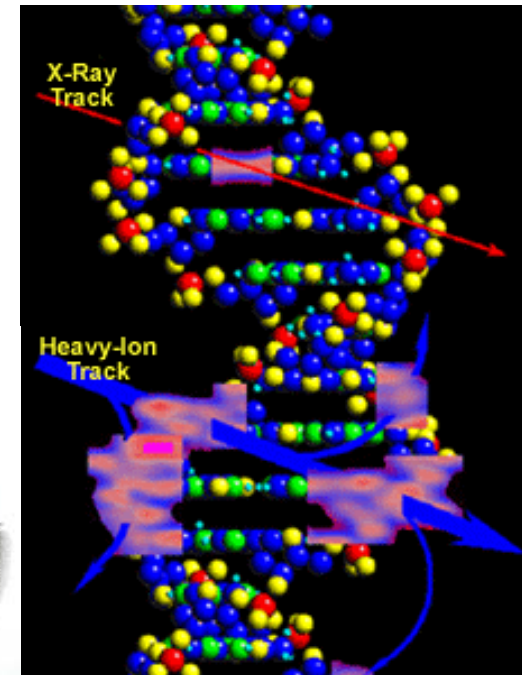
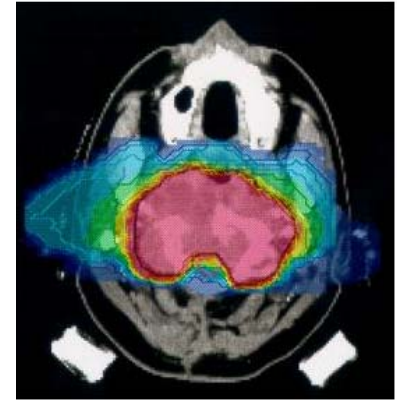
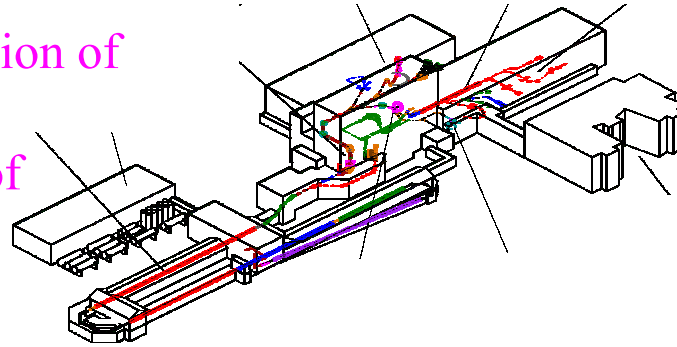
# Example Fragment Separation Technique (NSCL)

100 pA  $^{86}\text{Kr}$   
5 kW Beam power

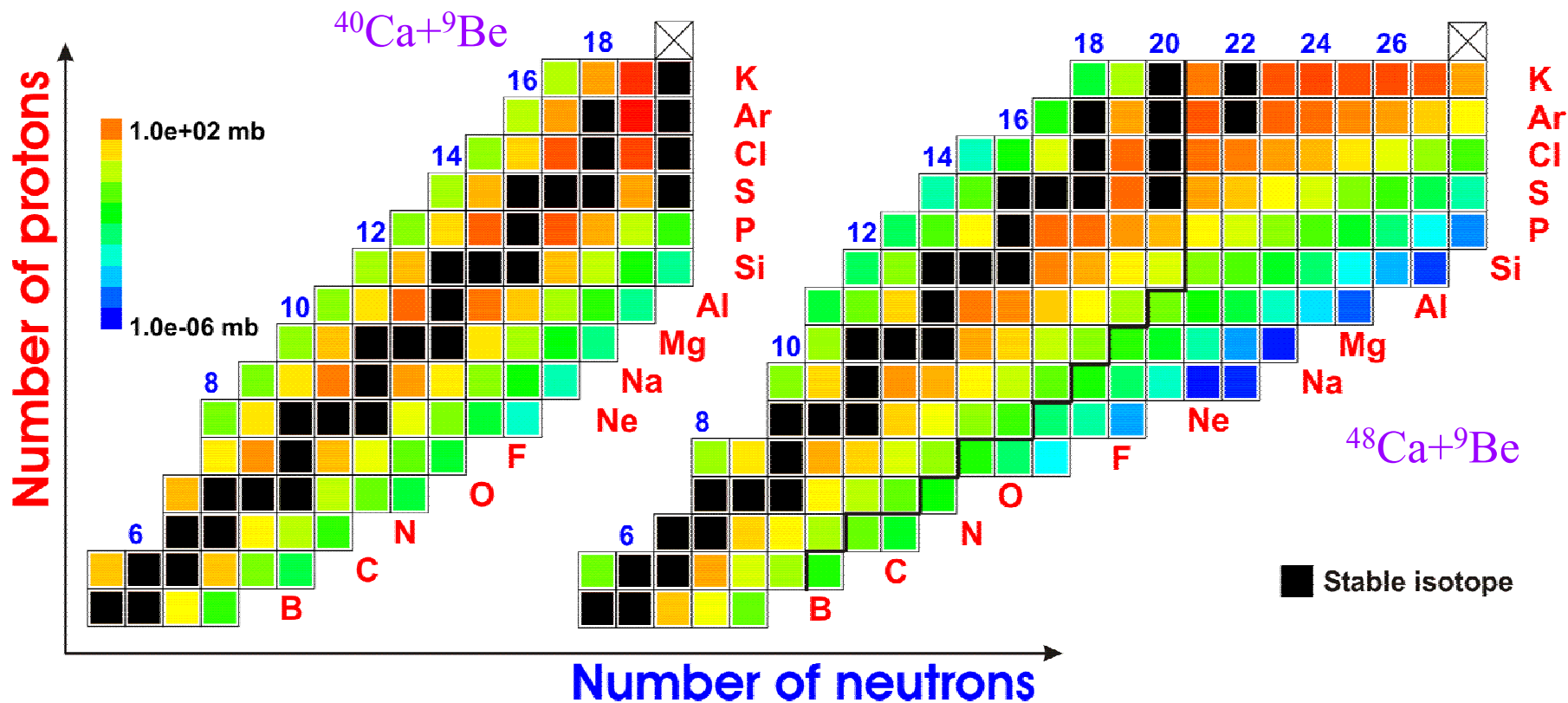


# Projectile Fragmentation

- Fundamental science
  - Mechanism in the production of rare isotopes
  - study of basic properties of atomic nuclei
- Applications
  - Benchmark data needed to test simulation code.
    - *Beam rate estimates for RI beam facilities*
    - *Design high power accelerators*
    - *tumor treatment*
    - *space radiation*
    - *nuclear waste transmutation*



# Rare Isotope Production (Mocko thesis & PRC, in press)

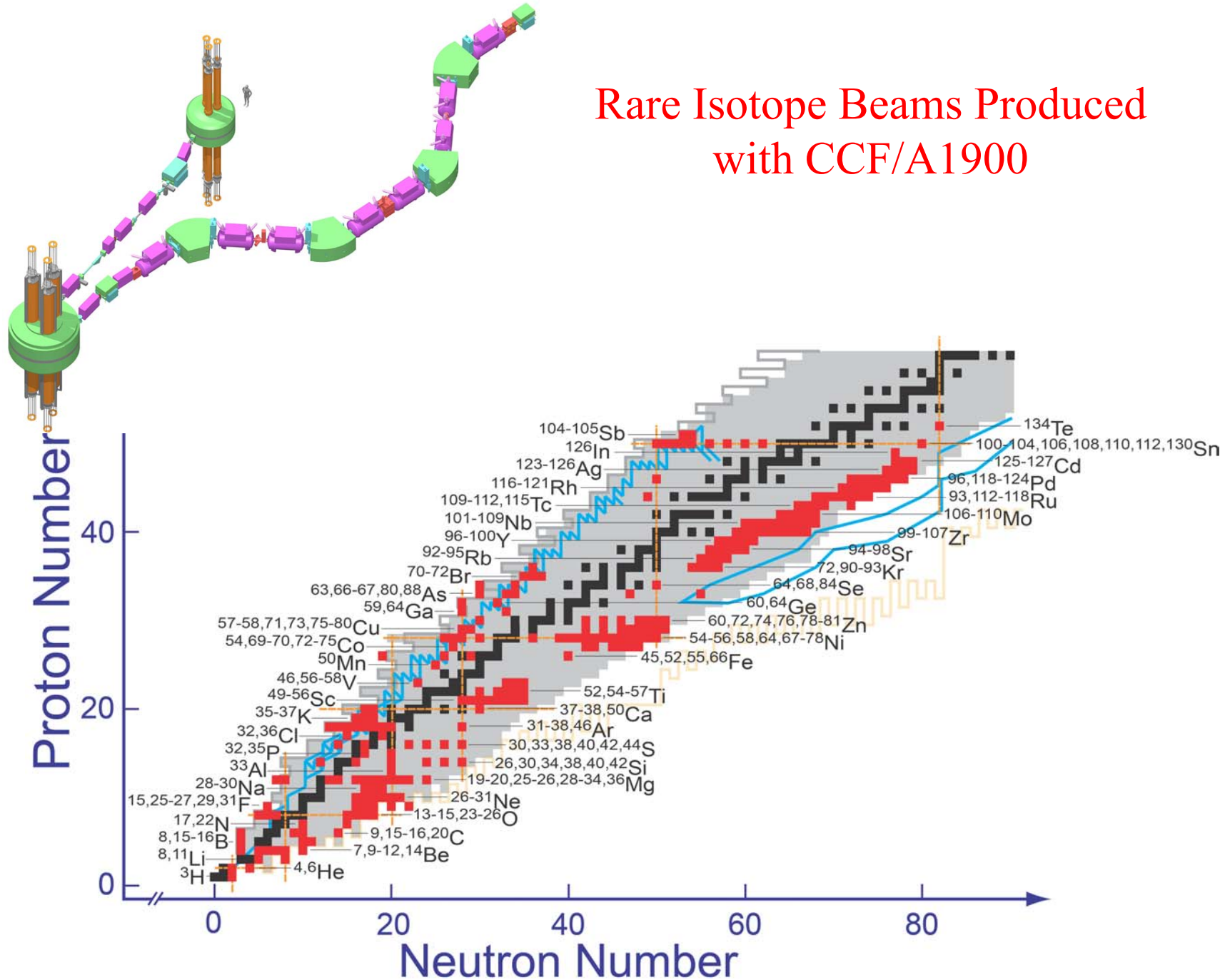


- *Nearly 2X more isotopes are produced in fragmentation of  $^{48}\text{Ca}$  than  $^{40}\text{Ca}$ .*
- *Primary beams:  $^{40,48}\text{Ca}$ ,  $^{58,64}\text{Ni}$  and unstable  $^{68}\text{Ni}$  and  $^{69}\text{Cu}$  beams.*
- *Data reveal deficiencies of EPAX parameterization.*
- *Improvement on theoretical understanding of the RI production mechanisms.*

NNDC data base for “fragmentation data”

Publication of cross-sections (Nuclear Data Sheets)

# Rare Isotope Beams Produced with CCF/A1900



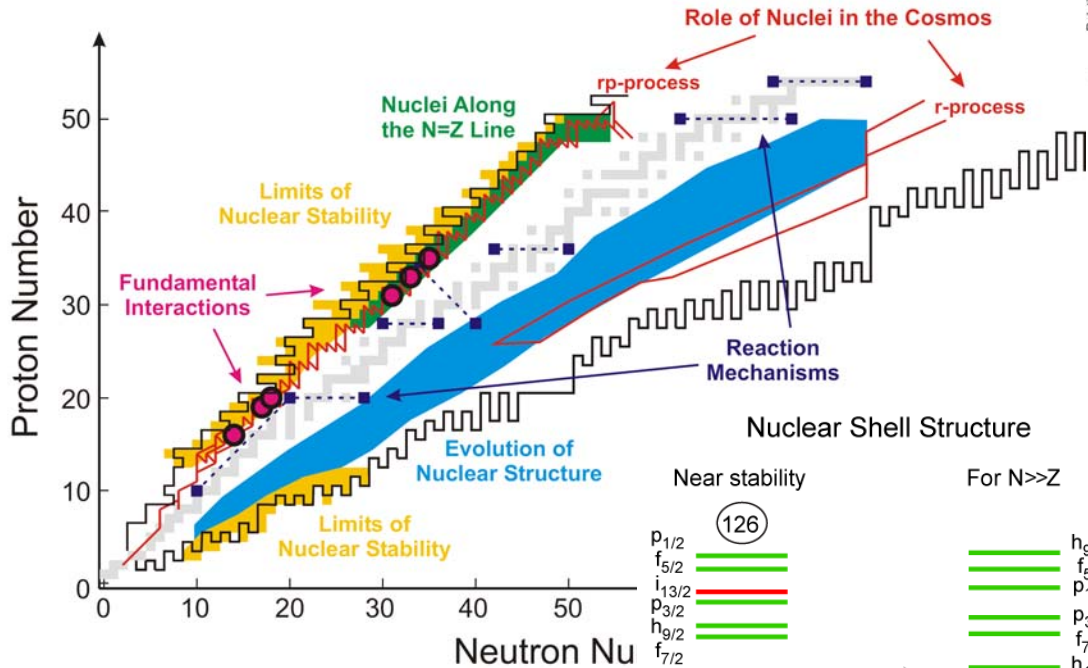
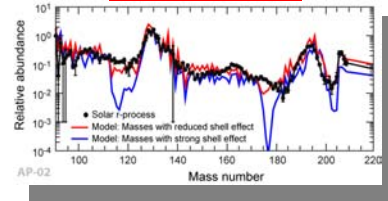
# Nuclear Science at the NSCL



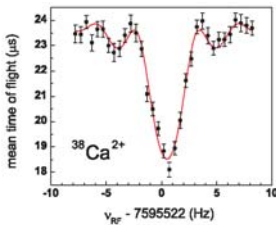
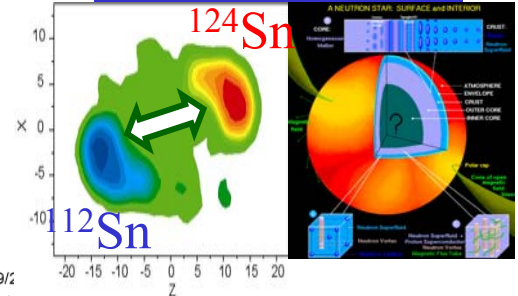
**Where are the limits of nuclear stability?**

**Properties N~Z nuclei  
r-p process**

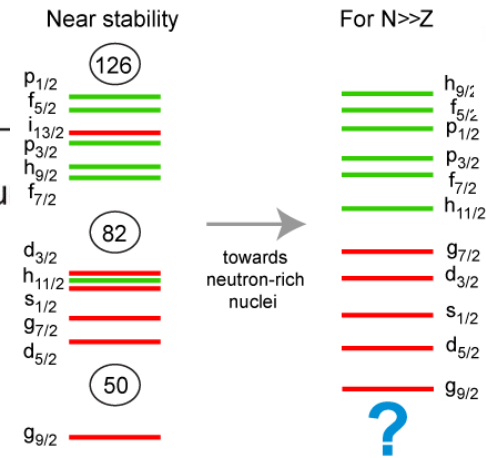
**r-process**



**EOS of n-rich matter**



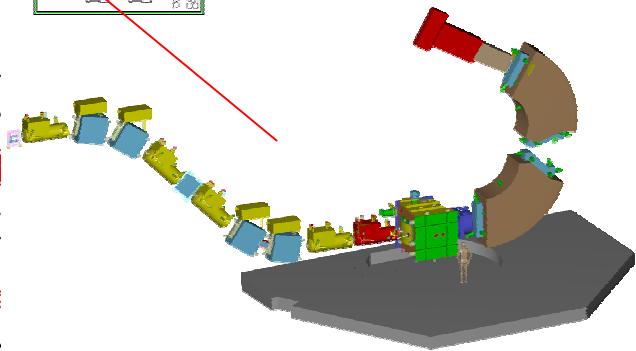
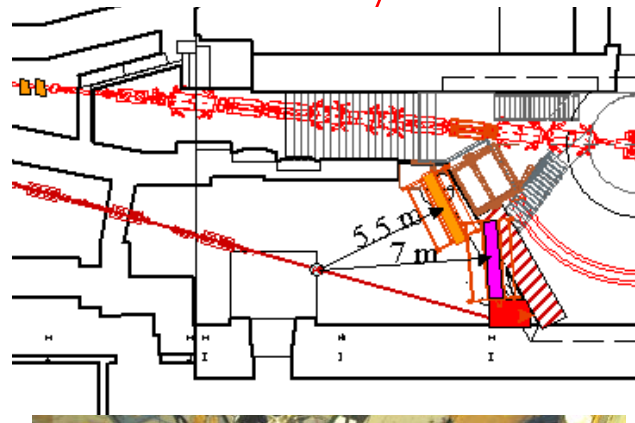
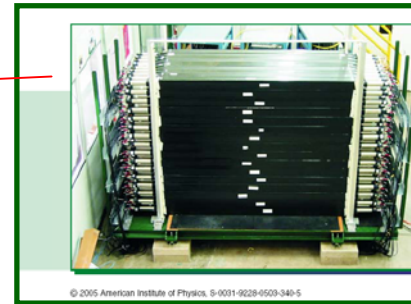
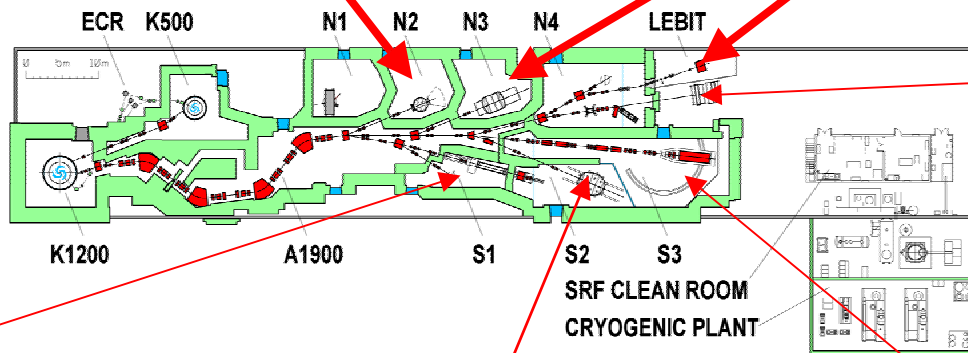
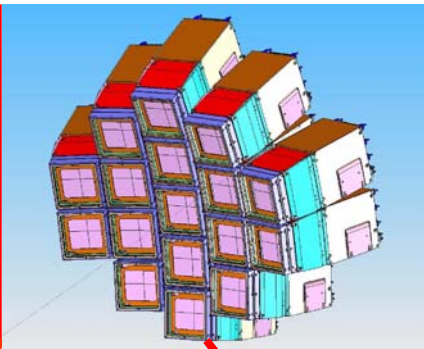
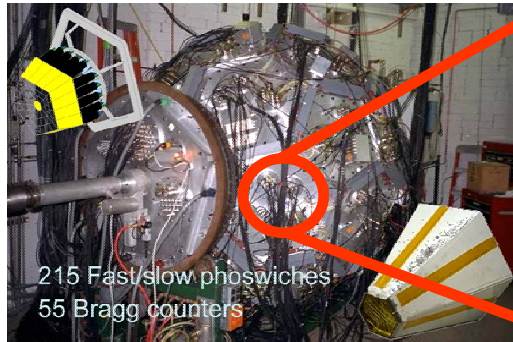
**Is there physics beyond the standard model?  
Mass measurements**



- Mean field near stability
- Strong spin-orbit term
- Mean field for N>>Z?
- Reduced spin-orbit
- Diffuse density
- Tensor force

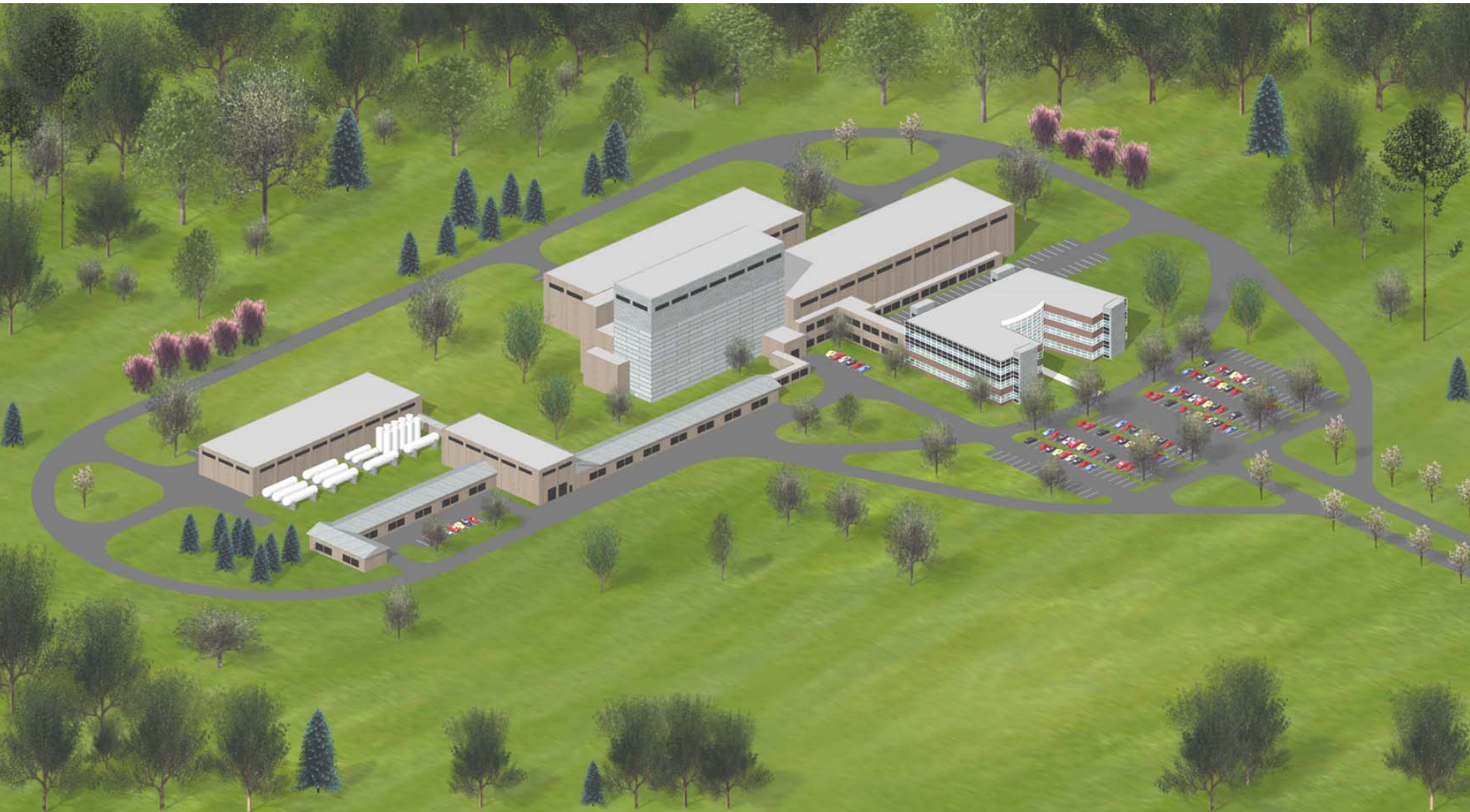


# Experimental Areas at NSCL



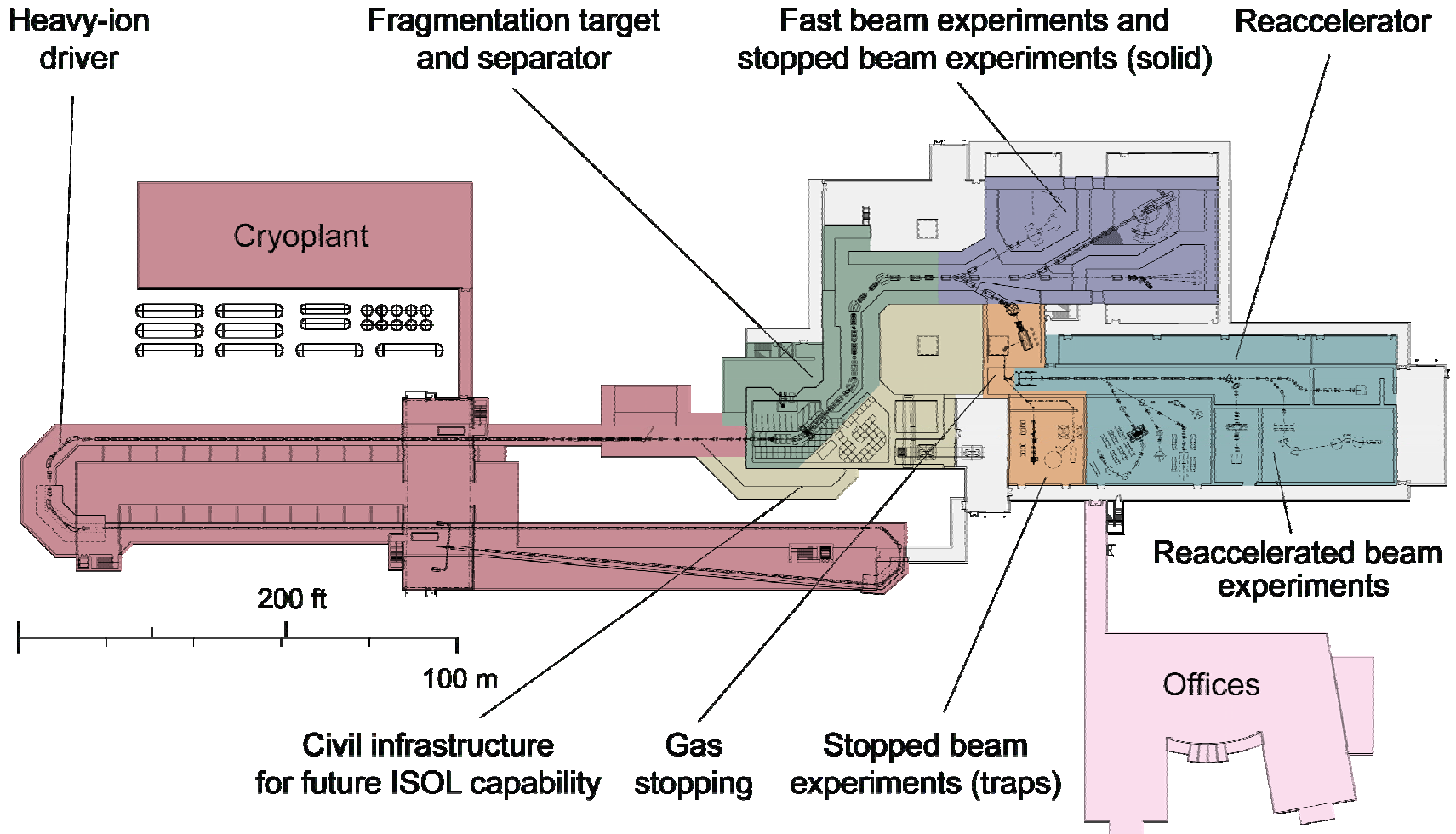
# ***ISOTOPE SCIENCE FACILITY AT MSU***

## ***Developing Plans for the Future (10-Year Horizon)***



# ISF@MSU

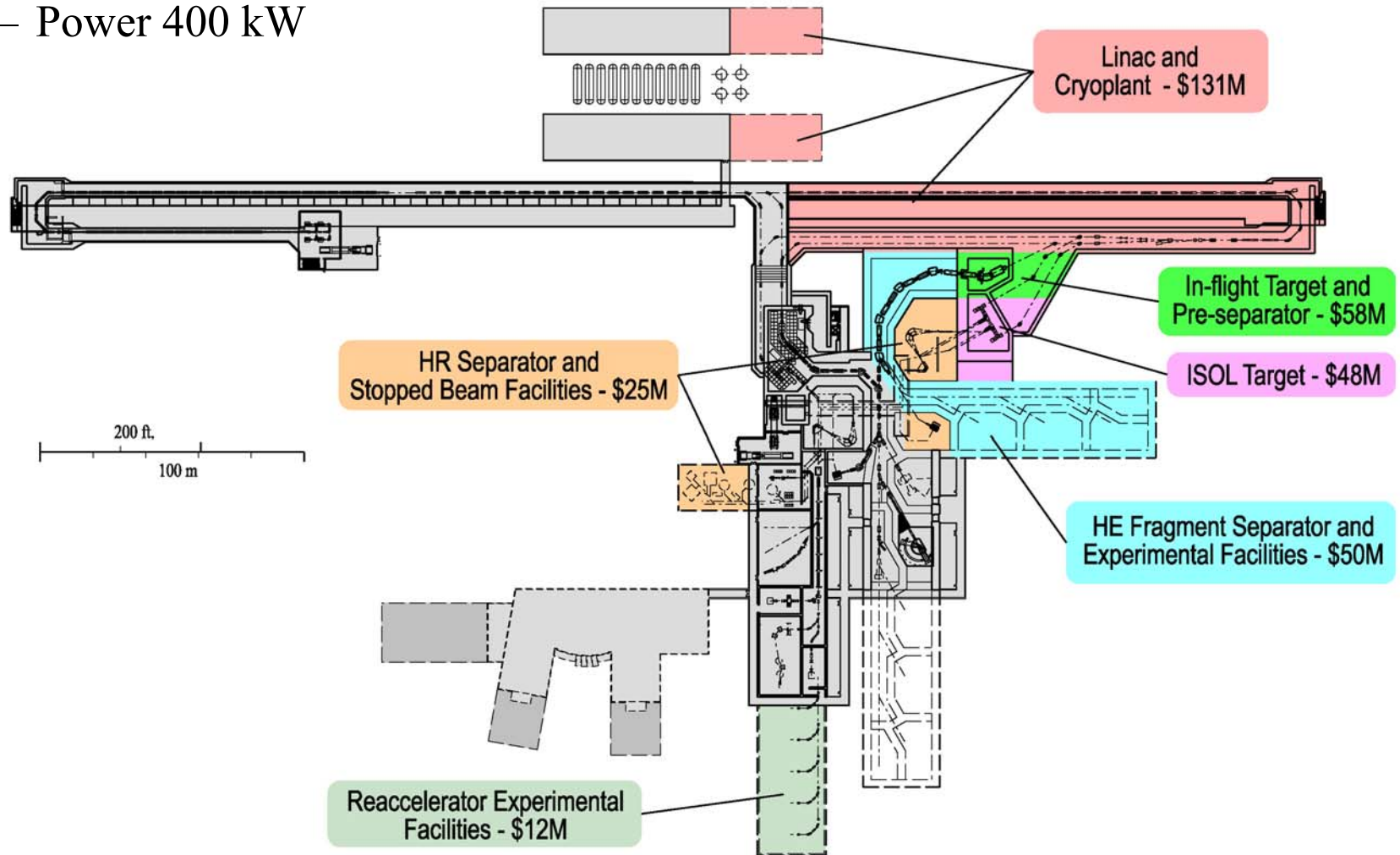
*Large intensity gains (factors of 100-100,000) over current capability  
rare isotope beams with energies between 0 and 200 MeV/nucleon*



# ISF Upgrade Options

## Modular, expandable capacity to meet future science needs

- Multi-user capability, flexible science-driven selection of upgrade elements
  - Energy/nucleon: 400 MeV  $^{238}\text{U}$ , 539 MeV  $^{129}\text{Xe}$ , 864 MeV  $^3\text{He}$ , 1122 MeV  $^1\text{H}$
  - Power 400 kW





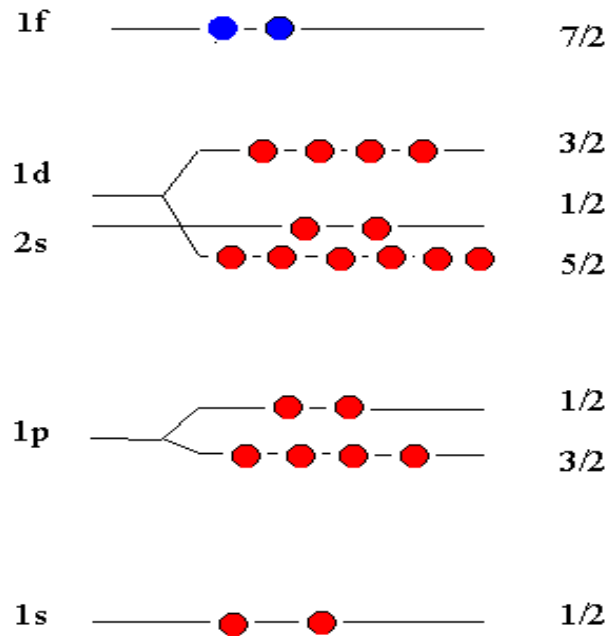
# Extracting spectroscopic factors from 40 years of (p,d) and (d,p) data

## Magic number

N=20

N=8

N=2



$^{42}\text{Ca}$

Spectroscopic Factors:  
measure the single  
particle nature of the  
valence nucleons.

# Properties of Single Particle

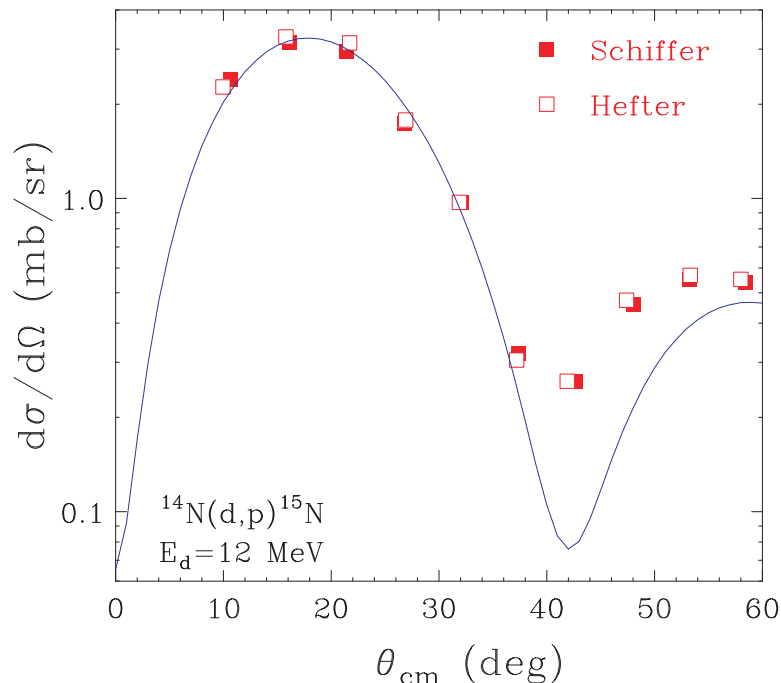
Experimental SF :

$$S_{gs} = \frac{\left(\frac{d\sigma}{d\Omega}\right)_{EX}}{\left(\frac{d\sigma}{d\Omega}\right)_{RM}}$$

⇒ **Spectroscopic factor(SF)**

measures the orbital configuration of the valence nucleons.

Independent Particle Model (IPM), SF represents how good can we describe the nucleus as a single particle plus a core.



$$\frac{S_{\text{exp}}}{S_{IPM}} = 1$$

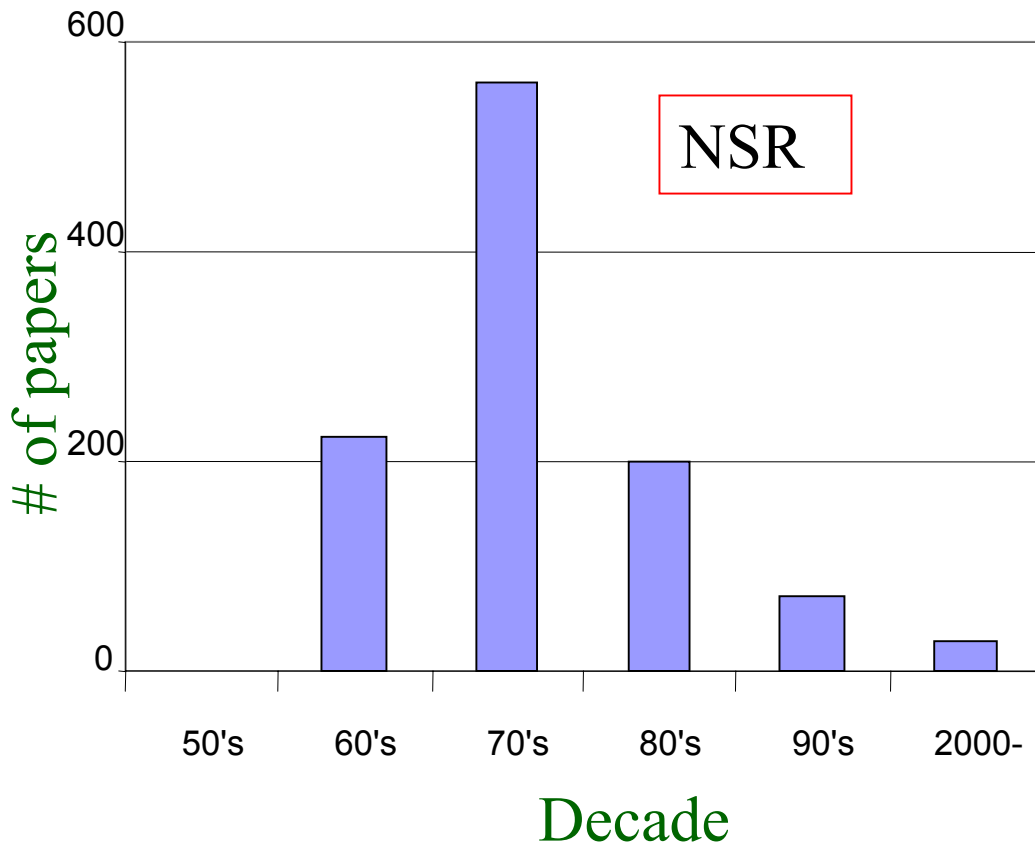
Orbital description is accurate

$$\frac{S_{\text{exp}}}{S_{IPM}} < 1$$

Valence nucleon occupies more than one orbit  
→ LBSM.

# Spectroscopic Studies from (p,d) & (d,p) transfer reactions

*SF is one of the important properties to understand the structure of the rare nuclei.*



## Pros:

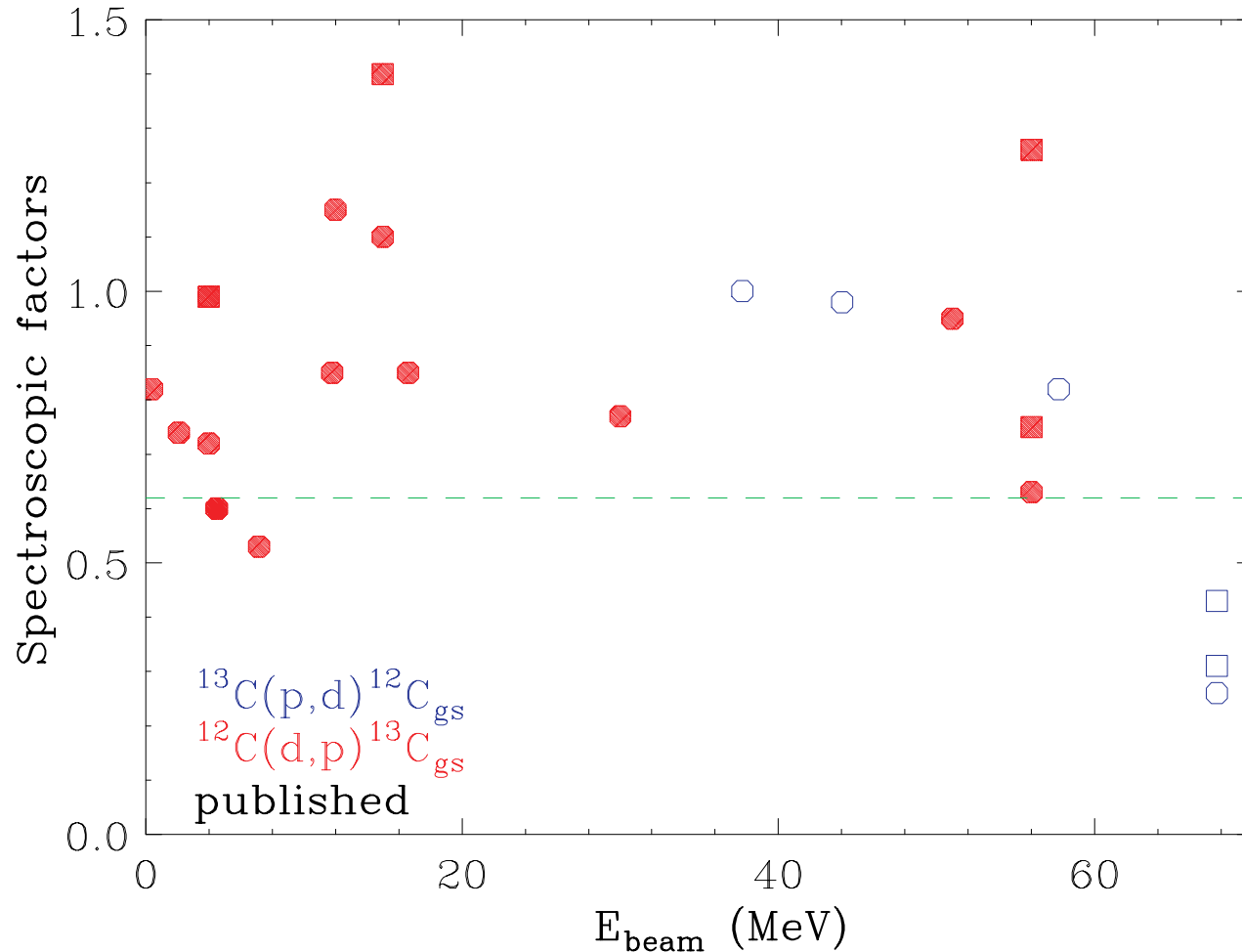
- ✓ We know the exact state of the nucleon transferred.
- ✓ Good understanding of the experimental technique and reaction theory (DWBA) & beyond
- ✓ Lots of data from past 40 years (NSR).

## Cons:

- ✗ Do we measure the “absolute” spectroscopic factors?
- ✗ Data appear to give inconsistent results

# Spectroscopic Factors from literatures

Example:  $1p_{1/2}$  neutron SF in  $^{13}\text{C} = ^{12}\text{C}+n$

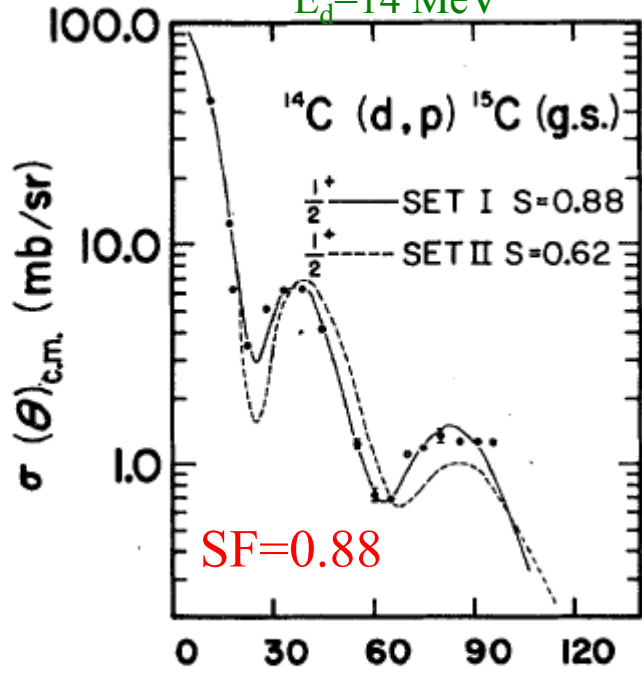


- *Published spectroscopic factors show large fluctuations from analysis to analysis*

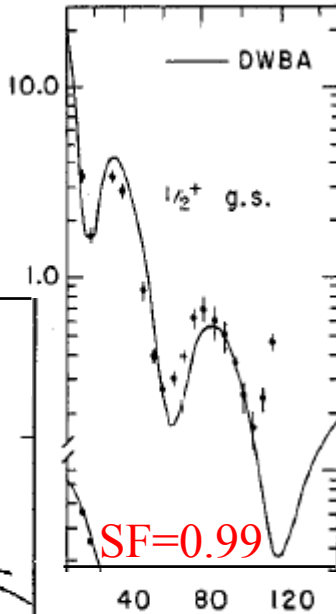


# $^{14}\text{C}(d,p)^{15}\text{C}$

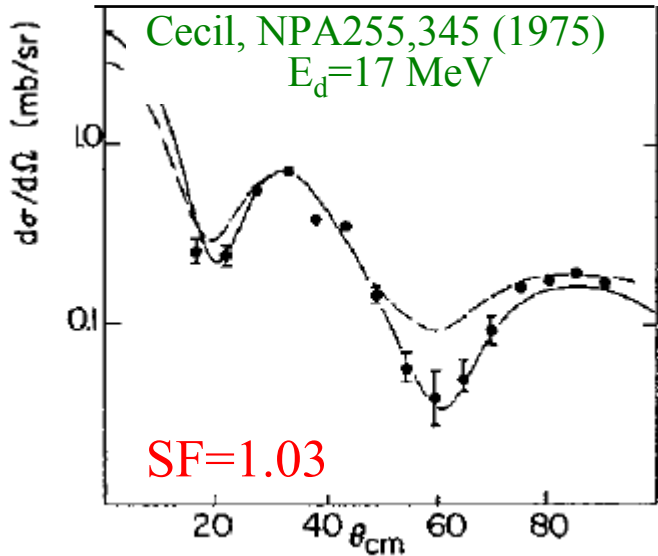
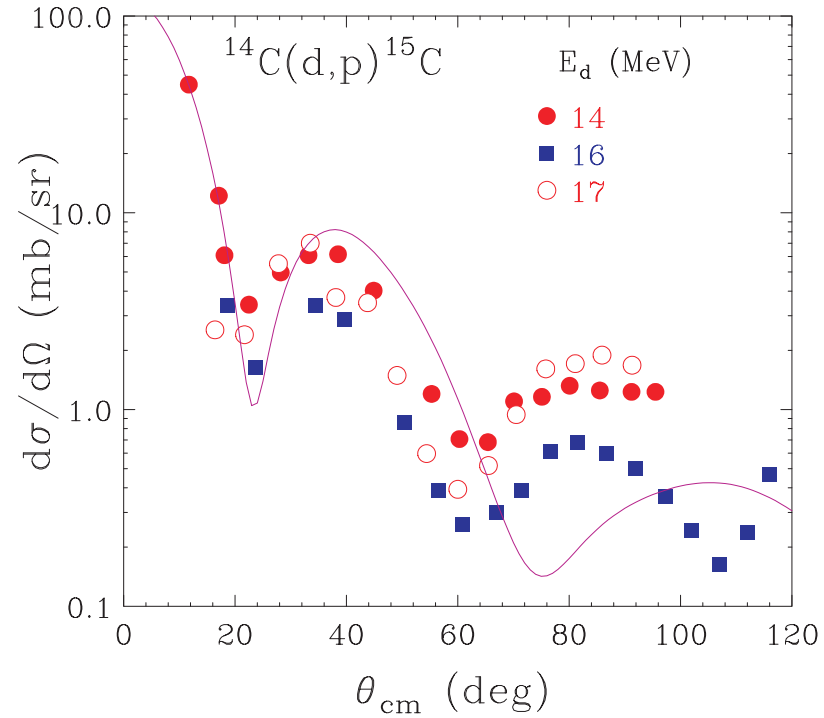
Goss, PRC12,1730 (1975)  
 $E_d=14\text{ MeV}$



$E_d=16\text{ MeV}$



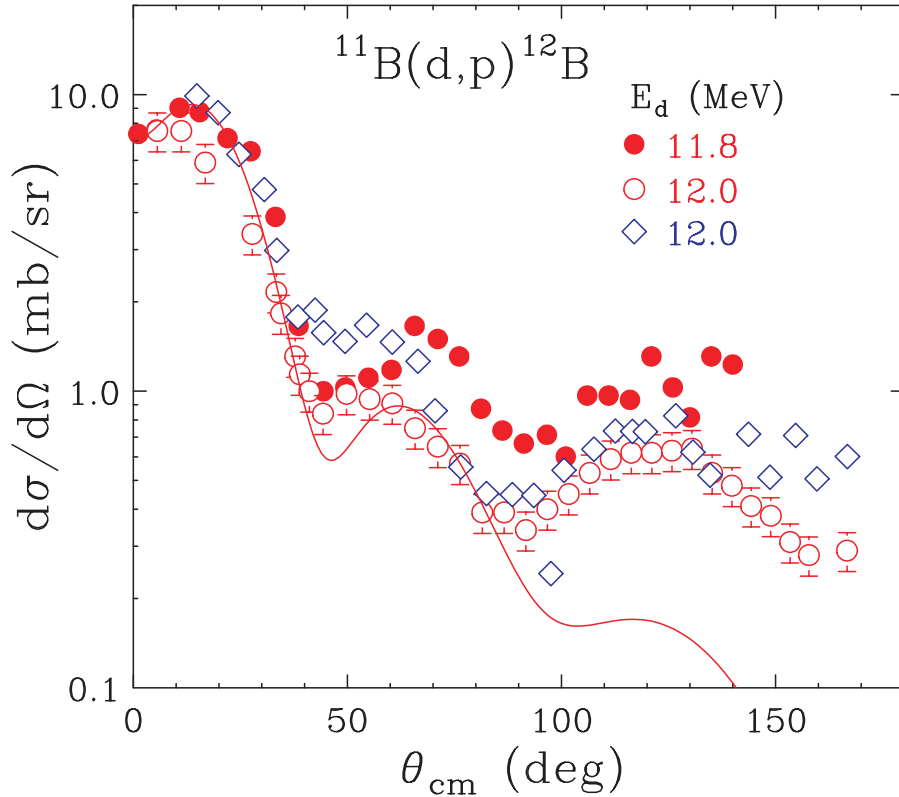
Murillo,  
NPA579,  
125 (1994)



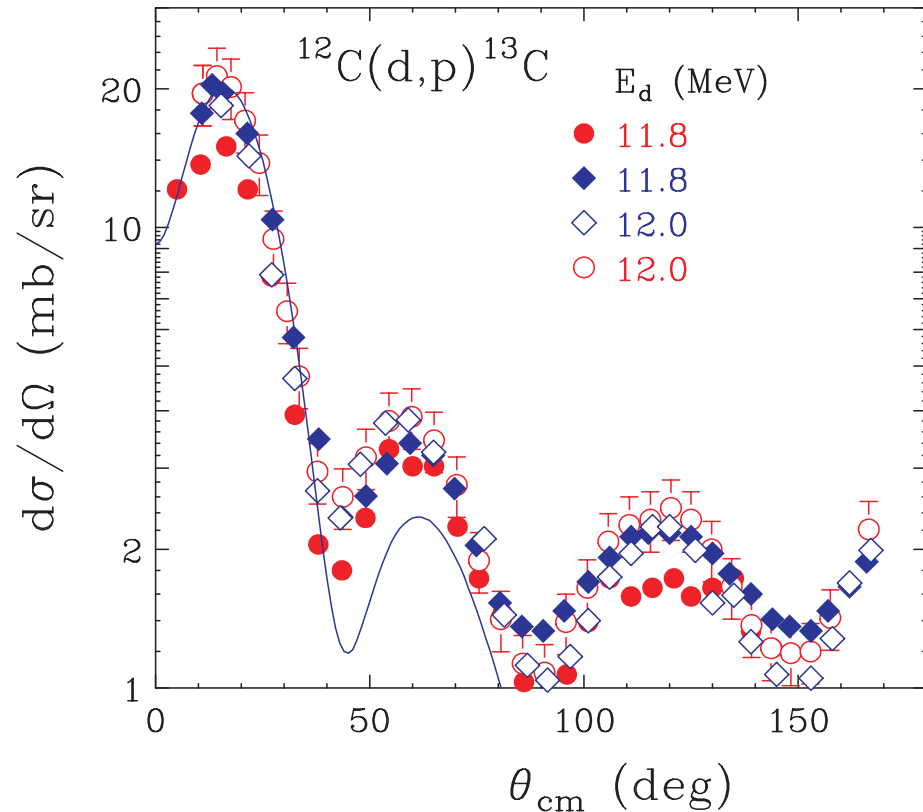
*The data differ by factor of 2 but SF's are nearly the same by varying the input parameters!!*

# Discrepancies between data sets

*Quoted experimental uncertainties are 6-20%*



J. P. Schiffer et al., Phys. Rev. 164, 1274 (1967).  
Z. H. Liu et al., Phys. Rev. C 64, 034312 (2001).  
D. Fick, J. NUK, 19, 693 (1974) (EXFOR).



J. P. Schiffer et al., Phys. Rev. 164, 1274 (1967).  
Z. H. Liu et al., Phys. Rev. C 64, 034312 (2001).  
J. Lang et al., Nucl. Phys. A477, 77 (1988).  
U. Schmidt-Rohr et al., Nucl. Phys. 53, 77 (1964).

Quality control from independent measurements

# TWOFNR (Tostevin)

*Soper-Johnson  
Adiabatic*

*Approximation to take  
care of d-break-up  
effects.*

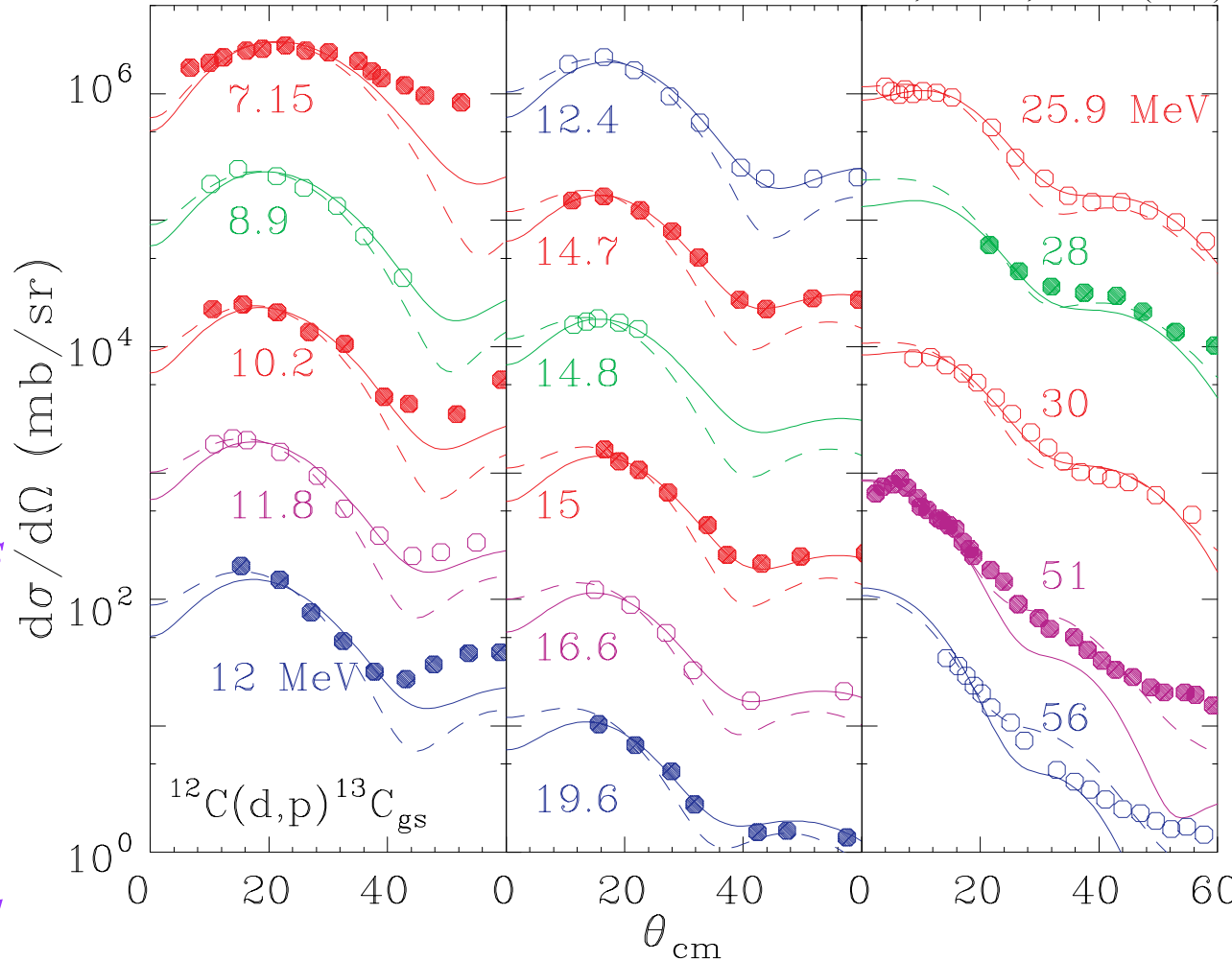
*Use global p and n  
optical potential with  
standardized parameters  
(CH89)*

*n-potential : Woods-  
Saxon shape  $r_o=1.25$  fm  
&  $a_o=0.65$ ; depth  
adjusted to experimental  
binding energy.*

*Include finite range &  
non-locality corrections*



Liu et al, PRC **69**, 064313 (2004)



SF=0.75±0.10; SF(SM) = 0.62

Apply the technique to a large data set

# Ground state n-spectroscopic factors for 80 nuclei

Tsang et al, PRL **95**, 222501 (2005)

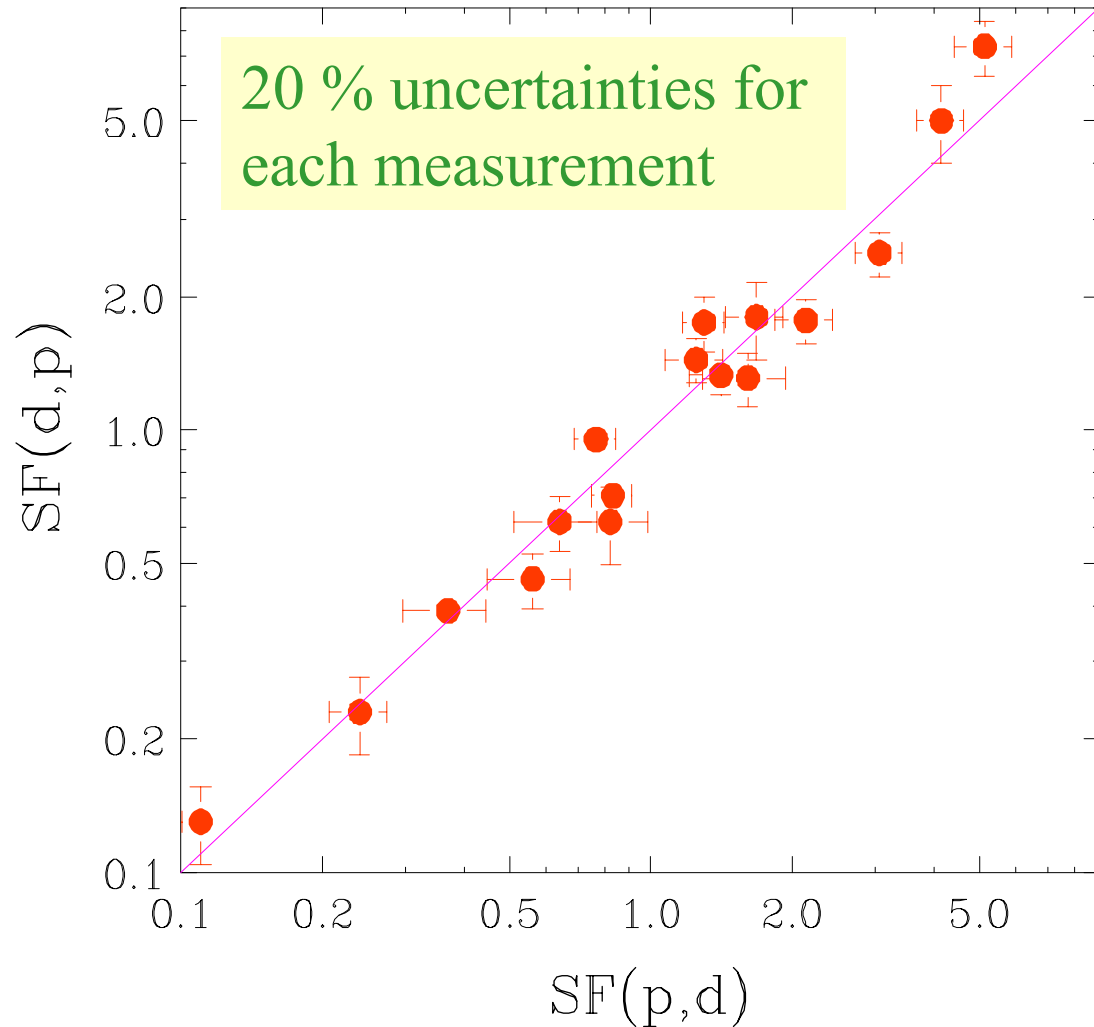
Z=3	Li	6, 7, 8, 9
Z=4	Be	9, 10, 11
Z=5	B	10, 11, 12
Z=6	C	12, 13, 14, 15
Z=7	N	14, 15, 16
Z=8	O	16, 17, 18, 19
Z=9	F	19, 20
Z=10	Ne	21, 22, 23
Z=11	Na	24
Z=12	Mg	24, 25, 26, 27
Z=13	Al	27, 28
Z=14	Si	28, 29, 30, 31
Z=15	P	32
Z=16	S	32, 33, 34, 35, 37
Z=17	Cl	35, 36, 37, 38
Z=18	Ar	36, 37, 38, 39, 40
Z=19	K	39, 40, 41, 42
Z=20	Ca	40, 41, 42, 43, 44, 45, 47, 48, 49
Z=21	Sc	45, 46
Z=22	Ti	46, 47, 48, 49, 50, 51
Z=23	V	51
Z=24	Cr	50, 51, 52, 53, 55

*Jenny Lee, 2004*  
*SURE student*

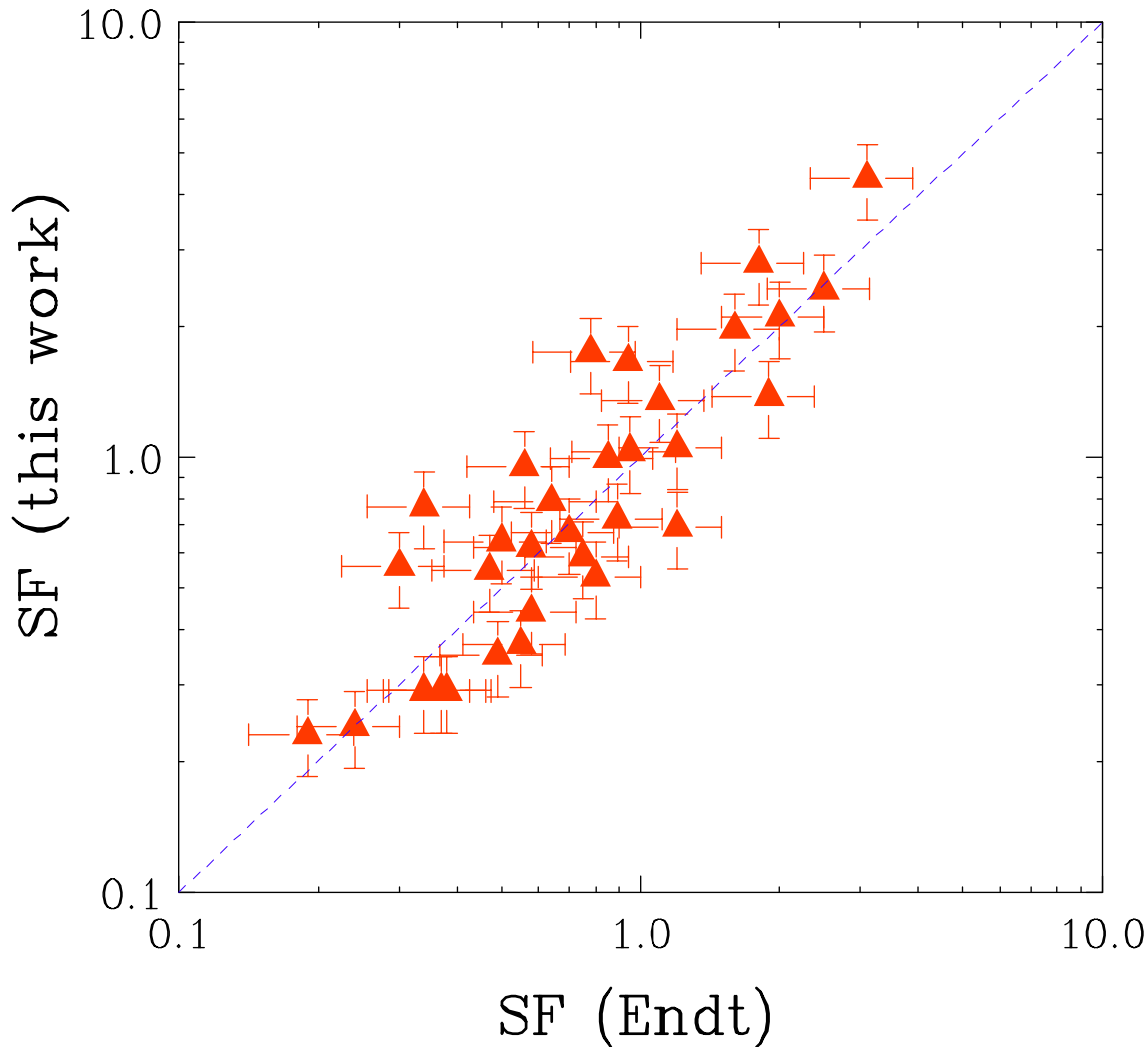
# Quality Control ?

80 nuclei from Li to Cr ( $\sim 430$  angular distributions)

$S_n$	80 nuclei
(p,d) : $S_+$	47 nuclei
(d,p) : $S_-$	56 nuclei
(p,d) & (d,p)	18 nuclei
$A+p \rightarrow B+d$	$S_+$
$B+d \rightarrow A+p$	$S_-$
Equivalent processes $S_+ = S_-$	
18 nuclei	
$\Rightarrow$ Self consistency checks	
$\Rightarrow$ Assign uncertainties	



# Comparison with Endt's (Atomic Data and Nuclear Tables 19, 23 (1977)) best SF values in A=21-44 region



## Endt's SF:

✓ uncertainty : **25% [(p,d), (d,p), (d,t), (<sup>3</sup>He, α)]**

**50 % for (d,p) and (p,d) reactions only**

✓ removal of normalization uncertainties

✓ mainly based on communication with authors

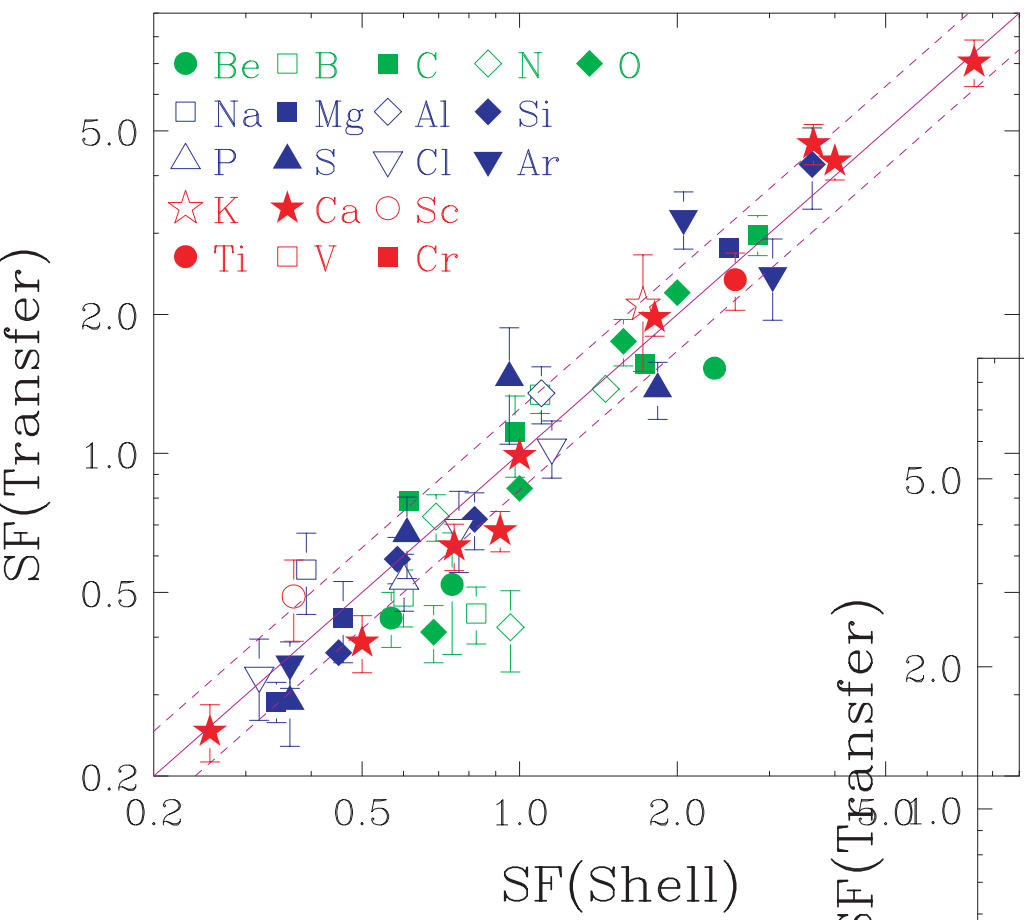
## Our SF :

✓ uncertainty : < 20 %

✓ re-analysis by consistent method and parameters

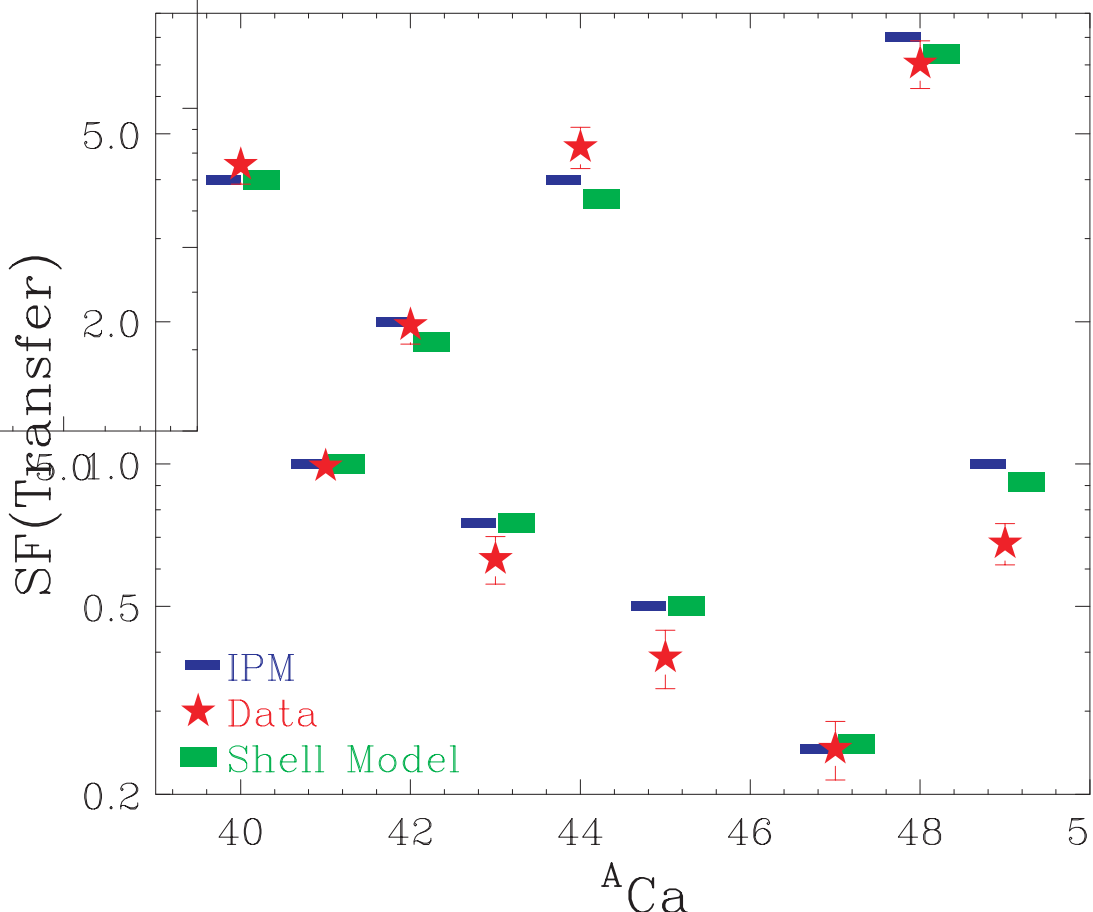
✓ can be applied to other data.

# Compare with LB-Shell Model (Oxbash, B.A. Brown)



*Austern's values were predicted 40 years ago*

*Good agreement with most isotopes*

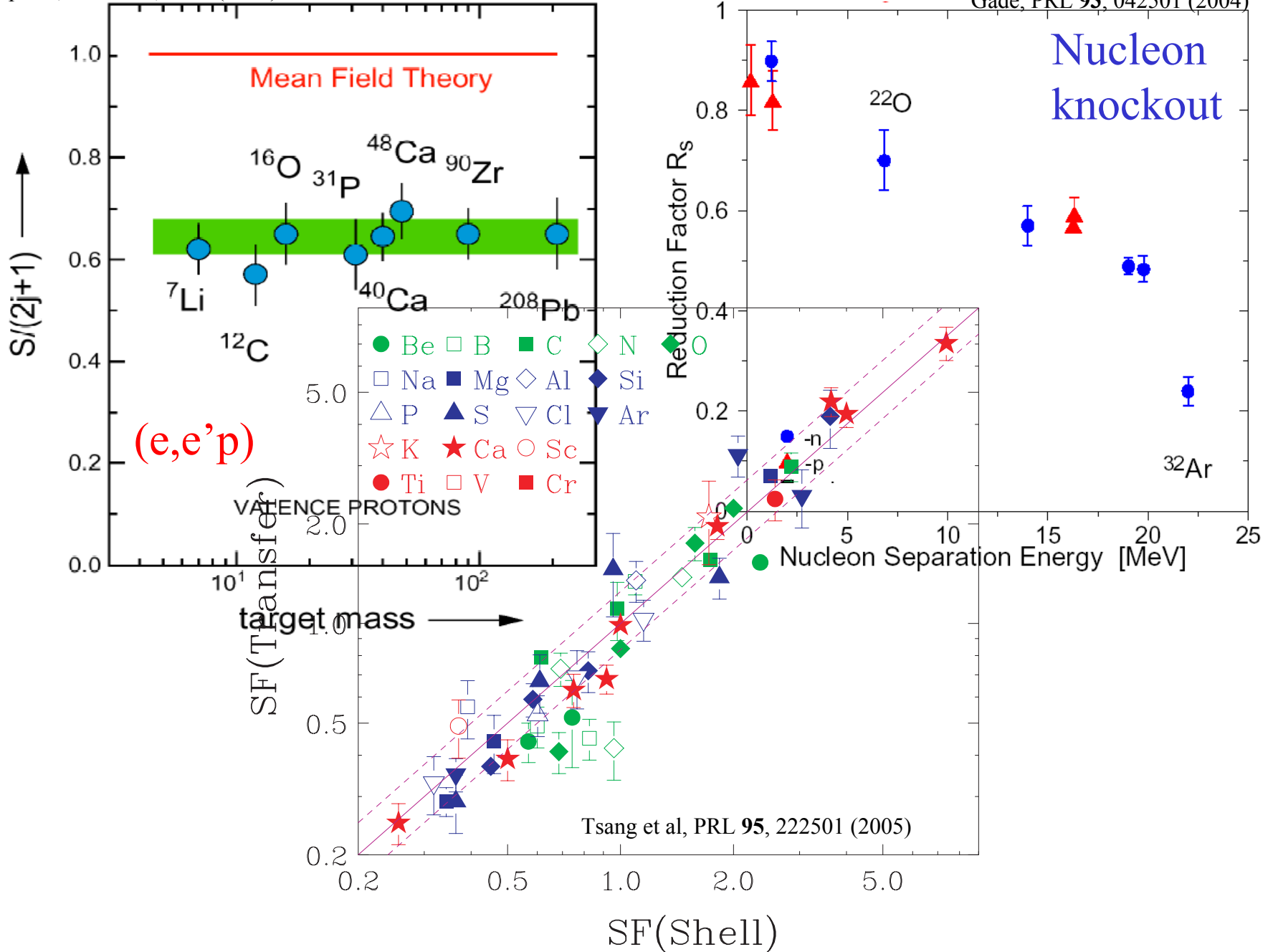


M.B. Tsang, et al, PRL95, 222501 (2005).

# Measurements of Spectroscopic Factors

Lapikas, NPA **553**, 297c (1993)

Gade, PRL **93**, 042501 (2004)

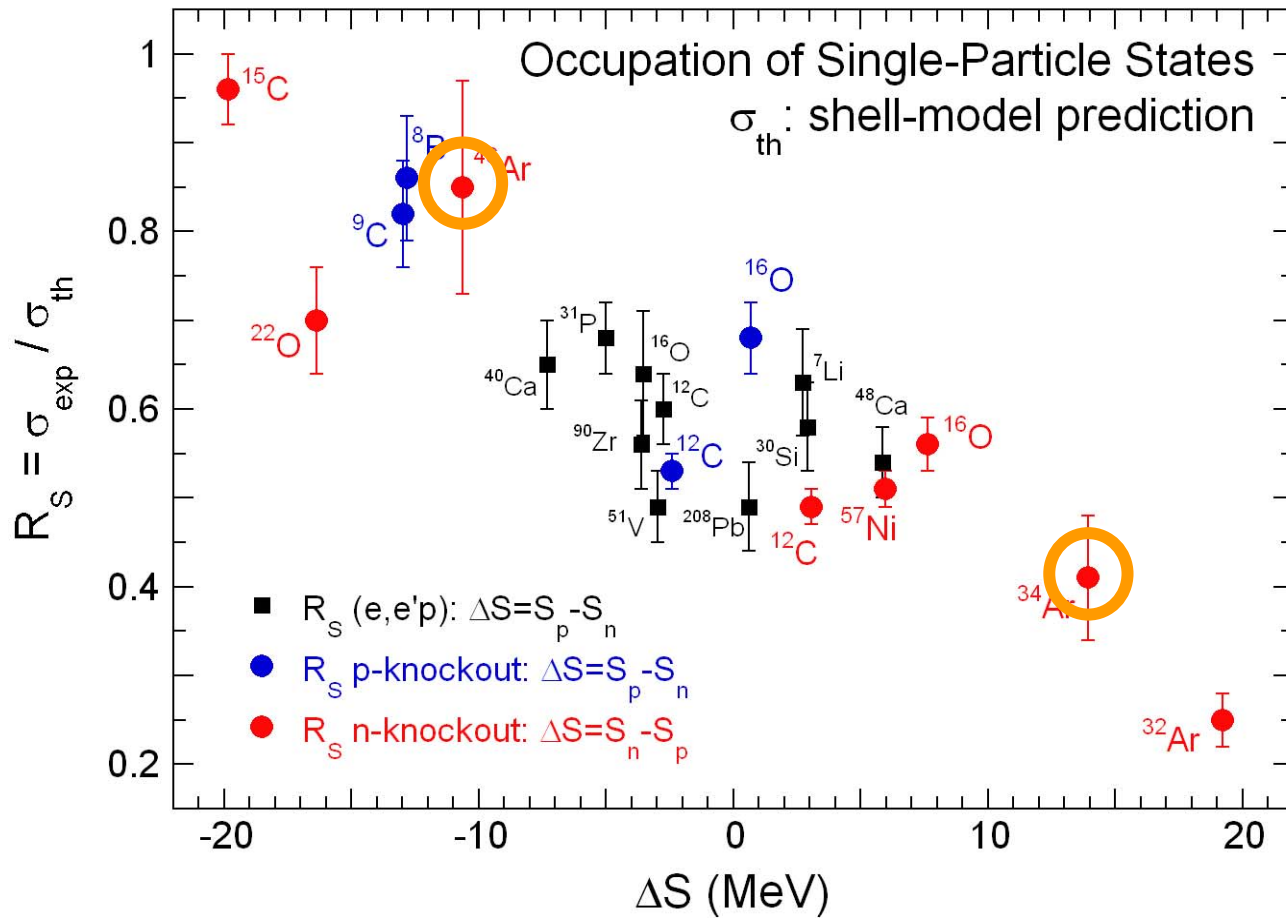




# Measurements of Spectroscopic Factors

*SF values and trends should be the same independent of measurement methods, i.e. (e,e'p), nucleon knockout and transfer reactions should give same SF values.*

Lee, PRC73, 044608 (2006); Gade, PRL 93, 042501 (2004)



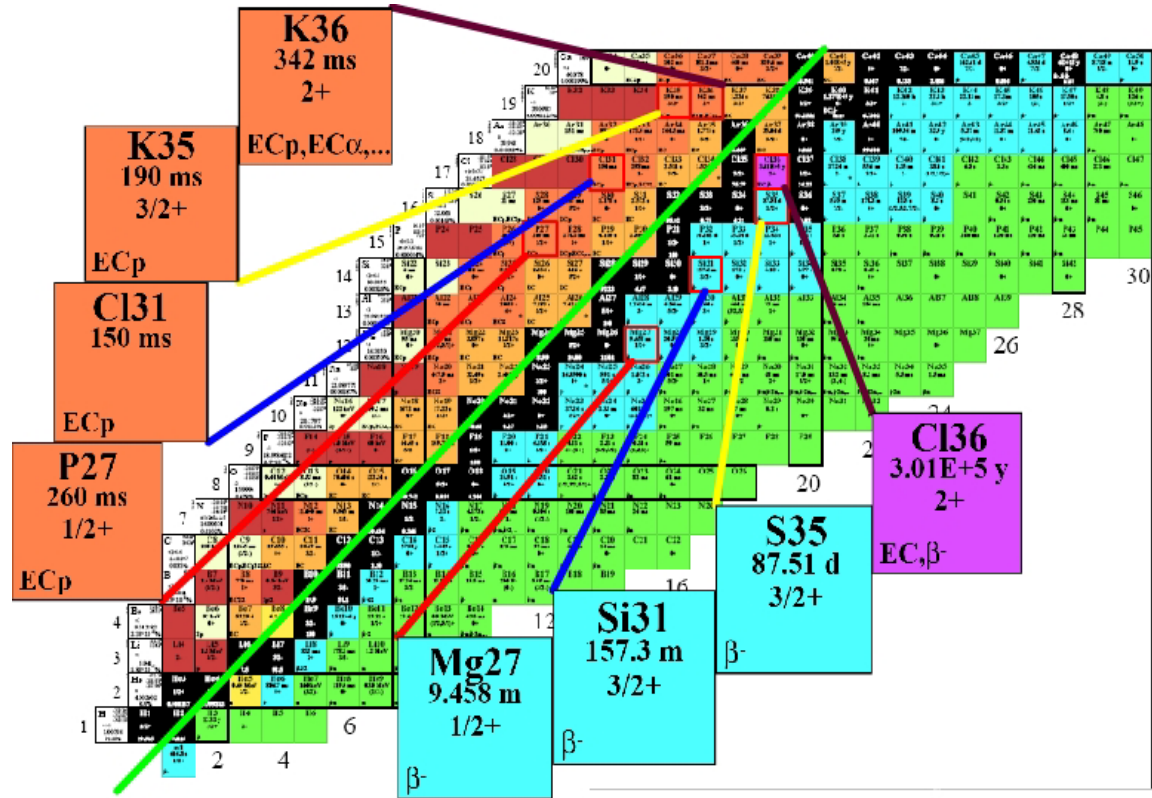
Approved experiments : p( $^{46}\text{Ar}$ , d) $^{45}\text{Ar}$ ; p( $^{34}\text{Ar}$ , d) $^{33}\text{Ar}$  – to study possible quenching effects in strong and weakly bound neutrons in rare isotopes.

# SF's of excited states for $^{27}\text{Mg}$ , $^{30}\text{Si}$ , $^{31}\text{Si}$ , $^{35}\text{S}$ & $^{36}\text{Cl}$

- The (unstable) mirror nuclei  $^{27}\text{P}$ ,  $^{30}\text{S}$ ,  $^{31}\text{Cl}$ ,  $^{35}\text{K}$  &  $^{36}\text{K}$  are of astrophysical importance in nucleosynthesis processes.
- no experimental (SF) data exist so reaction rates (and energy levels) rely on shell model calculations.

• Important to establish the accuracies of these calculations by comparing SF data to predictions.

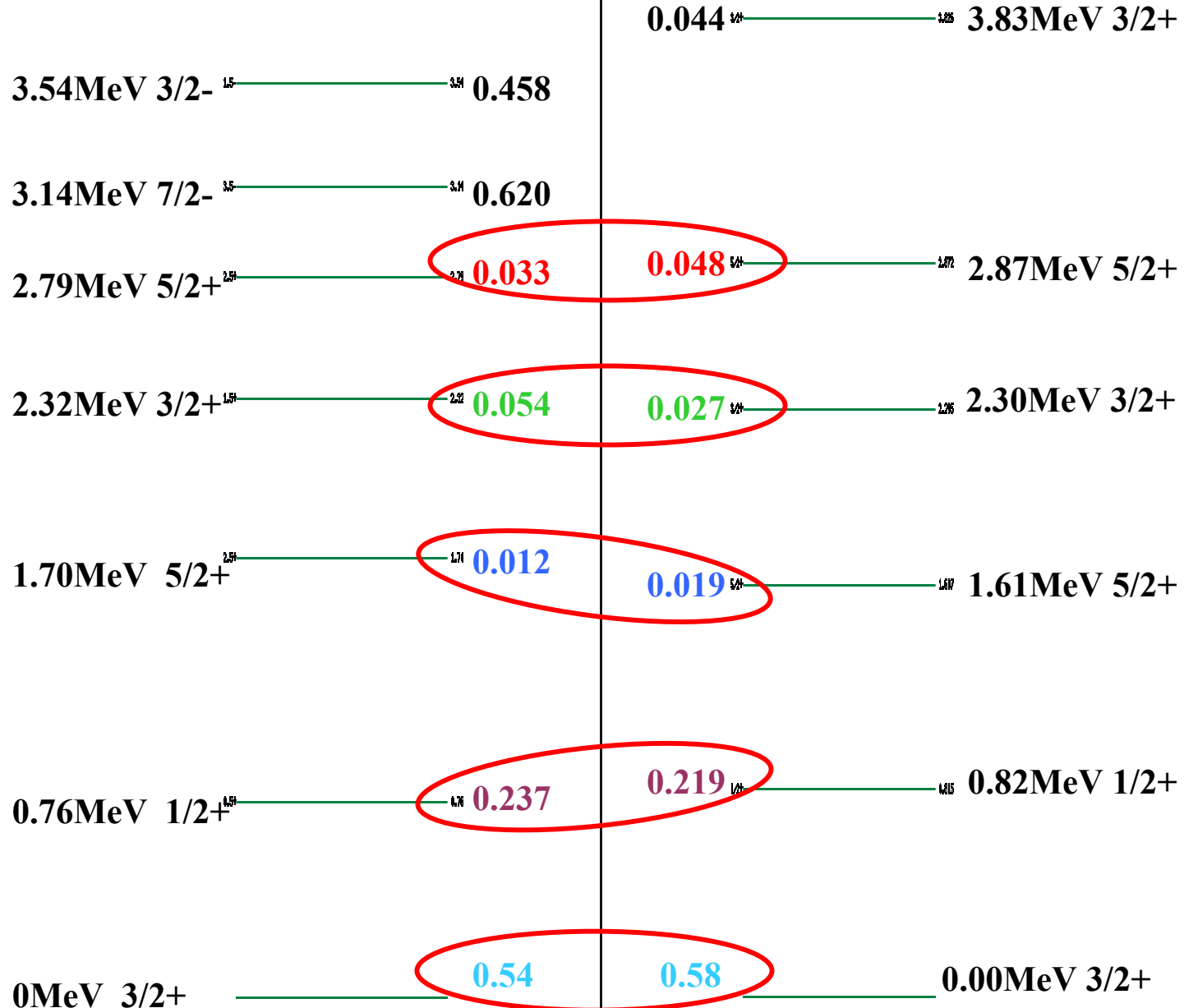
*Shi Chun Su, 2006*  
*SURE student*



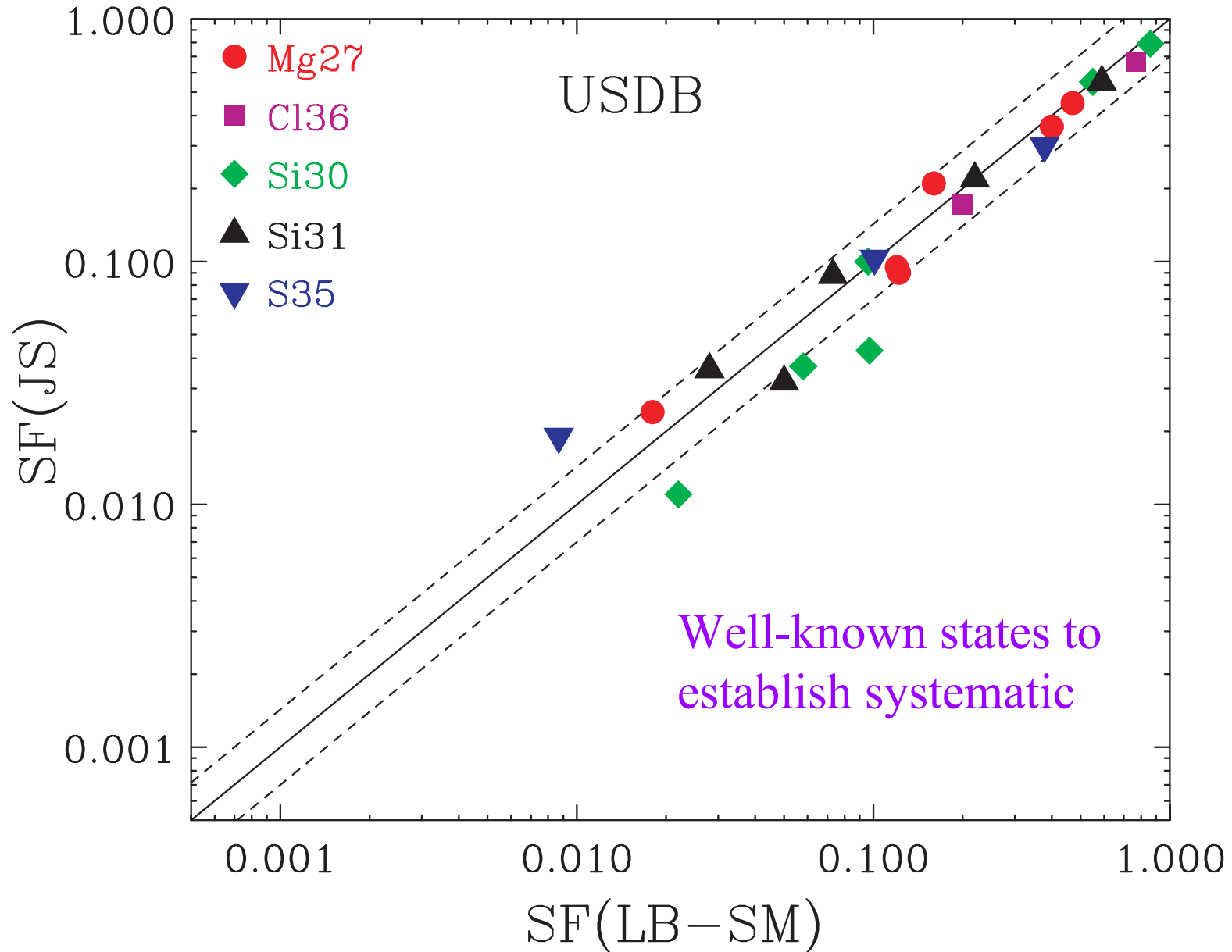
# $^{31}\text{Si}$ (mirror nuclei: $^{31}\text{Cl}$ ) $T=3/2$ $S_n=6.587$ MeV

Experiment:  $^{31}\text{Si}$  (NUDAT)

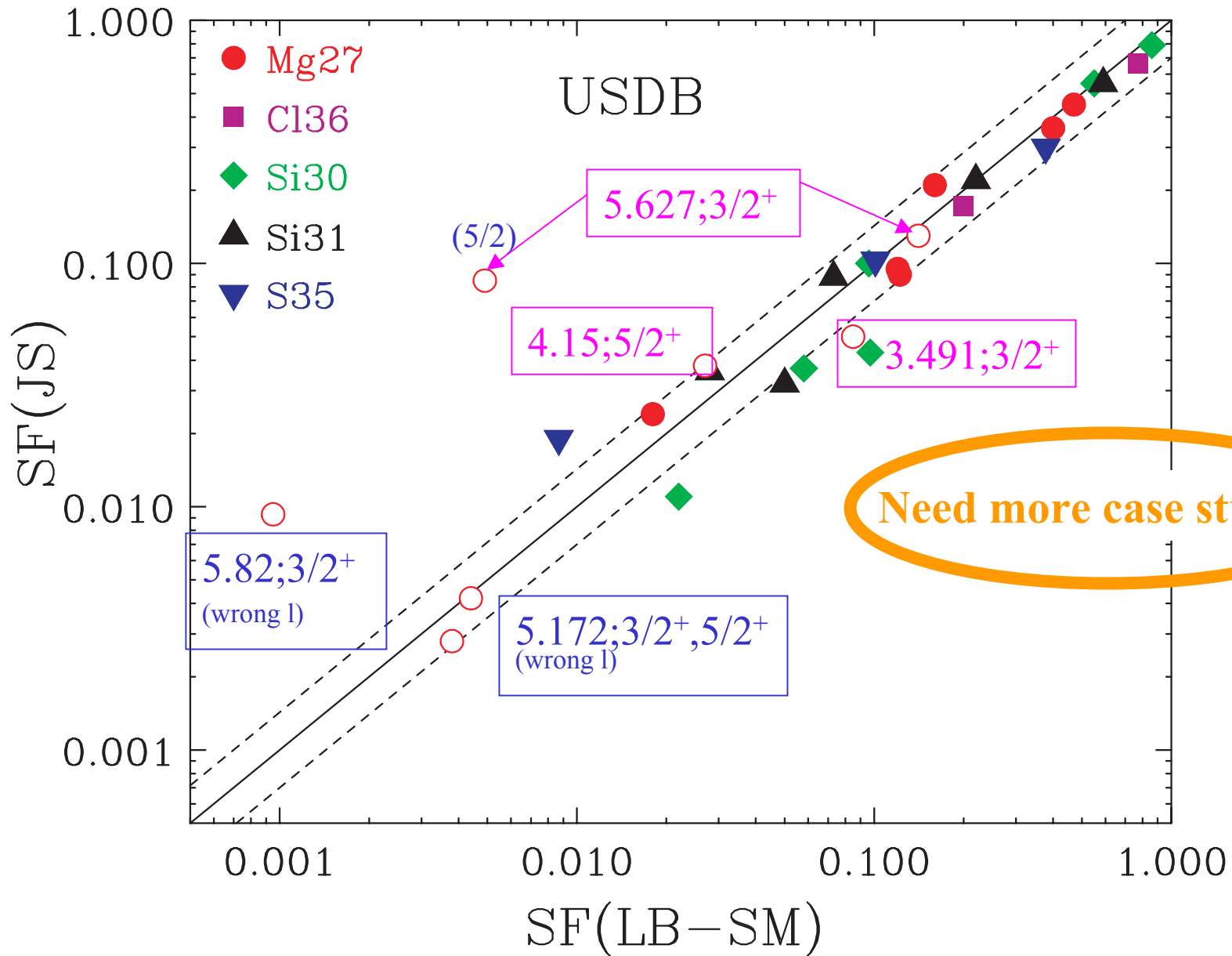
Oxbash:  $^{31}\text{Si}$



# Comparisons to LB-SM (oxbash, B.A. Brown) calculations



# Spin assignment from Systematics with SM



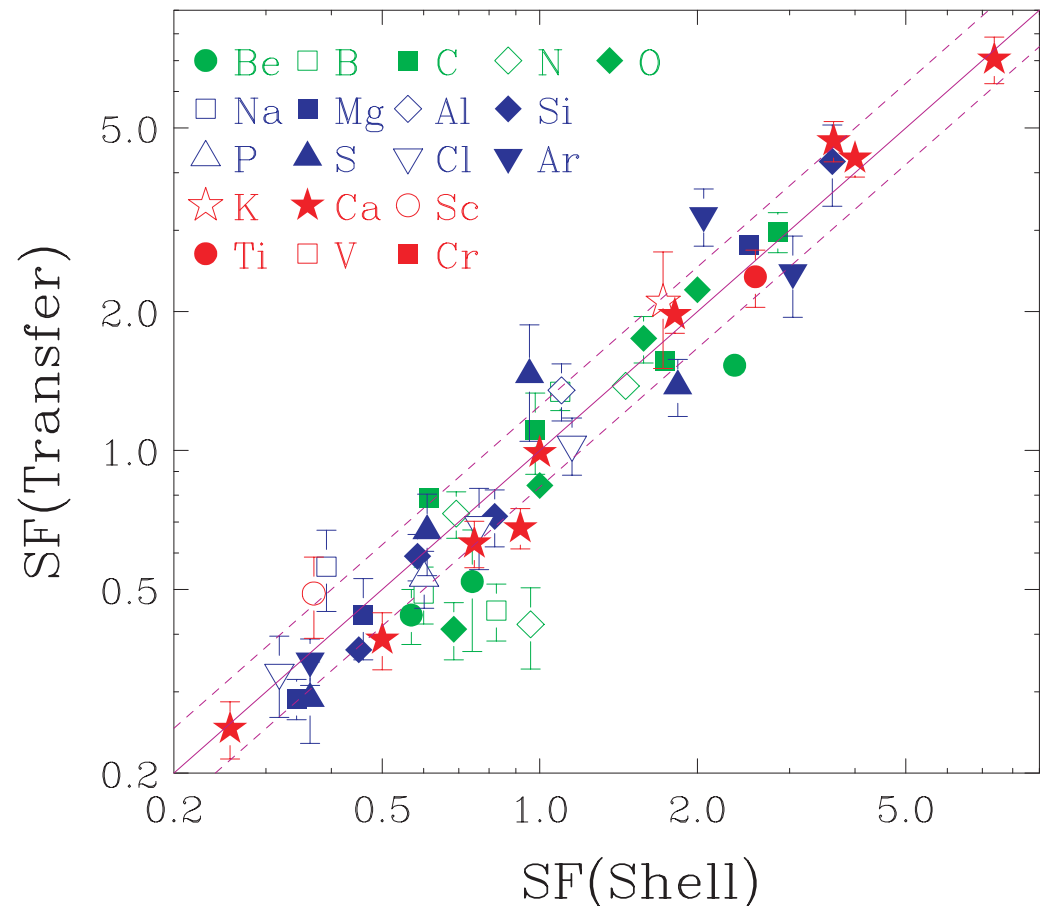
# Summary

- Last SF review was done by Endt in 1977. A new review of SF values is overdue with more data, better reaction models and better SM calculations;  $\rightarrow$  gives directions for rare-isotope research.*

Summer Undergraduate  
Research Experience,  
Chinese University of  
Hong Kong, (SURE)  
students

Jenny Lee (2004,  
ground states)

M.B. Tsang, et al, PRL95, 222501 (2005).



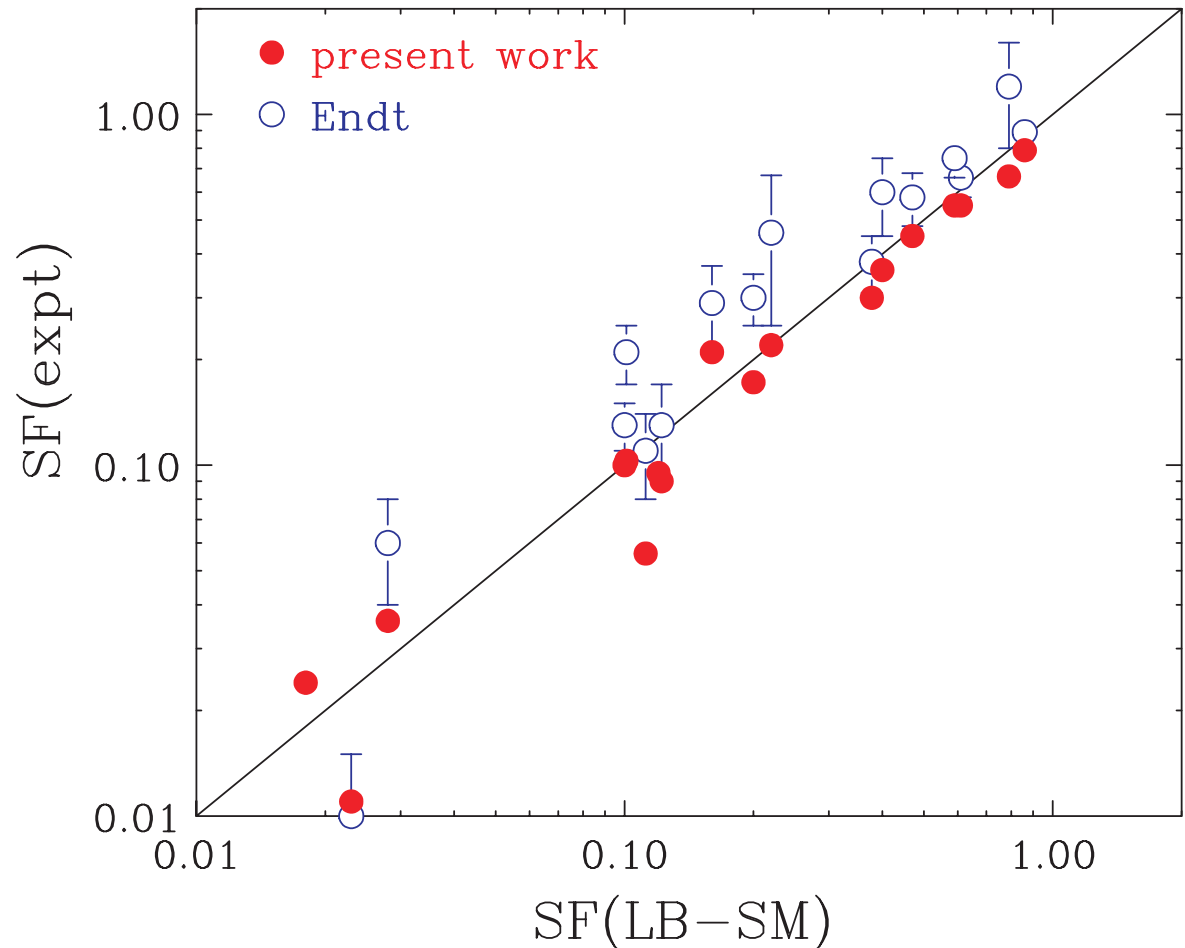
# Summary

- Last SF review was done by Endt in 1977. A new review of SF values is overdue with more data, better reaction models and better SM calculations; → gives directions for rare-isotope research.*

Summer Undergraduate  
Research Experience,  
Chinese University of  
Hong Kong, (SURE)  
students

Jenny Lee (2004,  
ground states)

Shi Chun Su (2006,  
excited states)



# Summary/Suggestions

- 1. Last SF review was done by Endt in 1977. A new review of SF values is overdue with more data, better reaction models and better SM calculations; → gives directions for rare-isotope research.*
- 2. Include projectile fragmentation cross-sections in NuDat as in spallation cross-sections.*
- 3. Publications in Nuclear Data Sheets?*
- 4. Direct inclusion of large sets of data from PRC, NP etc.*
- 5. Search, search , search ...incorporate google search engine in the data base?*





# NSCL Reacceleration Stage Options

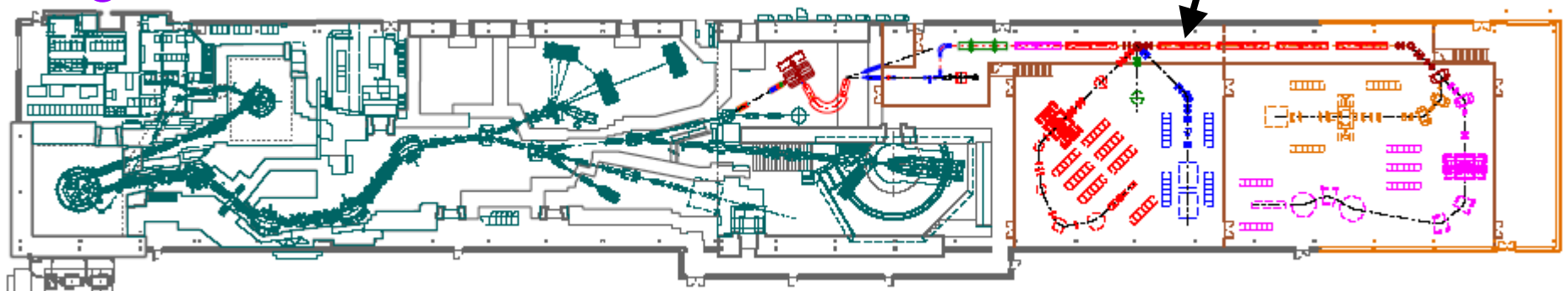
A1900/ Cyclotron Stopper/ Charge Breeder/ RFQ/ LINAC

Stage I 1-2 MeV/u



Reaccelerated  
beam area

Stage II 12 MeV/u



*In near future, transfer reactions will become an important and unique tool to understand structure and reaction mechanism.*