

Argonne National Laboratory

**ENDF/B Neutron Cross-section Data
for Natural Helium
(ENDF-125)**

by

E. M. Pennington

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ARGONNE NATIONAL LABORATORY
9700 South Cass Avenue
Argonne, Illinois 60439

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E. M. Pennington

Reactor Physics Division

October 1968

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ABSTRACT

This report describes the compilation of neutron cross-section data for natural helium. The elastic scattering cross section, $\bar{\mu}_L$, ξ , γ , and elastic scattering Legendre coefficients are included for ^4He . Since ^3He has a natural abundance of merely 0.00013%, only its (n,p) cross section, which is large at low energies, is considered. A listing of the data in the ENDF/B format is presented, as are graphs of much of the data.

I. INTRODUCTION

Since natural helium is a possible coolant for fast breeder reactors, the present helium cross-section data were compiled. The data will be distributed with ENDF/B identification number MAT = 1088.

The composition of natural helium is 99.99987% ^4He and 0.00013% ^3He . Because of the low abundance of ^3He , only its (n,p) cross section, which is large at low energies, need be considered. Elastic scattering is the only possible reaction for neutrons incident on ^4He at energies below 15 MeV. Thus the elastic scattering cross section and values of $\bar{\mu}_L$, ξ , and γ are included in the compilation, as well as elastic scattering Legendre coefficients. Here $\bar{\mu}_L$ is the average cosine of the angle of elastic scattering in the laboratory system, ξ is the average logarithmic energy decrement in an elastic collision, and γ , the Greuling-Goertzel parameter, is the average of the square of the logarithmic energy decrement divided by twice the average logarithmic energy decrement. Parameters for a free-gas thermal scattering law are also included.

II. DATA SOURCES AND CALCULATIONAL METHODS

The elastic scattering cross section and Legendre expansion coefficients were calculated from s-, p-, and d-wave phase shifts using a FORTRAN program written for the purpose. Appendix A presents the equations involved in this program. The phase shifts were read from smooth

curves based on Table I of Ref. 1. At energies below the 300-keV lower limit of this table, each of the two p-wave phase shifts was obtained by using a functional form based on the low-energy limit for a single p-wave resonance, with parameters determined from fitting the low-energy phase shifts of the table. Appendix B presents the equations connected with the low-energy phase shifts, and the parameters obtained by the fitting procedure. The s-wave phase shift below 300 keV was calculated using hard-sphere scattering and a nuclear radius of $a = 2.4 F$. This yields a thermal scattering cross section of $4\pi a^2 = 0.7238$ barn, in agreement with the experimental value² of 0.73 ± 0.05 barn. The low-energy s-wave phase shifts of Ref. 1 are consistent with a nuclear radius of about 2.48 F and so would yield a somewhat high thermal cross section.

Table I lists the phase shifts used in the calculations at energies above 10 keV.

TABLE I. Helium Phase Shifts Used in Calculations of Elastic Scattering Cross Sections and Legendre Expansion Coefficients

E_{lab} , MeV	δ_0^+	δ_1^+	δ_1^-	δ_2^+	δ_2^-	E_{lab} , MeV	δ_0^+	δ_1^+	δ_1^-	δ_2^+	δ_2^-
0.02	3.08203	0.00092	0.00022			2.9	2.4155	2.1660	0.4782	0.0030	0.0021
0.03	3.06865	0.00171	0.00040			3.0	2.4051	2.1677	0.5009	0.0031	0.0023
0.05	3.04742	0.00373	0.00086			3.2	2.3806	2.1712	0.5428	0.0037	0.0026
0.07	3.03017	0.00629	0.00143			3.4	2.3579	2.1729	0.5847	0.0042	0.0031
0.10	3.00842	0.0110	0.00246			3.6	2.3370	2.1694	0.6248	0.0049	0.0035
0.15	2.97849	0.0212	0.00457			3.8	2.3178	2.1625	0.6667	0.0054	0.0038
0.20	2.95326	0.0343	0.00711			4.0	2.2986	2.1537	0.7086	0.0061	0.0044
0.25	2.93103	0.0504	0.0100			4.2	2.2794	2.1468	0.7435	0.0070	0.0049
0.30	2.9025	0.0698	0.0133			4.4	2.2602	2.1398	0.7767	0.0077	0.0054
0.35	2.8833	0.0930	0.0170			4.6	2.2427	2.1328	0.8081	0.0084	0.0059
0.40	2.8658	0.1204	0.0209			4.8	2.2253	2.1258	0.8360	0.0093	0.0065
0.45	2.8466	0.1536	0.0252			5.0	2.2078	2.1171	0.8622	0.0101	0.0070
0.50	2.8292	0.1920	0.0299			5.2	2.1904	2.1084	0.8849	0.0110	0.0075
0.55	2.8152	0.2356	0.0348			5.4	2.1747	2.0996	0.9058	0.0120	0.0082
0.60	2.8047	0.2845	0.0401			5.6	2.1590	2.0892	0.9250	0.0131	0.0087
0.65	2.7908	0.3421	0.0454			5.8	2.1450	2.0804	0.9442	0.0141	0.0094
0.70	2.7786	0.4067	0.0524			6.0	2.1293	2.0717	0.9617	0.0152	0.0103
0.75	2.7646	0.4800	0.0576			6.2	2.1153	2.0630	0.9774	0.0162	0.0108
0.80	2.7524	0.5725	0.0646			6.4	2.1014	2.0543	0.9896	0.0175	0.0115
0.85	2.7402	0.6615	0.0698			6.6	2.0857	2.0438	1.0001	0.0185	0.0124
0.90	2.7297	0.7662	0.0768			6.8	2.0717	2.0351	1.0105	0.0197	0.0133
0.95	2.7175	0.8779	0.0838			7.0	2.0577	2.0263	1.0210	0.0209	0.0140
1.00	2.7070	0.9983	0.0908			7.2	2.0455	2.0176	1.0280	0.0222	0.0145
1.05	2.6965	1.1170	0.0977			7.4	2.0316	2.0089	1.0350	0.0236	0.0152
1.10	2.6861	1.2235	0.1065			7.6	2.0193	2.0001	1.0420	0.0248	0.0159
1.13	2.6791	1.2881	0.1100			7.8	2.0054	1.9914	1.0472	0.0262	0.0166
1.15	2.6756	1.3299	0.1134			8.0	1.9932	1.9827	1.0507	0.0279	0.0175
1.17	2.6721	1.3701	0.1169			8.2	1.9809	1.9740	1.0559	0.0297	0.0183
1.20	2.6669	1.4312	0.1222			8.4	1.9705	1.9652	1.0594	0.0314	0.0190
1.25	2.6564	1.5202	0.1292			8.6	1.9583	1.9565	1.0612	0.0332	0.0197
1.30	2.6477	1.5970	0.1379			8.8	1.9478	1.9478	1.0629	0.0349	0.0206
1.35	2.6389	1.6668	0.1466			9.0	1.9356	1.9391	1.0647	0.0367	0.0215
1.40	2.6302	1.7296	0.1553			9.2	1.9234	1.9321	1.0647	0.0384	0.0223
1.45	2.6215	1.7802	0.1641			9.4	1.9129	1.9234	1.0647	0.0401	0.0234
1.5	2.6128	1.8239	0.1745			9.6	1.9007	1.9146	1.0647	0.0419	0.0243
1.6	2.5953	1.9059	0.1937			9.8	1.8902	1.9059	1.0629	0.0436	0.0253
1.7	2.5796	1.9652	0.2129			10.0	1.8780	1.8972	1.0629	0.0454	0.0262
1.8	2.5639	2.0106	0.2321			10.5	1.8535	1.8780	1.0612	0.0506	0.0288
1.9	2.5482	2.0438	0.2531			11.0	1.8291	1.8570	1.0577	0.0541	0.0314
2.0	2.5342	2.0752	0.2758	0.0012	0.0009	11.5	1.8047	1.8378	1.0507	0.0593	0.0340
2.1	2.5203	2.0961	0.2967	0.0012	0.0009	12.0	1.7802	1.8169	1.0402	0.0646	0.0367
2.2	2.5063	2.1153	0.3194	0.0014	0.0010	12.5	1.7593	1.7994	1.0297	0.0698	0.0384
2.3	2.4923	2.1293	0.3403	0.0016	0.0012	13.0	1.7383	1.7820	1.0193	0.0750	0.0419
2.4	2.4784	2.1398	0.3630	0.0017	0.0012	13.5	1.7174	1.7628	1.0071	0.0803	0.0436
2.5	2.4644	2.1468	0.3857	0.0019	0.0014	14.0	1.6965	1.7453	0.9966	0.0855	0.0454
2.6	2.4522	2.1537	0.4084	0.0021	0.0016	14.5	1.6755	1.7279	0.9861	0.0908	0.0471
2.7	2.4400	2.1590	0.4328	0.0024	0.0017	15.0	1.6546	1.7104	0.9756	0.0960	0.0489
2.8	2.4278	2.1642	0.4555	0.0026	0.0019						

Values of $\bar{\mu}_L$, ξ , and γ were calculated from the Legendre coefficients using a FORTRAN program, MUXIGA. This program is based on the equations derived in Refs. 3-5. These equations are summarized in Appendix C.

An elastic scattering Legendre-coefficient transformation matrix from the center-of-mass system to the laboratory system was computed using CHAD.⁶ A minor revision was made in the CHAD code to avoid elements of the matrix being set equal to zero if they were larger than elements closer to the diagonal.

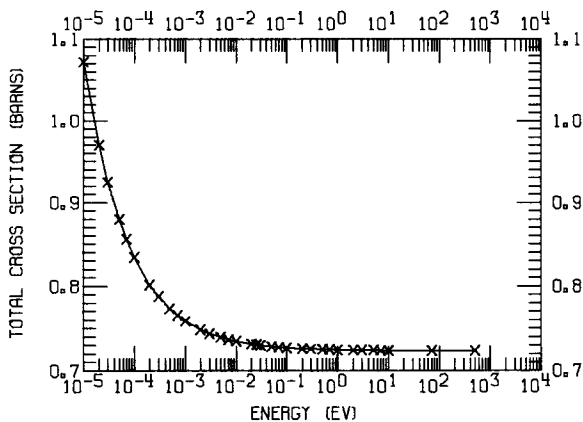
The (n,p) cross section for ^3He is that recommended in the ^3He evaluation by J. Als-Nielsen.⁷ Extension from 10 to 15 MeV was made using linear extrapolation on a log σ versus log E scale.

The total cross section is the sum of the elastic scattering and (n,p) cross sections.

The free-gas thermal scattering law involves a value of 0.7238 barn for the free-atom scattering cross section.

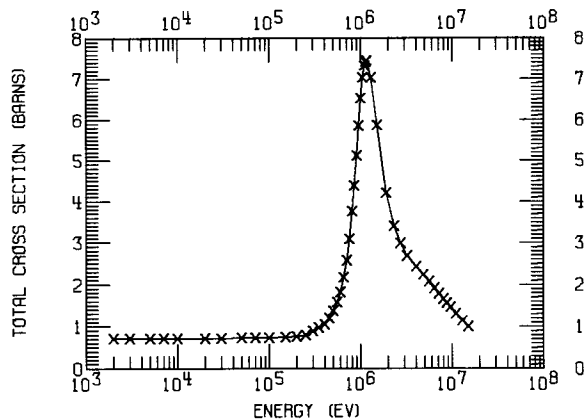
III. GRAPHS AND LISTING

Figures 1-8 are graphs of the ENDF/B File 3 data.⁸ The File 3 data are represented by a series of pairs of x and y values with an interpolation rule applying between successive pairs. The interpolation rule might specify, for example, that log y is linear in log x between successive (x,y) pairs. In Figs. 1-8 the axis types have been chosen to correspond to the interpolation rule. Thus in Figs. 1 and 2 a linear axis is used for the total cross section and a logarithmic axis is used for the energy, because linear y versus log x interpolation is specified for this cross section. The total cross section



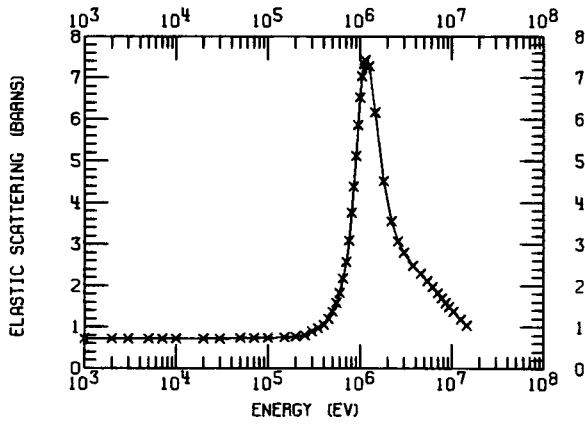
113-691

Fig. 1. Helium Total Cross Section,
10⁻⁵ eV to 1 keV



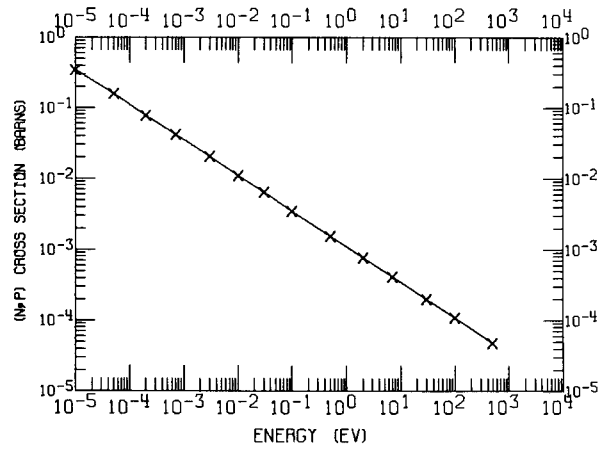
113-682

Fig. 2. Helium Total Cross Section,
1 keV to 15 MeV



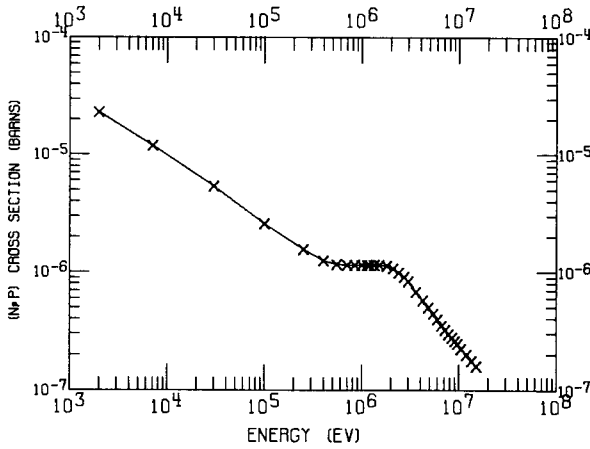
113-681

Fig. 3. Helium Elastic Scattering Cross Section



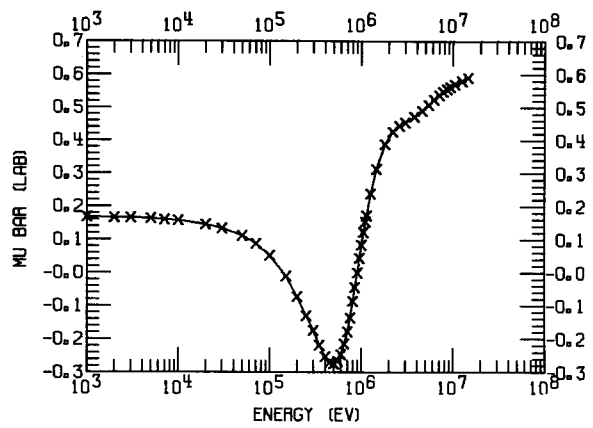
113-686

Fig. 4. Helium (n,p) Cross Section, 10^{-5} eV to 1 keV



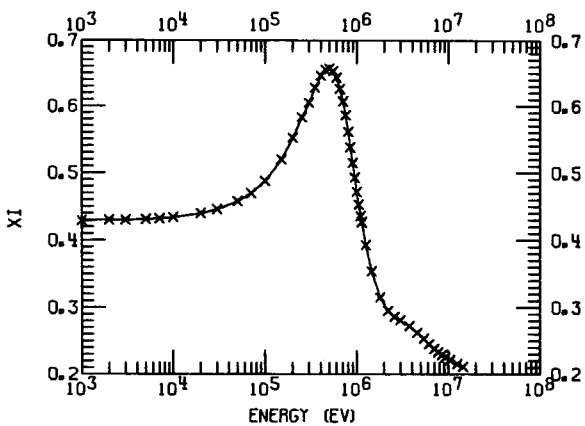
113-685

Fig. 5. Helium (n,p) Cross Section, 1 keV to 15 MeV



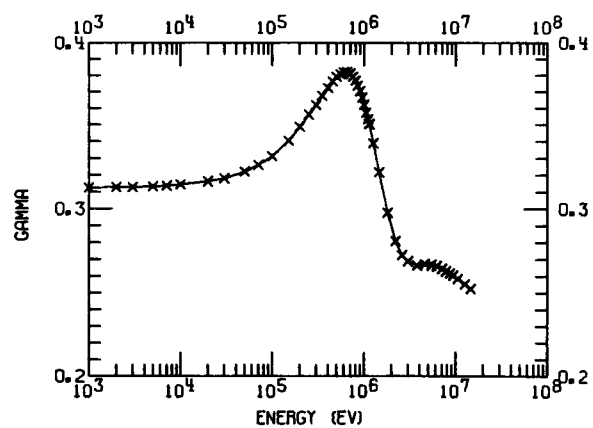
113-696

Fig. 6. Helium Average Elastic Scattering Cosine, $\bar{\mu}_L$



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Fig. 7. Helium Average Logarithmic Energy Decrement, ξ



113-680

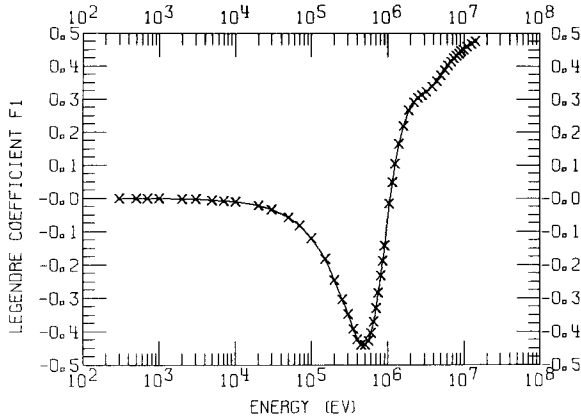
Fig. 8. Helium Greuling-Goertzel Parameter, γ

and the (n,p) cross section have been plotted in two energy ranges in Figs. 1 and 2 and Figs 4 and 5, respectively, in order to display the data better. The data in Figs. 3, 6, 7, and 8 for the elastic scattering cross section, $\bar{\mu}_L$, ξ , and γ are not plotted below 1 keV because the values are almost constant at low energies. Not all data points are plotted, especially at high energies, to avoid clutter on the graphs.

Figures 9-12 display the Legendre coefficients for elastic scattering angular distributions in the center-of-mass system, f_1 through f_4 . The elastic scattering angular distribution, $d\sigma(E)/d\Omega$, is given by⁸

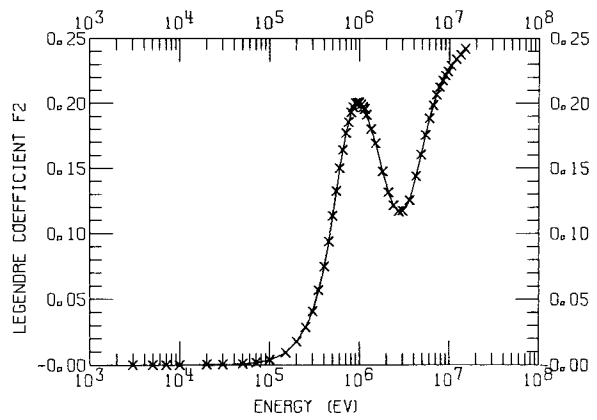
$$\frac{d\sigma(E)}{d\Omega} = \frac{\sigma_s(E)}{4\pi} \sum_{\ell=0} (2\ell + 1) f_{\ell}(E) P_{\ell}(\mu), \quad (1)$$

where the elastic scattering cross section $\sigma_s(E)$ is tabulated in ENDF/B File 3, and the expansion coefficients $f_{\ell}(E)$ are presented at a series of



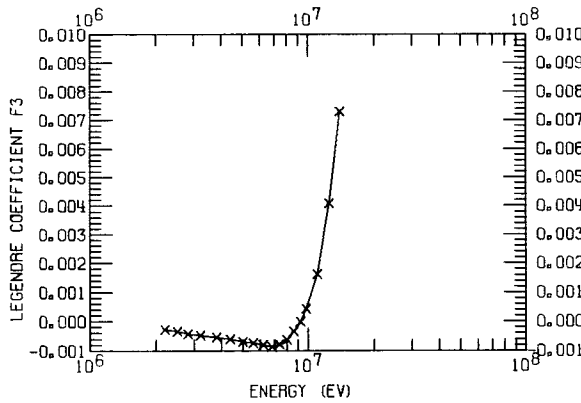
113-694

Fig. 9. Helium Elastic Scattering Legendre Coefficient f_1



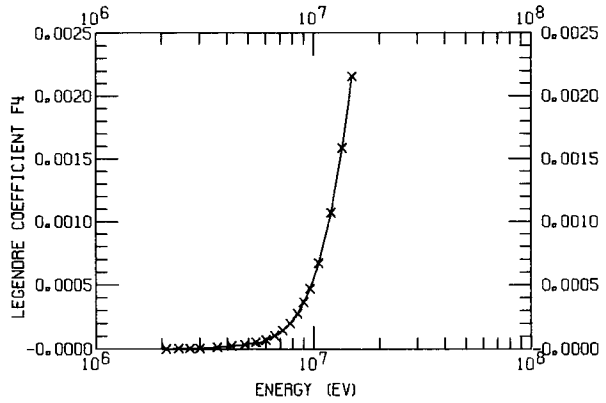
113-688

Fig. 10. Helium Elastic Scattering Legendre Coefficient f_2



113-702

Fig. 11. Helium Elastic Scattering Legendre Coefficient f_3

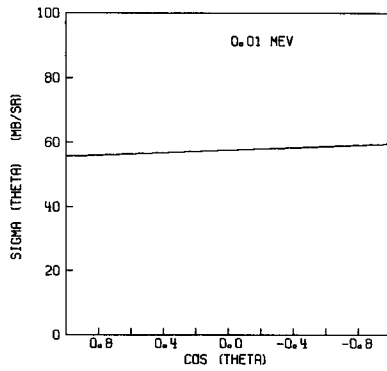


113-674

Fig. 12. Helium Elastic Scattering Legendre Coefficient f_4

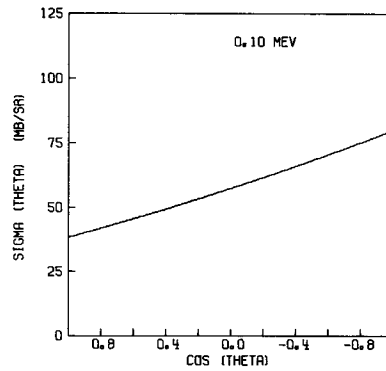
energies in File 4. In Figs. 13-31 the angular distributions have been calculated from Eq. 1 at a representative sequence of 19 energies. Note that the angular distributions at the energies shown below 1.2 MeV are peaked in the backward direction, as is typical on the low-energy side of a p-wave resonance. All graphs were drawn with the aid of the CDC-3600 computer and the Calcomp 580 plotter.

The helium data in the ENDF/B format are listed in Appendix D. The listing will not be explained here since all information necessary for understanding the formats involved is in Ref. 8.



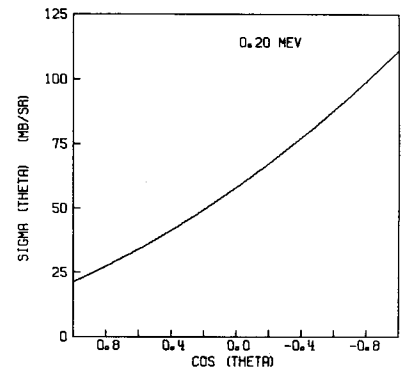
113-701

Fig. 13



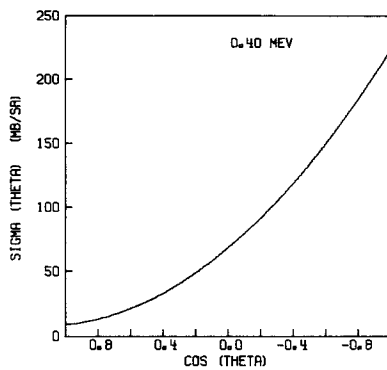
113-678

Fig. 14



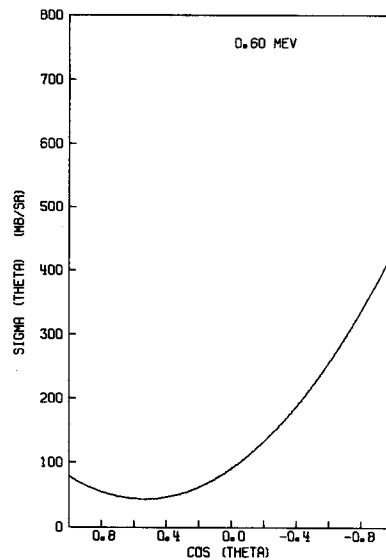
113-700

Fig. 15



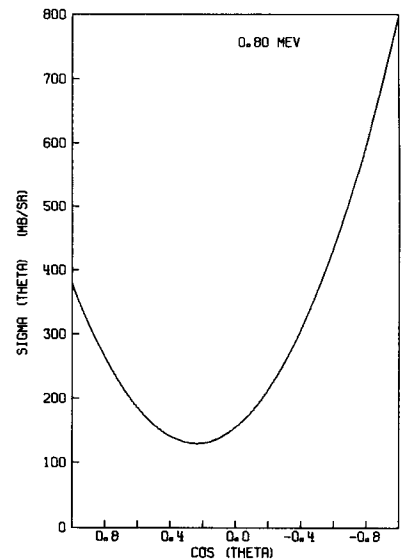
113-676

Fig. 16



113-703

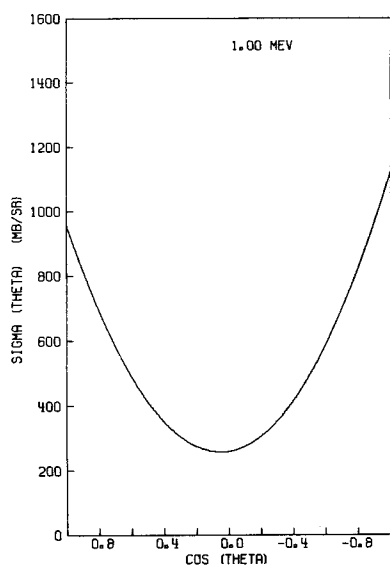
Fig. 17



113-683

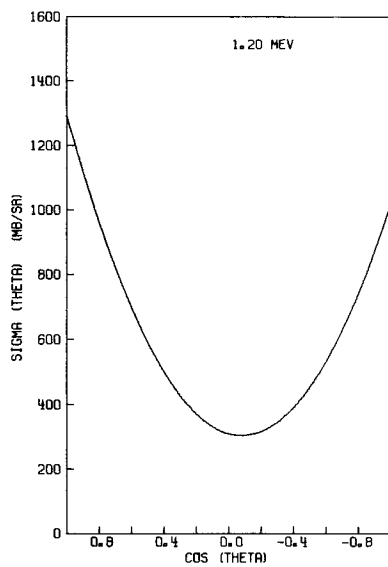
Fig. 18

Figs. 13-18. Helium Elastic Scattering Angular Distributions



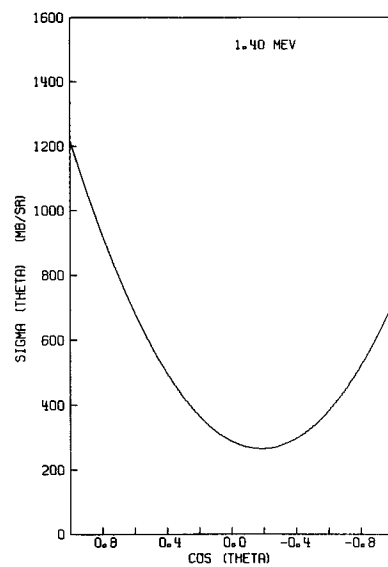
113-677

Fig. 19



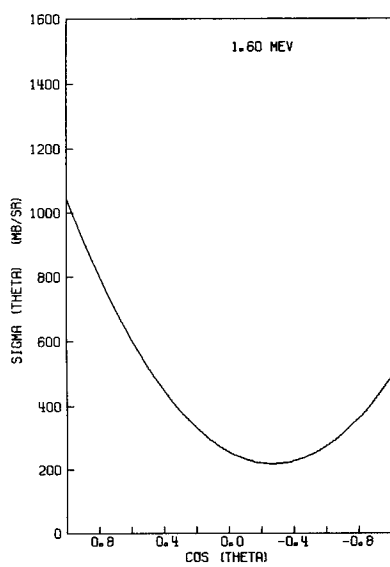
113-697

Fig. 20



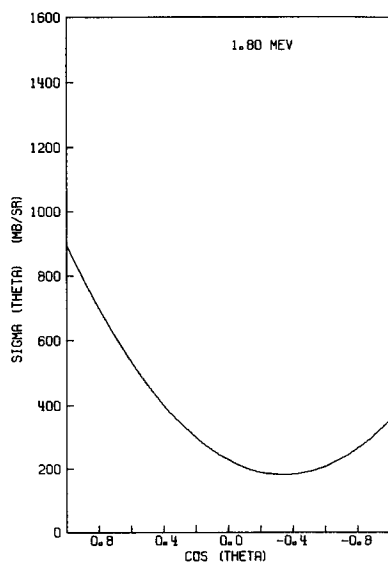
113-699

Fig. 21



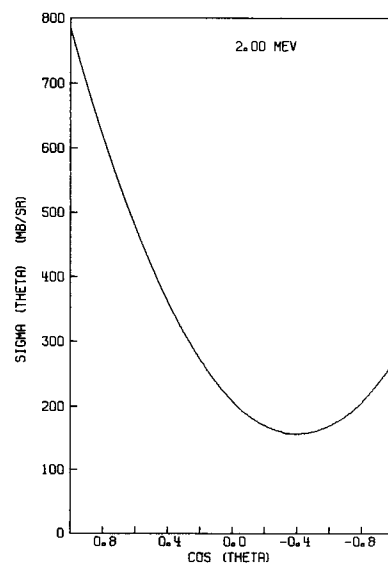
113-695

Fig. 22



113-684

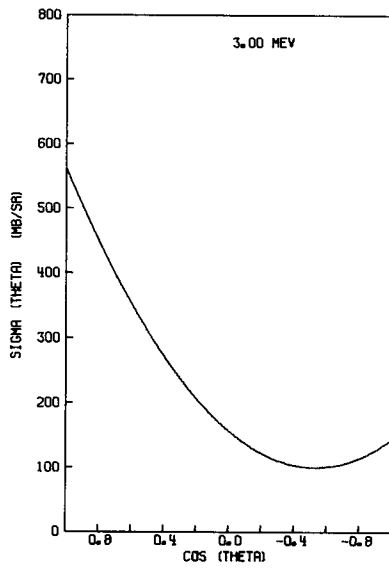
Fig. 23



113-692

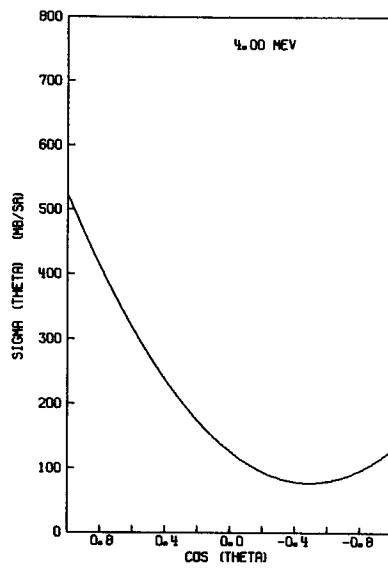
Fig. 24

Figs. 19-24. Helium Elastic Scattering Angular Distributions



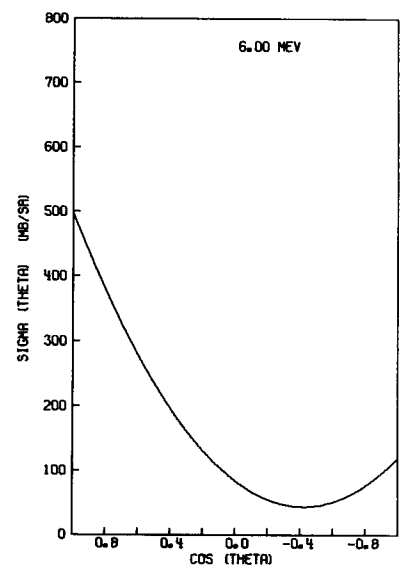
113-693

Fig. 25



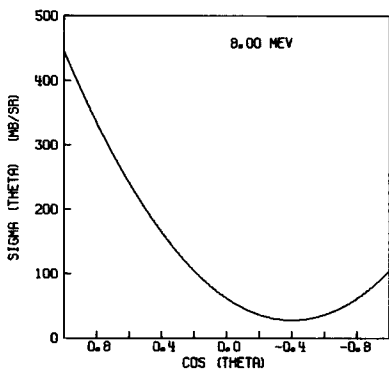
113-675

Fig. 26



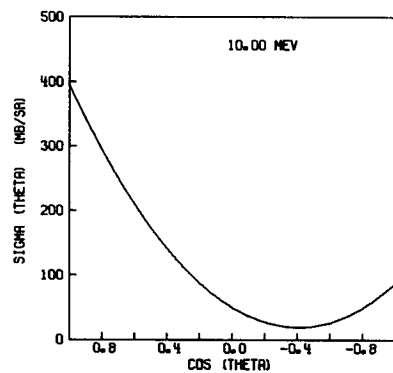
113-690

Fig. 27



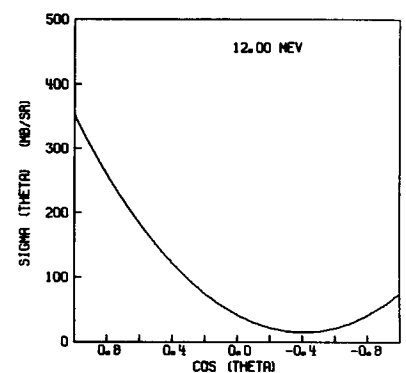
113-679

Fig. 28



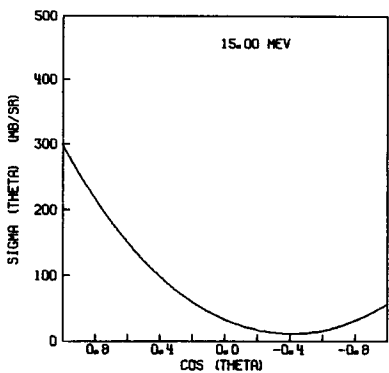
113-687

Fig. 29



113-704

Fig. 30



113-689

Fig. 31

Figs. 25-31
Helium Elastic Scattering Angular Distributions

IV. DISCUSSION

The phase shifts of Ref. 1, which were used in the compilation, are optical-model phase shifts chosen to fit both angular-distribution and polarization data at many energies. The total cross section is also fit within the scatter of the experimental points. Because Ref. 1 is recent and considers the experimental data comprehensively, the data calculated from the phase shifts should be reliable. Another recent set of phase shifts⁹ is not very different from that of Ref. 1 and could also have been used in the present work.

As discussed in Ref. 7, the ^3He (n,p) cross section is rather well known. Probably more error is introduced into the (n,p) cross section for natural helium by the uncertainty in the ^3He isotopic abundance than by the uncertainty in the ^3He (n,p) cross section itself.

Previous evaluations of natural helium for reactor calculations include those of Schmidt¹⁰ and of Buckingham *et al.*^{11,12} Schmidt's evaluation includes the (n,p) cross section for ^3He and $\sigma_s, \bar{\mu}_L$, and a set of phase shifts for ^4He . Buckingham *et al.* present separate compilations for ^3He and ^4He . For ^3He , elastic, (n,p), (\bar{n},d), and (n,2n) cross sections are given, as well as elastic angular distributions. The ^4He evaluation consists of σ_s and angular distributions.

The (n,p) cross section of ^3He , which was based on Ref. 7, is not very different from those of previous evaluations,^{10,12} as may be seen from Table 3 of Ref. 7.

The values of the elastic scattering cross section are in fairly good agreement with those in the other evaluations.^{10,11} Schmidt's values¹⁰ agree with those of the present evaluation at energies below the main resonance and are generally a little larger at higher energies, except for a range on the high-energy side of the main resonance. The English values¹¹ are higher than the present values at energies below about 1 MeV and lower at higher energies.

The present values of $\bar{\mu}_L$ are in rather good agreement with those shown on Fig. He-3 in Part I of KFK-120¹⁰ at energies above approximately 1 MeV, but do not agree well at lower energies.

APPENDIX A

Equations Relating the Elastic Scattering Cross Section and Legendre Expansion Coefficients to the s-, p-, and d-wave Phase Shifts

The elastic scattering angular distribution, $d\sigma/d\Omega$, in the center-of-mass system is given by¹³

$$\frac{d\sigma}{d\Omega} = \frac{1}{4k^2} (|a|^2 + |b|^2) = \sum_n C_n P_n(\mu), \quad (\text{A.1})$$

where

$$a = \sum_{\ell=0}^{\infty} \left[(\ell+1)(e^{2i\delta_{\ell}^+} - 1) + \ell(e^{2i\delta_{\ell}^-} - 1) \right] P_{\ell}(\mu), \quad (\text{A.2})$$

and

$$b = \sum_{\ell=0}^{\infty} \left(e^{2i\delta_{\ell}^+} - e^{2i\delta_{\ell}^-} \right) P_{\ell}^1(\mu). \quad (\text{A.3})$$

Here μ is the cosine of the center-of-mass scattering angle, $P_{\ell}(\mu)$ is the Legendre polynomial of order ℓ , and

$$P_{\ell}^1(\mu) = (1 - \mu^2)^{1/2} \frac{d}{d\mu} P_{\ell}(\mu).$$

The quantity $k = \sqrt{2mE/\hbar^2}$, where E is the energy of relative motion of neutron and nucleus in the center-of-mass system, and m is the reduced mass. The phase shifts δ_{ℓ}^+ and δ_{ℓ}^- refer to $j = \ell + 1/2$ and $j = \ell - 1/2$, respectively, where j is the angular momentum quantum number referring to the addition of the orbital and spin angular momenta.

On restricting the sums in Eqs. A.2 and A.3 by considering only s-, p-, and d-wave phase shifts, and using the explicit forms for the Legendre polynomials, we obtain

$$k^2 C_0 = \sin^2 \delta_0^+ + 2 \sin^2 \delta_1^+ + \sin^2 \delta_1^- + 3 \sin^2 \delta_2^+ + 2 \sin^2 \delta_2^-, \quad (\text{A.4})$$

$$\begin{aligned} k^2 C_1 = & 3 \sin^2 \delta_0^+ + 6 \sin^2 \delta_1^+ + 3 \sin^2 \delta_1^- + \frac{18}{5} \sin^2 \delta_2^+ + \frac{12}{5} \sin^2 \delta_2^- \\ & - 2 \sin^2 (\delta_0^+ - \delta_1^+) - \sin^2 (\delta_0^+ - \delta_1^-) - \frac{18}{5} \sin^2 (\delta_1^+ - \delta_2^+) \\ & - 2 \sin^2 (\delta_1^- - \delta_2^-) - \frac{2}{5} \sin^2 (\delta_1^+ - \delta_2^-), \end{aligned} \quad (\text{A.5})$$

$$\begin{aligned}
k^2 C_2 = & 5 \sin^2 \delta_0^+ + 4 \sin^2 \delta_1^+ + 2 \sin^2 \delta_1^- + \frac{51}{7} \sin^2 \delta_2^+ + \frac{34}{7} \sin^2 \delta_2^- \\
& - 2 \sin^2 (\delta_1^+ - \delta_1^-) - \frac{6}{7} \sin^2 (\delta_2^+ - \delta_2^-) - 3 \sin^2 (\delta_0^+ - \delta_2^+) \\
& - 2 \sin^2 (\delta_0^+ - \delta_2^-), \tag{A.6}
\end{aligned}$$

$$\begin{aligned}
k^2 C_3 = & 6 \sin^2 \delta_1^+ + 3 \sin^2 \delta_1^- + \frac{27}{5} \sin^2 \delta_2^+ + \frac{18}{5} \sin^2 \delta_2^- \\
& - \frac{12}{5} \sin^2 (\delta_1^+ - \delta_2^+) - \frac{18}{5} \sin^2 (\delta_1^+ - \delta_2^-) - 3 \sin^2 (\delta_1^- - \delta_2^+), \tag{A.7}
\end{aligned}$$

and

$$k^2 C_4 = \frac{54}{7} \sin^2 \delta_2^+ + \frac{36}{7} \sin^2 \delta_2^- - \frac{36}{7} \sin^2 (\delta_2^+ - \delta_2^-). \tag{A.8}$$

Equation 1 gives the angular distribution in the ENDF/B normalization. Thus the elastic scattering cross section is $\sigma_s = 4\pi C_0$, and the Legendre coefficients are given by

$$f_\ell = \frac{C_\ell}{(2\ell + 1) C_0}.$$

APPENDIX B

Low-energy Phase Shifts from Resonance Parameters

The phase shift, $\delta_{\ell J}$, near an isolated purely scattering resonance with orbital angular momentum ℓ and total angular momentum J is¹⁴

$$\delta_{\ell J} = \tan^{-1} \left(\frac{R_{\ell J} P_{\ell}}{1 - R_{\ell J} \hat{S}_{\ell}} \right) - \phi_{\ell}, \quad (\text{B.1})$$

where

$$\phi_{\ell} = \tan^{-1} \left(\frac{F_{\ell}}{G_{\ell}} \right) \quad (\text{B.2})$$

with

$$F_{\ell} = \rho j_{\ell}(\rho) \quad (\text{B.3})$$

and

$$G_{\ell} = -\rho n_{\ell}(\rho). \quad (\text{B.4})$$

The functions $j_{\ell}(\rho)$ and $n_{\ell}(\rho)$ are spherical Bessel functions.¹⁵ The quantity ρ is defined by

$$\rho = ka = a \sqrt{2mE/\hbar^2} = a \sqrt{\frac{2m}{\hbar^2} \frac{A}{A+1} E_{\text{lab}}} = C \sqrt{E_{\text{lab}}},$$

where E is the energy of the relative motion of neutron and target in the center-of-mass system, E_{lab} is the neutron energy in the laboratory system, $m = m_n A/(1+A)$, with A being the ratio of the target mass to the neutron mass, m_n , and a is the nuclear radius. The penetration and shift factors are

$$P_{\ell} = \frac{\rho}{F_{\ell}^2 + G_{\ell}^2} \quad (\text{B.5})$$

and

$$S_{\ell} = \frac{\rho(F_{\ell}' F_{\ell}' + G_{\ell}' G_{\ell}')}{F_{\ell}^2 + G_{\ell}^2} \quad (\text{B.6})$$

where the prime signifies differentiation with respect to ρ . The \hat{S}_{ℓ} in Eq. B.1 is related to S_{ℓ} by $\hat{S}_{\ell} = S_{\ell} - B_{\ell J}$, where $B_{\ell J}$ is a boundary-condition constant.¹⁴ The function $R_{\ell J}$ is

$$R_{\ell J} = \frac{\gamma_{\lambda \ell J}^2}{E_{\lambda \ell J} - E}, \quad (\text{B.7})$$

where $\gamma_{\lambda \ell J}^2$ is the reduced width of the resonance, and $E_{\lambda \ell J}$ is the associated energy eigenvalue.

For $\ell = 1$, the explicit forms of F_ℓ and G_ℓ are

$$F_1 = \frac{\sin \rho - \rho \cos \rho}{\rho} \quad (\text{B.8})$$

and

$$G_1 = \frac{\cos \rho + \rho \sin \rho}{\rho}. \quad (\text{B.9})$$

Using Eqs. B.5-B.9 in conjunction with Eq. B.1 and the boundary condition $B_{\ell J} = 0$ results in

$$\delta_{1J} + \phi_1 = \tan^{-1} \left(\frac{\alpha \rho^3}{1 + \beta \rho^2 + (\alpha + \beta - 1) \rho^4} \right) \approx \frac{\alpha \rho^3}{1 + \beta \rho^2 + (\alpha + \beta - 1) \rho^4}, \quad (\text{B.10})$$

where

$$\alpha = \frac{\gamma_{\lambda 1J}^2}{E_{\lambda 1J} + \gamma_{\lambda 1J}^2} \quad (\text{B.11})$$

and

$$\beta = \frac{E_{\lambda 1J} - \frac{A}{A+1} \frac{1}{C^2}}{E_{\lambda 1J} + \gamma_{\lambda 1J}^2} \quad (\text{B.12})$$

The parameters α and β were determined by fitting the low-energy p-wave phase shifts of Table I of Ref. 1 using Eq. B.10 and $a = 3.0 \times 10^{-13}$ cm. The phase shifts at 0.3 and 0.4 MeV were fit for $J = 3/2$; those at 0.4 and 0.6 MeV were fit for $J = 1/2$. This procedure gives two linear equations in α and β for both $J = 3/2$ and $J = 1/2$. Table II presents the solutions of the equations.

TABLE II. Low-energy Parameters for p-wave Phase Shifts

J	α	β
3/2	2.528	-2.534
1/2	0.857	-0.204

APPENDIX C

Equations for Calculation of $\bar{\mu}_L$, ξ , and γ

Equation 1 gives the angular distribution in the center-of-mass system for elastic scattering. The equations for $\bar{\mu}_L$, ξ , and γ , in terms of the f_l expansion coefficients, derived in Refs. 3-5 and used in FORTRAN program MUXIGA, are given below.

The average cosine of the angle of elastic scattering in the laboratory system is

$$\bar{\mu}_L = \sum_{l=0}^{\infty} T_{1l} f_l, \quad (\text{C.1})$$

where

$$T_{1l} = \frac{l}{2l-1} \left(\frac{-1}{A}\right)^{l-1} - \frac{l+2}{2l+3} \left(\frac{-1}{A}\right)^{l+1}, \quad (\text{C.2})$$

A being the ratio of the mass of the scatterer to the neutron mass.

The average logarithmic energy decrement in elastic scattering is

$$\xi = \sum_{l=0}^{\infty} \sum_{p=l+\delta_{l0}}^{\infty} (1-\alpha)^p A_{pl} f_l, \quad (\text{C.3})$$

where

$$A_{pl} = \frac{(-1)^l (2l+1) p! p!}{p(p-l)! (p+l+1)!} \quad (\text{C.4})$$

and

$$\alpha = \left(\frac{A-1}{A+1}\right)^2.$$

The Greuling-Goertzel parameter, γ , is given by

$$2\xi\gamma = \sum_{l=0}^{\infty} \sum_{p=l+\delta_{l1}+\delta_{l0}}^{\infty} (1-\alpha)^p A_{pl} C_{pl} f_l, \quad (\text{C.5})$$

where

$$C_p = 2 \sum_{q=1}^{p-1} \frac{1}{q}. \quad (\text{C.6})$$

The δ_{l_0} and δ_{l_1} in Eqs. C.3 and C.5 are Kronecker δ symbols; that is, $\delta_{ll'} = 0$ for $l \neq l'$ and $\delta_{ll'} = 1$ for $l = l'$.

APPENDIX D
 ENDF/B Listing of Helium

2000,0	3.96822	0	0	0	01088	1451	1
0,0	0,0	0	0	74	01088	1451	2
HELIUM CROSS SECTIONS MATERIAL 1088					1088	1451	3
COMPILED BY ED PENNINGTON, ARGONNE NATIONAL LAB., IN JUNE 1968.					1088	1451	4
NATURAL HELIUM CONSISTS OF 0.00013 PER CENT HE-3 AND 99.99987 PER					1088	1451	5
CENT HE-4,					1088	1451	6
BECAUSE OF THE LOW ABUNDANCE OF HE-3, ONLY ITS (N,P) CROSS					1088	1451	7
SECTION, WHICH IS VERY LARGE AT LOW ENERGIES, NEED BE CONSIDERED,					1088	1451	8
ELASTIC SCATTERING IS THE ONLY POSSIBLE REACTION FOR NEUTRONS					1088	1451	9
INCIDENT ON HE-4 AT ENERGIES BELOW 15 MEV. THUS THE ELASTIC					1088	1451	10
SCATTERING CROSS SECTION AND VALUES OF MU BAR(LAB), XI, AND GAMMA					1088	1451	11
ARE GIVEN IN FILE 3, AND ELASTIC SCATTERING LEGENDRE COEFFICIENTS					1088	1451	12
ARE GIVEN IN FILE 4. PARAMETERS FOR A FREE GAS THERMAL SCATTERING					1088	1451	13
LAW ARE IN FILE 7,					1088	1451	14
THE ELASTIC SCATTERING CROSS SECTION AND THE LEGENDRE EXPANSION					1088	1451	15
COEFFICIENTS WERE CALCULATED FROM S-,P-, AND D-WAVE PHASE SHIFTS					1088	1451	16
USING A FORTRAN PROGRAM WRITTEN FOR THE PURPOSE, THE PHASE SHIFTS					1088	1451	17
WERE READ FROM SMOOTH CURVES BASED ON TABLE I OF REF.1. AT					1088	1451	18
ENERGIES BELOW THE 300 KEV, LOWER LIMIT OF TABLE I, EACH OF THE					1088	1451	19
TWO P-WAVE PHASE SHIFTS WAS OBTAINED BY ASSUMING A FUNCTIONAL					1088	1451	20
FORM BASED ON THE LOW ENERGY LIMIT FOR A SINGLE P-WAVE RESONANCE,					1088	1451	21
WITH PARAMETERS DETERMINED FROM FITTING THE LOW ENERGY PHASE					1088	1451	22
SHIFTS OF TABLE I, THE S-WAVE PHASE SHIFT BELOW 300 KEV, WAS					1088	1451	23
CALCULATED USING HARD SPHERE SCATTERING AND A NUCLEAR RADIUS, A=					1088	1451	24
2.4 FERMI, THIS YIELDS THE THERMAL SCATTERING CROSS SECTION =					1088	1451	25
4.*PI*A**2= 0.7238 BARNS IN AGREEMENT WITH THE EXPERIMENTAL VALUE					1088	1451	26
OF 0.73+- 0.05 BARNS (REF.2). THE LOW ENERGY S-WAVE PHASE SHIFTS					1088	1451	27
OF REF.1 ARE CONSISTENT WITH A NUCLEAR RADIUS OF ABOUT 2.48					1088	1451	28
FERMI, AND SO WOULD YIELD A SOMEWHAT HIGH THERMAL CROSS SECTION.					1088	1451	29
VALUES OF MU BAR(LAB), XI, AND GAMMA WERE CALCULATED FROM THE					1088	1451	30
LEGENDRE COEFFICIENTS USING A FORTRAN PROGRAM, MUXIGA. THIS					1088	1451	31
PROGRAM USES THE EQUATIONS OF REF.3-5,					1088	1451	32
AN ELASTIC SCATTERING TRANSFORMATION MATRIX FROM THE CENTER-OF-					1088	1451	33
MASS TO THE LABORATORY SYSTEM WAS COMPUTED USING CHAD (REF.6),					1088	1451	34
THE (N,P) CROSS SECTION FOR HE-3 IS THAT RECOMMENDED IN THE					1088	1451	35
EVALUATION OF HE-3 BY J. ALS-NIELSEN GIVEN IN REF.7. EXTENSION					1088	1451	36
FROM 10 TO 15 MEV. WAS MADE USING LINEAR EXTRAPOLATION ON A					1088	1451	37
LOG SIGMA= LOG E SCALE.					1088	1451	38
THE TOTAL CROSS SECTION IS THE SUM OF THE ELASTIC SCATTERING AND					1088	1451	39
(N,P) CROSS SECTIONS.					1088	1451	40
COMMENTS.					1088	1451	41
THE PHASE SHIFTS OF REF.1 ARE OPTICAL MODEL PHASE SHIFTS CHOSEN					1088	1451	42
TO FIT BOTH ANGULAR DISTRIBUTION AND POLARIZATION DATA AT MANY					1088	1451	43
ENERGIES. THE TOTAL SCATTERING CROSS SECTION IS ALSO FIT WITHIN					1088	1451	44
THE SCATTER OF THE EXPERIMENTAL POINTS, ANOTHER RECENT SET OF					1088	1451	45
PHASE SHIFTS (REF.8) IS NOT VERY DIFFERENT FROM THOSE USED HERE,					1088	1451	46
AND COULD ALSO HAVE BEEN USED IN THE PRESENT WORK, THERE SHOULD					1088	1451	47
BE NO SERIOUS DISAGREEMENTS WITH EXPERIMENTAL VALUES IN THE HE-4					1088	1451	48
DATA CALCULATED FROM THE PHASE SHIFTS,					1088	1451	49
AS DISCUSSED IN REF.7, THE HE-3 (N,P) CROSS SECTION IS RATHER					1088	1451	50
WELL KNOWN. PROBABLY MORE ERROR IS INTRODUCED INTO THE (N,P)					1088	1451	51
CROSS SECTION FOR NATURAL HELIUM BY THE UNCERTAINTY IN THE HE-3					1088	1451	52
ISOTOPIC ABUNDANCE THAN BY THE UNCERTAINTY IN THE HE-3 (N,P)					1088	1451	53
CROSS SECTION ITSELF.					1088	1451	54
PREVIOUS EVALUATIONS OF HELIUM FOR REACTOR CALCULATIONS INCLUDE					1088	1451	55
THOSE OF J.J.SCHMIDT (REF.9) AND B.R.S.BUCKINGHAM ET AL (REF.10).					1088	1451	56
SCHMIDT-S EVALUATION INCLUDES THE (N,P) CROSS SECTION FOR HE-3,					1088	1451	57
AND SIGMA ELASTIC, MU BAR(LAB), AND A SET OF PHASE SHIFTS FOR					1088	1451	58
HE-4, BUCKINGHAM ET AL GIVE SEPARATE EVALUATIONS FOR HE-3 AND					1088	1451	59
HE-4, FOR HE-3 ELASTIC, (N,P), (N,D), AND (N,2N) CROSS SECTIONS					1088	1451	60
ARE GIVEN, AS WELL AS ELASTIC ANGULAR DISTRIBUTIONS. THE HE-4					1088	1451	61
EVALUATION GIVES THE ELASTIC CROSS SECTION AND ANGULAR					1088	1451	62

DISTRIBUTIONS.				1088	1451	63
THE PRESENT COMPILATION WILL BE DESCRIBED IN DETAIL IN REF.11,				1088	1451	64
REFERENCES-				1088	1451	65
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10.B.R.S.BUCKINGHAM ET AL AWRE O-28/60,(1961),				1088	1451	75
11.E.M.PENNINGTON ANL-7462,(TO BE ISSUED),				1088	1451	76
0.0	0.0	0	0	0	01088	1 0 77
0.0	0.0	0	0	0	01088	0 0 78
2000.0	3.96822	0	0	0	01088	3 1 79
0.0	0.0	0	0	1	1421088	3 1 80
142	3				1088	3 1 81
1.00E-05	1.0721E+00	2.00E-05	0.9701E+00	3.00E-05	0.9249E+00	1088 3 1 82
5.00E-05	0.8796E+00	7.00E-05	0.8555E+00	1.00E-04	0.8339E+00	1088 3 1 83
2.00E-04	0.8017E+00	3.00E-04	0.7874E+00	5.00E-04	0.7731E+00	1088 3 1 84
7.00E-04	0.7654E+00	1.00E-03	0.7586E+00	2.00E-03	0.7484E+00	1088 3 1 85
3.00E-03	0.7439E+00	5.00E-03	0.7394E+00	7.00E-03	0.7370E+00	1088 3 1 86
1.00E-02	0.7348E+00	2.00E-02	0.7316E+00	2.53E-02	0.7307E+00	1088 3 1 87
3.00E-02	0.7302E+00	5.00E-02	0.7287E+00	7.00E-02	0.7280E+00	1088 3 1 88
1.00E-01	0.7273E+00	2.00E-01	0.7263E+00	3.00E-01	0.7258E+00	1088 3 1 89
5.00E-01	0.7254E+00	7.00E-01	0.7251E+00	1.00E+00	0.7249E+00	1088 3 1 90
2.00E+00	0.7246E+00	3.00E+00	0.7244E+00	5.00E+00	0.7243E+00	1088 3 1 91
7.00E+00	0.7242E+00	1.00E+01	0.7241E+00	2.00E+01	0.7240E+00	1088 3 1 92
3.00E+01	0.7240E+00	5.00E+01	0.7240E+00	7.00E+01	0.7239E+00	1088 3 1 93
1.00E+02	0.7239E+00	2.00E+02	0.7239E+00	3.00E+02	0.7239E+00	1088 3 1 94
5.00E+02	0.7238E+00	7.00E+02	0.7238E+00	1.00E+03	0.7238E+00	1088 3 1 95
2.00E+03	0.7237E+00	3.00E+03	0.7237E+00	5.00E+03	0.7236E+00	1088 3 1 96
7.00E+03	0.7236E+00	1.00E+04	0.7235E+00	2.00E+04	0.7235E+00	1088 3 1 97
3.00E+04	0.7234E+00	5.00E+04	0.7241E+00	7.00E+04	0.7256E+00	1088 3 1 98
1.00E+05	0.7297E+00	1.50E+05	0.7425E+00	2.00E+05	0.7644E+00	1088 3 1 99
2.50E+05	0.7977E+00	3.00E+05	0.8978E+00	3.50E+05	0.9654E+00	1088 3 1 100
4.00E+05	0.1056E+01	4.50E+05	0.1197E+01	5.00E+05	0.1373E+01	1088 3 1 101
5.50E+05	0.1581E+01	6.00E+05	0.1826E+01	6.50E+05	0.2168E+01	1088 3 1 102
7.00E+05	0.2576E+01	7.50E+05	0.3076E+01	8.00E+05	0.3750E+01	1088 3 1 103
8.50E+05	0.4380E+01	9.00E+05	0.5114E+01	9.50E+05	0.5844E+01	1088 3 1 104
1.00E+06	0.6525E+01	1.05E+06	0.7038E+01	1.10E+06	0.7321E+01	1088 3 1 105
1.13E+06	0.7424E+01	1.15E+06	0.7456E+01	1.17E+06	0.7461E+01	1088 3 1 106
1.20E+06	0.7432E+01	1.25E+06	0.7278E+01	1.30E+06	0.7040E+01	1088 3 1 107
1.35E+06	0.6757E+01	1.40E+06	0.6453E+01	1.45E+06	0.6157E+01	1088 3 1 108
1.50E+06	0.5875E+01	1.60E+06	0.5333E+01	1.70E+06	0.4882E+01	1088 3 1 109
1.80E+06	0.4509E+01	1.90E+06	0.4211E+01	2.00E+06	0.3944E+01	1088 3 1 110
2.10E+06	0.3734E+01	2.20E+06	0.3551E+01	2.30E+06	0.3399E+01	1088 3 1 111
2.40E+06	0.3273E+01	2.50E+06	0.3169E+01	2.60E+06	0.3071E+01	1088 3 1 112
2.70E+06	0.2988E+01	2.80E+06	0.2911E+01	2.90E+06	0.2849E+01	1088 3 1 113
3.00E+06	0.2789E+01	3.20E+06	0.2684E+01	3.40E+06	0.2595E+01	1088 3 1 114
3.60E+06	0.2524E+01	3.80E+06	0.2469E+01	4.00E+06	0.2424E+01	1088 3 1 115
4.20E+06	0.2373E+01	4.40E+06	0.2325E+01	4.60E+06	0.2278E+01	1088 3 1 116
4.80E+06	0.2232E+01	5.00E+06	0.2190E+01	5.20E+06	0.2149E+01	1088 3 1 117
5.40E+06	0.2107E+01	5.60E+06	0.2070E+01	5.80E+06	0.2031E+01	1088 3 1 118
6.00E+06	0.1994E+01	6.20E+06	0.1957E+01	6.40E+06	0.1921E+01	1088 3 1 119
6.60E+06	0.1887E+01	6.80E+06	0.1853E+01	7.00E+06	0.1821E+01	1088 3 1 120
7.20E+06	0.1787E+01	7.40E+06	0.1756E+01	7.60E+06	0.1726E+01	1088 3 1 121
7.80E+06	0.1696E+01	8.00E+06	0.1667E+01	8.20E+06	0.1640E+01	1088 3 1 122
8.40E+06	0.1612E+01	8.60E+06	0.1585E+01	8.80E+06	0.1559E+01	1088 3 1 123
9.00E+06	0.1534E+01	9.20E+06	0.1509E+01	9.40E+06	0.1485E+01	1088 3 1 124

9.60E+06	0.1462E+01	9.80E+06	0.1439E+01	1.00E+07	0.1418E+011088	3	1	125
1.05E+07	0.1365E+01	1.10E+07	0.1315E+01	1.15E+07	0.1268E+011088	3	1	126
1.20E+07	0.1224E+01	1.25E+07	0.1180E+01	1.30E+07	0.1140E+011088	3	1	127
1.35E+07	0.1102E+01	1.40E+07	0.1066E+01	1.45E+07	0.1032E+011088	3	1	128
1.50E+07	0.9992E+00				1088	3	1	129
0.0	0.0	0	0	0	01088	3	0	130
2000.0	3.96822	0	0	0	01088	3	2	131
0.0	0.0	0	0	1	1421088	3	2	132
142	3				1088	3	2	133
1.00E-05	0.7238E+00	2.00E-05	0.7238E+00	3.00E-05	0.7238E+001088	3	2	134
5.00E-05	0.7238E+00	7.00E-05	0.7238E+00	1.00E-04	0.7238E+001088	3	2	135
2.00E-04	0.7238E+00	3.00E-04	0.7238E+00	5.00E-04	0.7238E+001088	3	2	136
7.00E-04	0.7238E+00	1.00E-03	0.7238E+00	2.00E-03	0.7238E+001088	3	2	137
3.00E-03	0.7238E+00	5.00E-03	0.7238E+00	7.00E-03	0.7238E+001088	3	2	138
1.00E-02	0.7238E+00	2.00E-02	0.7238E+00	2.53E-02	0.7238E+001088	3	2	139
3.00E-02	0.7238E+00	5.00E-02	0.7238E+00	7.00E-02	0.7238E+001088	3	2	140
1.00E-01	0.7238E+00	2.00E-01	0.7238E+00	3.00E-01	0.7238E+001088	3	2	141
5.00E-01	0.7238E+00	7.00E-01	0.7238E+00	1.00E+00	0.7238E+001088	3	2	142
2.00E+00	0.7238E+00	3.00E+00	0.7238E+00	5.00E+00	0.7238E+001088	3	2	143
7.00E+00	0.7238E+00	1.00E+01	0.7238E+00	2.00E+01	0.7238E+001088	3	2	144
3.00E+01	0.7238E+00	5.00E+01	0.7238E+00	7.00E+01	0.7238E+001088	3	2	145
1.00E+02	0.7238E+00	2.00E+02	0.7238E+00	3.00E+02	0.7238E+001088	3	2	146
5.00E+02	0.7238E+00	7.00E+02	0.7238E+00	1.00E+03	0.7238E+001088	3	2	147
2.00E+03	0.7237E+00	3.00E+03	0.7237E+00	5.00E+03	0.7236E+001088	3	2	148
7.00E+03	0.7236E+00	1.00E+04	0.7235E+00	2.00E+04	0.7235E+001088	3	2	149
3.00E+04	0.7234E+00	5.00E+04	0.7241E+00	7.00E+04	0.7256E+001088	3	2	150
1.00E+05	0.7297E+00	1.50E+05	0.7425E+00	2.00E+05	0.7644E+001088	3	2	151
2.50E+05	0.7977E+00	3.00E+05	0.8978E+00	3.50E+05	0.9654E+001088	3	2	152
4.00E+05	0.1056E+01	4.50E+05	0.1197E+01	5.00E+05	0.1373E+011088	3	2	153
5.50E+05	0.1581E+01	6.00E+05	0.1826E+01	6.50E+05	0.2168E+011088	3	2	154
7.00E+05	0.2576E+01	7.50E+05	0.3076E+01	8.00E+05	0.3750E+011088	3	2	155
8.50E+05	0.4380E+01	9.00E+05	0.5114E+01	9.50E+05	0.5844E+011088	3	2	156
1.00E+06	0.6525E+01	1.05E+06	0.7038E+01	1.10E+06	0.7321E+011088	3	2	157
1.13E+06	0.7424E+01	1.15E+06	0.7456E+01	1.17E+06	0.7461E+011088	3	2	158
1.20E+06	0.7432E+01	1.25E+06	0.7278E+01	1.30E+06	0.7040E+011088	3	2	159
1.35E+06	0.6757E+01	1.40E+06	0.6453E+01	1.45E+06	0.6157E+011088	3	2	160
1.50E+06	0.5875E+01	1.60E+06	0.5333E+01	1.70E+06	0.4882E+011088	3	2	161
1.80E+06	0.4509E+01	1.90E+06	0.4211E+01	2.00E+06	0.3944E+011088	3	2	162
2.10E+06	0.3734E+01	2.20E+06	0.3551E+01	2.30E+06	0.3399E+011088	3	2	163
2.40E+06	0.3273E+01	2.50E+06	0.3169E+01	2.60E+06	0.3071E+011088	3	2	164
2.70E+06	0.2988E+01	2.80E+06	0.2911E+01	2.90E+06	0.2849E+011088	3	2	165
3.00E+06	0.2789E+01	3.20E+06	0.2684E+01	3.40E+06	0.2595E+011088	3	2	166
3.60E+06	0.2524E+01	3.80E+06	0.2469E+01	4.00E+06	0.2424E+011088	3	2	167
4.20E+06	0.2373E+01	4.40E+06	0.2325E+01	4.60E+06	0.2278E+011088	3	2	168
4.80E+06	0.2232E+01	5.00E+06	0.2190E+01	5.20E+06	0.2149E+011088	3	2	169
5.40E+06	0.2107E+01	5.60E+06	0.2070E+01	5.80E+06	0.2031E+011088	3	2	170
6.00E+06	0.1994E+01	6.20E+06	0.1957E+01	6.40E+06	0.1921E+011088	3	2	171
6.60E+06	0.1887E+01	6.80E+06	0.1853E+01	7.00E+06	0.1821E+011088	3	2	172
7.20E+06	0.1787E+01	7.40E+06	0.1756E+01	7.60E+06	0.1726E+011088	3	2	173
7.80E+06	0.1696E+01	8.00E+06	0.1667E+01	8.20E+06	0.1640E+011088	3	2	174
8.40E+06	0.1612E+01	8.60E+06	0.1585E+01	8.80E+06	0.1559E+011088	3	2	175
9.00E+06	0.1534E+01	9.20E+06	0.1509E+01	9.40E+06	0.1485E+011088	3	2	176
9.60E+06	0.1462E+01	9.80E+06	0.1439E+01	1.00E+07	0.1418E+011088	3	2	177
1.05E+07	0.1365E+01	1.10E+07	0.1315E+01	1.15E+07	0.1268E+011088	3	2	178
1.20E+07	0.1224E+01	1.25E+07	0.1180E+01	1.30E+07	0.1140E+011088	3	2	179
1.35E+07	0.1102E+01	1.40E+07	0.1066E+01	1.45E+07	0.1032E+011088	3	2	180
1.50E+07	0.9992E+00				1088	3	2	181
0.0	0.0	0	0	0	01088	3	0	182
2000.0	3.96822	0	0	0	01088	3103		183
0.0	0.7644E+06	0	0	1	1421088	3103		184
142	5				1088	3103		185
1.00E-05	0.3483E+00	2.00E-05	0.2463E+00	3.00E-05	0.2011E+001088	3103		186

5.00E-05	0.1558E+00	7.00E-05	0.1317E+00	1.00E-04	0.1101E+00	1088	3103	187
2.00E-04	0.7789E-01	3.00E-04	0.6359E-01	5.00E-04	0.4926E-01	1088	3103	188
7.00E-04	0.4163E-01	1.00E-03	0.3483E-01	2.00E-03	0.2463E-01	1088	3103	189
3.00E-03	0.2011E-01	5.00E-03	0.1558E-01	7.00E-03	0.1316E-01	1088	3103	190
1.00E-02	0.1101E-01	2.00E-02	0.7787E-02	2.53E-02	0.6924E-02	1088	3103	191
3.00E-02	0.6358E-02	5.00E-02	0.4924E-02	7.00E-02	0.4161E-02	1088	3103	192
1.00E-01	0.3481E-02	2.00E-01	0.2461E-02	3.00E-01	0.2010E-02	1088	3103	193
5.00E-01	0.1556E-02	7.00E-01	0.1316E-02	1.00E+00	0.1100E-02	1088	3103	194
2.00E+00	0.7773E-03	3.00E+00	0.6344E-03	5.00E+00	0.4910E-03	1088	3103	195
7.00E+00	0.4147E-03	1.00E+01	0.3467E-03	2.00E+01	0.2448E-03	1088	3103	196
3.00E+01	0.1996E-03	5.00E+01	0.1542E-03	7.00E+01	0.1301E-03	1088	3103	197
1.00E+02	0.1086E-03	2.00E+02	0.7631E-04	3.00E+02	0.6201E-04	1088	3103	198
5.00E+02	0.4771E-04	7.00E+02	0.4004E-04	1.00E+03	0.3328E-04	1088	3103	199
2.00E+03	0.2314E-04	3.00E+03	0.1859E-04	5.00E+03	0.1417E-04	1088	3103	200
7.00E+03	0.1183E-04	1.00E+04	0.9880E-05	2.00E+04	0.6825E-05	1088	3103	201
3.00E+04	0.5330E-05	5.00E+04	0.3900E-05	7.00E+04	0.3185E-05	1088	3103	202
1.00E+05	0.2574E-05	1.50E+05	0.2067E-05	2.00E+05	0.1755E-05	1088	3103	203
2.50E+05	0.1560E-05	3.00E+05	0.1430E-05	3.50E+05	0.1313E-05	1088	3103	204
4.00E+05	0.1248E-05	4.50E+05	0.1196E-05	5.00E+05	0.1183E-05	1088	3103	205
5.50E+05	0.1170E-05	6.00E+05	0.1157E-05	6.50E+05	0.1157E-05	1088	3103	206
7.00E+05	0.1157E-05	7.50E+05	0.1157E-05	8.00E+05	0.1157E-05	1088	3103	207
8.50E+05	0.1157E-05	9.00E+05	0.1157E-05	9.50E+05	0.1157E-05	1088	3103	208
1.00E+06	0.1157E-05	1.05E+06	0.1157E-05	1.10E+06	0.1157E-05	1088	3103	209
1.13E+06	0.1157E-05	1.15E+06	0.1157E-05	1.17E+06	0.1157E-05	1088	3103	210
1.20E+06	0.1157E-05	1.25E+06	0.1157E-05	1.30E+06	0.1157E-05	1088	3103	211
1.35E+06	0.1157E-05	1.40E+06	0.1157E-05	1.45E+06	0.1157E-05	1088	3103	212
1.50E+06	0.1157E-05	1.60E+06	0.1151E-05	1.70E+06	0.1144E-05	1088	3103	213
1.80E+06	0.1138E-05	1.90E+06	0.1118E-05	2.00E+06	0.1092E-05	1088	3103	214
2.10E+06	0.1066E-05	2.20E+06	0.1040E-05	2.30E+06	0.1014E-05	1088	3103	215
2.40E+06	0.9880E-06	2.50E+06	0.9620E-06	2.60E+06	0.9360E-06	1088	3103	216
2.70E+06	0.9100E-06	2.80E+06	0.8840E-06	2.90E+06	0.8580E-06	1088	3103	217
3.00E+06	0.8320E-06	3.20E+06	0.7800E-06	3.40E+06	0.7280E-06	1088	3103	218
3.60E+06	0.6825E-06	3.80E+06	0.6435E-06	4.00E+06	0.6110E-06	1088	3103	219
4.20E+06	0.5785E-06	4.40E+06	0.5460E-06	4.60E+06	0.5265E-06	1088	3103	220
4.80E+06	0.5005E-06	5.00E+06	0.4810E-06	5.20E+06	0.4615E-06	1088	3103	221
5.40E+06	0.4420E-06	5.60E+06	0.4225E-06	5.80E+06	0.4095E-06	1088	3103	222
6.00E+06	0.3965E-06	6.20E+06	0.3770E-06	6.40E+06	0.3640E-06	1088	3103	223
6.60E+06	0.3510E-06	6.80E+06	0.3406E-06	7.00E+06	0.3315E-06	1088	3103	224
7.20E+06	0.3211E-06	7.40E+06	0.3133E-06	7.60E+06	0.3055E-06	1088	3103	225
7.80E+06	0.2977E-06	8.00E+06	0.2912E-06	8.20E+06	0.2847E-06	1088	3103	226
8.40E+06	0.2769E-06	8.60E+06	0.2717E-06	8.80E+06	0.2665E-06	1088	3103	227
9.00E+06	0.2600E-06	9.20E+06	0.2548E-06	9.40E+06	0.2483E-06	1088	3103	228
9.60E+06	0.2431E-06	9.80E+06	0.2379E-06	1.00E+07	0.2340E-06	1088	3103	229
1.05E+07	0.2236E-06	1.10E+07	0.2145E-06	1.15E+07	0.2054E-06	1088	3103	230
1.20E+07	0.1976E-06	1.25E+07	0.1898E-06	1.30E+07	0.1833E-06	1088	3103	231
1.35E+07	0.1768E-06	1.40E+07	0.1703E-06	1.45E+07	0.1651E-06	1088	3103	232
1.50E+07	0.1599E-06					1088	3103	233
0.0	0.0	0	0	0	0	01088	3	0
2000.0	3.96822	0	0	0	0	01088	3251	235
0.0	0.0	0	0	1	1	1081088	3251	236
108	3					1088	3251	237
1.00E-05	0.1680E+00	2.53E-02	0.1680E+00	1.00E+02	0.1679E+00	1088	3251	238
2.00E-02	0.1678E+00	3.00E+02	0.1677E+00	5.00E+02	0.1675E+00	1088	3251	239
7.00E-02	0.1672E+00	1.00E+03	0.1669E+00	2.00E+03	0.1658E+00	1088	3251	240
3.00E+03	0.1647E+00	5.00E+03	0.1625E+00	7.00E+03	0.1603E+00	1088	3251	241
1.00E+04	0.1570E+00	2.00E+04	0.1458E+00	3.00E+04	0.1344E+00	1088	3251	242
5.00E+04	0.1116E+00	7.00E+04	0.8798E-01	1.00E+05	0.5208E-01	1088	3251	243
1.50E+05	0.9740E-02	2.00E+05	0.7161E-01	2.50E+05	0.1304E+00	1088	3251	244
3.00E+05	0.1739E+00	3.50E+05	0.2185E+00	4.00E+05	0.2518E+00	1088	3251	245
4.50E+05	0.2702E+00	5.00E+05	0.2746E+00	5.50E+05	0.2658E+00	1088	3251	246
6.00E+05	0.2457E+00	6.50E+05	0.2143E+00	7.00E+05	0.1776E+00	1088	3251	247
7.50E+05	0.1357E+00	8.00E+05	0.8704E-01	8.50E+05	0.4441E-01	1088	3251	248

9.00E+05	0.5200E-04	9.50E+05	0.4267E-01	1.00E+06	0.8390E-01	1088	3251	249
1.05E+06	0.1213E+00	1.10E+06	0.1529E+00	1.13E+06	0.1720E+00	1088	3251	250
1.15E+06	0.1836E+00	1.17E+06	0.1948E+00	1.20E+06	0.2115E+00	1088	3251	251
1.25E+06	0.2370E+00	1.30E+06	0.2585E+00	1.35E+06	0.2784E+00	1088	3251	252
1.40E+06	0.2967E+00	1.45E+06	0.3122E+00	1.50E+06	0.3258E+00	1088	3251	253
1.60E+06	0.3520E+00	1.70E+06	0.3718E+00	1.80E+06	0.3878E+00	1088	3251	254
1.90E+06	0.4002E+00	2.00E+06	0.4104E+00	2.10E+06	0.4185E+00	1088	3251	255
2.20E+06	0.4255E+00	2.30E+06	0.4315E+00	2.40E+06	0.4363E+00	1088	3251	256
2.50E+06	0.4402E+00	2.60E+06	0.4434E+00	2.70E+06	0.4460E+00	1088	3251	257
2.80E+06	0.4489E+00	2.90E+06	0.4512E+00	3.00E+06	0.4530E+00	1088	3251	258
3.20E+06	0.4585E+00	3.40E+06	0.4634E+00	3.60E+06	0.4675E+00	1088	3251	259
3.80E+06	0.4710E+00	4.00E+06	0.4749E+00	4.20E+06	0.4795E+00	1088	3251	260
4.40E+06	0.4845E+00	4.60E+06	0.4892E+00	4.80E+06	0.4940E+00	1088	3251	261
5.00E+06	0.4987E+00	5.20E+06	0.5035E+00	5.40E+06	0.5077E+00	1088	3251	262
5.60E+06	0.5117E+00	5.80E+06	0.5153E+00	6.00E+06	0.5195E+00	1088	3251	263
6.20E+06	0.5231E+00	6.40E+06	0.5264E+00	6.60E+06	0.5301E+00	1088	3251	264
6.80E+06	0.5333E+00	7.00E+06	0.5365E+00	7.20E+06	0.5390E+00	1088	3251	265
7.40E+06	0.5418E+00	7.60E+06	0.5443E+00	7.80E+06	0.5470E+00	1088	3251	266
8.00E+06	0.5492E+00	8.20E+06	0.5513E+00	8.40E+06	0.5530E+00	1088	3251	267
8.60E+06	0.5549E+00	8.80E+06	0.5565E+00	9.00E+06	0.5584E+00	1088	3251	268
9.20E+06	0.5603E+00	9.40E+06	0.5618E+00	9.60E+06	0.5635E+00	1088	3251	269
9.80E+06	0.5649E+00	1.00E+07	0.5666E+00	1.05E+07	0.5696E+00	1088	3251	270
1.10E+07	0.5728E+00	1.15E+07	0.5756E+00	1.20E+07	0.5783E+00	1088	3251	271
1.25E+07	0.5804E+00	1.30E+07	0.5828E+00	1.35E+07	0.5850E+00	1088	3251	272
1.40E+07	0.5872E+00	1.45E+07	0.5894E+00	1.50E+07	0.5917E+00	1088	3251	273
0.0	0.0	0	0	0	0	1088	3	274
2000.0	3.96822	0	0	0	0	1088	3252	275
0.0	0.0	0	0	1	1081088	3252	276	
108	3				1088	3252	277	
1.00E-05	0.4282E+00	2.53E-02	0.4282E+00	1.00E+02	0.4282E+00	1088	3252	278
2.00E+02	0.4283E+00	3.00E+02	0.4284E+00	5.00E+02	0.4285E+00	1088	3252	279
7.00E+02	0.4286E+00	1.00E+03	0.4287E+00	2.00E+03	0.4293E+00	1088	3252	280
3.00E+03	0.4299E+00	5.00E+03	0.4310E+00	7.00E+03	0.4322E+00	1088	3252	281
1.00E+04	0.4339E+00	2.00E+04	0.4397E+00	3.00E+04	0.4455E+00	1088	3252	282
5.00E+04	0.4574E+00	7.00E+04	0.4696E+00	1.00E+05	0.4881E+00	1088	3252	283
1.50E+05	0.5201E+00	2.00E+05	0.5521E+00	2.50E+05	0.5826E+00	1088	3252	284
3.00E+05	0.6051E+00	3.50E+05	0.6281E+00	4.00E+05	0.6454E+00	1088	3252	285
4.50E+05	0.6550E+00	5.00E+05	0.6572E+00	5.50E+05	0.6527E+00	1088	3252	286
6.00E+05	0.6423E+00	6.50E+05	0.6261E+00	7.00E+05	0.6071E+00	1088	3252	287
7.50E+05	0.5855E+00	8.00E+05	0.5603E+00	8.50E+05	0.5382E+00	1088	3252	288
9.00E+05	0.5152E+00	9.50E+05	0.4932E+00	1.00E+06	0.4719E+00	1088	3252	289
1.05E+06	0.4525E+00	1.10E+06	0.4362E+00	1.13E+06	0.4263E+00	1088	3252	290
1.15E+06	0.4203E+00	1.17E+06	0.4145E+00	1.20E+06	0.4059E+00	1088	3252	291
1.25E+06	0.3927E+00	1.30E+06	0.3816E+00	1.35E+06	0.3712E+00	1088	3252	292
1.40E+06	0.3618E+00	1.45E+06	0.3538E+00	1.50E+06	0.3467E+00	1088	3252	293
1.60E+06	0.3331E+00	1.70E+06	0.3229E+00	1.80E+06	0.3146E+00	1088	3252	294
1.90E+06	0.3082E+00	2.00E+06	0.3029E+00	2.10E+06	0.2988E+00	1088	3252	295
2.20E+06	0.2951E+00	2.30E+06	0.2920E+00	2.40E+06	0.2895E+00	1088	3252	296
2.50E+06	0.2875E+00	2.60E+06	0.2858E+00	2.70E+06	0.2845E+00	1088	3252	297
2.80E+06	0.2830E+00	2.90E+06	0.2818E+00	3.00E+06	0.2809E+00	1088	3252	298
3.20E+06	0.2781E+00	3.40E+06	0.2755E+00	3.60E+06	0.2734E+00	1088	3252	299
3.80E+06	0.2716E+00	4.00E+06	0.2696E+00	4.20E+06	0.2672E+00	1088	3252	300
4.40E+06	0.2646E+00	4.60E+06	0.2622E+00	4.80E+06	0.2597E+00	1088	3252	301
5.00E+06	0.2573E+00	5.20E+06	0.2548E+00	5.40E+06	0.2526E+00	1088	3252	302
5.60E+06	0.2506E+00	5.80E+06	0.2487E+00	6.00E+06	0.2465E+00	1088	3252	303
6.20E+06	0.2447E+00	6.40E+06	0.2430E+00	6.60E+06	0.2411E+00	1088	3252	304
6.80E+06	0.2394E+00	7.00E+06	0.2378E+00	7.20E+06	0.2365E+00	1088	3252	305
7.40E+06	0.2350E+00	7.60E+06	0.2337E+00	7.80E+06	0.2323E+00	1088	3252	306
8.00E+06	0.2312E+00	8.20E+06	0.2301E+00	8.40E+06	0.2293E+00	1088	3252	307
8.60E+06	0.2283E+00	8.80E+06	0.2274E+00	9.00E+06	0.2265E+00	1088	3252	308
9.20E+06	0.2255E+00	9.40E+06	0.2247E+00	9.60E+06	0.2238E+00	1088	3252	309
9.80E+06	0.2231E+00	1.00E+07	0.2222E+00	1.05E+07	0.2207E+00	1088	3252	310

1.10E+07	0.2190E+00	1.15E+07	0.2176E+00	1.20E+07	0.2162E+00	0.01088	3252	311
1.25E+07	0.2151E+00	1.30E+07	0.2139E+00	1.35E+07	0.2127E+00	0.01088	3252	312
1.40E+07	0.2116E+00	1.45E+07	0.2104E+00	1.50E+07	0.2093E+00	0.01088	3252	313
0.0	0.0	0	0	0	0	0.01088	3	0
2000.0	3.96822	0	0	0	0	0.01088	3253	315
0.0	0.0	0	0	1	1081088	0.01088	3253	316
108	3				1088	0.01088	3253	317
1.00E-05	0.3121E+00	2.53E-02	0.3121E+00	1.00E+02	0.3121E+00	0.01088	3253	318
2.00E+02	0.3122E+00	3.00E+02	0.3122E+00	5.00E+02	0.3122E+00	0.01088	3253	319
7.00E+02	0.3122E+00	1.00E+03	0.3123E+00	2.00E+03	0.3125E+00	0.01088	3253	320
3.00E+03	0.3127E+00	5.00E+03	0.3131E+00	7.00E+03	0.3135E+00	0.01088	3253	321
1.00E+04	0.3141E+00	2.00E+04	0.3161E+00	3.00E+04	0.3180E+00	0.01088	3253	322
5.00E+04	0.3219E+00	7.00E+04	0.3257E+00	1.00E+05	0.3312E+00	0.01088	3253	323
1.50E+05	0.3402E+00	2.00E+05	0.3485E+00	2.50E+05	0.3561E+00	0.01088	3253	324
3.00E+05	0.3617E+00	3.50E+05	0.3675E+00	4.00E+05	0.3724E+00	0.01088	3253	325
4.50E+05	0.3762E+00	5.00E+05	0.3790E+00	5.50E+05	0.3808E+00	0.01088	3253	326
6.00E+05	0.3818E+00	6.50E+05	0.3817E+00	7.00E+05	0.3809E+00	0.01088	3253	327
7.50E+05	0.3791E+00	8.00E+05	0.3765E+00	8.50E+05	0.3736E+00	0.01088	3253	328
9.00E+05	0.3702E+00	9.50E+05	0.3662E+00	1.00E+06	0.3618E+00	0.01088	3253	329
1.05E+06	0.3572E+00	1.10E+06	0.3530E+00	1.13E+06	0.3501E+00	0.01088	3253	330
1.15E+06	0.3482E+00	1.17E+06	0.3464E+00	1.20E+06	0.3435E+00	0.01088	3253	331
1.25E+06	0.3388E+00	1.30E+06	0.3344E+00	1.35E+06	0.3300E+00	0.01088	3253	332
1.40E+06	0.3256E+00	1.45E+06	0.3216E+00	1.50E+06	0.3179E+00	0.01088	3253	333
1.60E+06	0.3100E+00	1.70E+06	0.3034E+00	1.80E+06	0.2975E+00	0.01088	3253	334
1.90E+06	0.2925E+00	2.00E+06	0.2879E+00	2.10E+06	0.2842E+00	0.01088	3253	335
2.20E+06	0.2808E+00	2.30E+06	0.2779E+00	2.40E+06	0.2756E+00	0.01088	3253	336
2.50E+06	0.2738E+00	2.60E+06	0.2722E+00	2.70E+06	0.2711E+00	0.01088	3253	337
2.80E+06	0.2699E+00	2.90E+06	0.2691E+00	3.00E+06	0.2687E+00	0.01088	3253	338
3.20E+06	0.2671E+00	3.40E+06	0.2661E+00	3.60E+06	0.2658E+00	0.01088	3253	339
3.80E+06	0.2664E+00	4.00E+06	0.2671E+00	4.20E+06	0.2672E+00	0.01088	3253	340
4.40E+06	0.2671E+00	4.60E+06	0.2671E+00	4.80E+06	0.2670E+00	0.01088	3253	341
5.00E+06	0.2669E+00	5.20E+06	0.2666E+00	5.40E+06	0.2665E+00	0.01088	3253	342
5.60E+06	0.2664E+00	5.80E+06	0.2664E+00	6.00E+06	0.2661E+00	0.01088	3253	343
6.20E+06	0.2659E+00	6.40E+06	0.2656E+00	6.60E+06	0.2652E+00	0.01088	3253	344
6.80E+06	0.2648E+00	7.00E+06	0.2644E+00	7.20E+06	0.2641E+00	0.01088	3253	345
7.40E+06	0.2636E+00	7.60E+06	0.2634E+00	7.80E+06	0.2628E+00	0.01088	3253	346
8.00E+06	0.2624E+00	8.20E+06	0.2622E+00	8.40E+06	0.2620E+00	0.01088	3253	347
8.60E+06	0.2616E+00	8.80E+06	0.2614E+00	9.00E+06	0.2610E+00	0.01088	3253	348
9.20E+06	0.2604E+00	9.40E+06	0.2601E+00	9.60E+06	0.2597E+00	0.01088	3253	349
9.80E+06	0.2594E+00	1.00E+07	0.2590E+00	1.05E+07	0.2583E+00	0.01088	3253	350
1.10E+07	0.2576E+00	1.15E+07	0.2568E+00	1.20E+07	0.2559E+00	0.01088	3253	351
1.25E+07	0.2552E+00	1.30E+07	0.2543E+00	1.35E+07	0.2536E+00	0.01088	3253	352
1.40E+07	0.2529E+00	1.45E+07	0.2522E+00	1.50E+07	0.2515E+00	0.01088	3253	353
0.0	0.0	0	0	0	0	0.01088	3	0
0.0	0.0	0	0	0	0	0.01088	0	0
2000.0	3.96822	1	1	0	0	0.01088	4	2
0.0	3.96822	0	2	100	91088	0.01088	4	2
1.0000E+00	1.6800E-01	1.2819E-02	0.0	-6.6316E-05	0.0	0.01088	4	2
6.3701E-07	0.0	-7.4839E-09	0.0	0.0	9.6190E-01	0.01088	4	2
2.9686E-01	4.3546E-02	3.1027E-03	0.0	-1.4971E-05	0.0	0.01088	4	2
1.3935E-07	0.0	0.0	-1.5886E-01	9.0195E-01	4.1067E-01	0.01088	4	2
8.8718E-02	1.1085E-02	7.1925E-04	0.0	-3.1239E-06	0.0	0.01088	4	2
0.0	3.5863E-02	-2.7304E-01	8.1319E-01	5.0658E-01	1.4568E-01	0.01088	4	2
2.5474E-02	2.8077E-03	1.6752E-04	0.0	0.0	-8.5905E-03	0.01088	4	2
7.8689E-02	-3.6481E-01	7.0133E-01	5.8110E-01	2.1109E-01	4.7327E-01	0.01088	4	2
7.1261E-03	7.0975E-04	0.0	2.1026E-03	-2.2043E-02	1.2928E-01	0.01088	4	2
-4.3373E-01	5.7179E-01	6.3117E-01	2.8107E-01	7.7131E-02	1.4600E-02	0.01088	4	2
0.0	-5.1992E-04	6.0621E-03	-4.1723E-02	1.8451E-01	-4.7795E-01	0.01088	4	2
4.3070E-01	6.5479E-01	3.5139E-01	1.1474E-01	0.0	1.2929E-04	0.01088	4	2
-1.6456E-03	1.2786E-02	-6.7791E-02	2.4055E-01	-4.9642E-01	2.8461E-01	0.01088	4	2
6.5122E-01	4.1767E-01	0.0	-3.2264E-05	4.4243E-04	-3.7901E-03	0.01088	4	2
2.2986E-02	-9.9735E-02	2.9341E-01	-4.8921E-01	1.4018E-01	6.2111E-01	0.01088	4	2

0.0	8.0695E-06	-1.1807E-04	1.0976E-03	-7.4043E-03	3.7198E-02	1088	4	2	373
-1.3644E-01	3.3928E-01	-4.5769E-01	3.8210E-03			1088	4	2	374
0.0	0.0	0	0		1	1081088	4	2	375
108	3					1088	4	2	376
0.0	1.00E-05	0	0		1	01088	4	2	377
0.0		0	0			1088	4	2	378
0.0	2.53E-02	0	0		1	01088	4	2	379
0.0						1088	4	2	380
0.0	1.00E+02	0	0		2	01088	4	2	381
-1.130E-04	0.0					1088	4	2	382
0.0	2.00E+02	0	0		2	01088	4	2	383
-2.270E-04	0.0					1088	4	2	384
0.0	3.00E+02	0	0		2	01088	4	2	385
-3.400E-04	0.0					1088	4	2	386
0.0	5.00E+02	0	0		2	01088	4	2	387
-5.670E-04	0.0					1088	4	2	388
0.0	7.00E+02	0	0		2	01088	4	2	389
-7.940E-04	0.0					1088	4	2	390
0.0	1.00E+03	0	0		2	01088	4	2	391
-1.135E-03	0.0					1088	4	2	392
0.0	2.00E+03	0	0		2	01088	4	2	393
-2.272E-03	1.000E-06					1088	4	2	394
0.0	3.00E+03	0	0		2	01088	4	2	395
-3.410E-03	3.000E-06					1088	4	2	396
0.0	5.00E+03	0	0		2	01088	4	2	397
-5.691E-03	9.000E-06					1088	4	2	398
0.0	7.00E+03	0	0		2	01088	4	2	399
-7.979E-03	1.700E-05					1088	4	2	400
0.0	1.00E+04	0	0		2	01088	4	2	401
-1.142E-02	3.500E-05					1088	4	2	402
0.0	2.00E+04	0	0		2	01088	4	2	403
-2.303E-02	1.410E-04					1088	4	2	404
0.0	3.00E+04	0	0		2	01088	4	2	405
-3.483E-02	3.230E-04					1088	4	2	406
0.0	5.00E+04	0	0		2	01088	4	2	407
-5.853E-02	9.160E-04					1088	4	2	408
0.0	7.00E+04	0	0		2	01088	4	2	409
-8.289E-02	1.850E-03					1088	4	2	410
0.0	1.00E+05	0	0		2	01088	4	2	411
-1.199E-01	3.916E-03					1088	4	2	412
0.0	1.50E+05	0	0		2	01088	4	2	413
-1.832E-01	9.426E-03					1088	4	2	414
0.0	2.00E+05	0	0		2	01088	4	2	415
-2.462E-01	1.777E-02					1088	4	2	416
0.0	2.50E+05	0	0		2	01088	4	2	417
-3.054E-01	2.902E-02					1088	4	2	418
0.0	3.00E+05	0	0		2	01088	4	2	419
-3.487E-01	4.071E-02					1088	4	2	420
0.0	3.50E+05	0	0		2	01088	4	2	421
-3.924E-01	5.688E-02					1088	4	2	422
0.0	4.00E+05	0	0		2	01088	4	2	423
-4.240E-01	7.510E-02					1088	4	2	424
0.0	4.50E+05	0	0		2	01088	4	2	425
-4.401E-01	9.412E-02					1088	4	2	426
0.0	5.00E+05	0	0		2	01088	4	2	427
-4.414E-01	1.134E-01					1088	4	2	428
0.0	5.50E+05	0	0		2	01088	4	2	429
-4.291E-01	1.322E-01					1088	4	2	430
0.0	6.00E+05	0	0		2	01088	4	2	431
-4.053E-01	1.499E-01					1088	4	2	432
0.0	6.50E+05	0	0		2	01088	4	2	433
-3.704E-01	1.641E-01					1088	4	2	434

-3.301E-01	1.769E-01	1088	4	2	436
0.0	7.50E+05	1088	4	2	437
-2.852E-01	1.652E-01	1088	4	2	438
0.0	8.00E+05	1088	4	2	439
-2.333E-01	1.929E-01	1088	4	2	440
0.0	8.50E+05	1088	4	2	441
-1.884E-01	1.967E-01	1088	4	2	442
0.0	9.00E+05	1088	4	2	443
-1.416E-01	1.997E-01	1088	4	2	444
0.0	9.50E+05	1088	4	2	445
-9.717E-02	2.006E-01	1088	4	2	446
0.0	1.00E+06	1088	4	2	447
-5.435E-02	2.003E-01	1088	4	2	448
0.0	1.05E+06	1088	4	2	449
-1.572E-02	1.988E-01	1088	4	2	450
0.0	1.10E+06	1088	4	2	451
1.681E-02	1.970E-01	1088	4	2	452
0.0	1.13E+06	1088	4	2	453
3.635E-02	1.952E-01	1088	4	2	454
0.0	1.15E+06	1088	4	2	455
4.831E-02	1.941E-01	1088	4	2	456
0.0	1.17E+06	1088	4	2	457
5.970E-02	1.929E-01	1088	4	2	458
0.0	1.20E+06	1088	4	2	459
7.677E-02	1.910E-01	1088	4	2	460
0.0	1.25E+06	1088	4	2	461
1.026E-01	1.873E-01	1088	4	2	462
0.0	1.30E+06	1088	4	2	463
1.244E-01	1.837E-01	1088	4	2	464
0.0	1.35E+06	1088	4	2	465
1.445E-01	1.800E-01	1088	4	2	466
0.0	1.40E+06	1088	4	2	467
1.629E-01	1.760E-01	1088	4	2	468
0.0	1.45E+06	1088	4	2	469
1.783E-01	1.723E-01	1088	4	2	470
0.0	1.50E+06	1088	4	2	471
1.919E-01	1.687E-01	1088	4	2	472
0.0	1.60E+06	1088	4	2	473
2.179E-01	1.608E-01	1088	4	2	474
0.0	1.70E+06	1088	4	2	475
2.372E-01	1.538E-01	1088	4	2	476
0.0	1.80E+06	1088	4	2	477
2.528E-01	1.474E-01	1088	4	2	478
0.0	1.90E+06	1088	4	2	479
2.649E-01	1.419E-01	1088	4	2	480
0.0	2.00E+06	1088	4	2	481
2.745E-01	1.357E-01	1088	4	2	482
0.0	2.10E+06	1088	4	2	483
2.821E-01	1.314E-01	1088	4	2	484
0.0	2.20E+06	1088	4	2	485
2.888E-01	1.272E-01	1088	4	2	486
0.0	2.30E+06	1088	4	2	487
2.944E-01	1.239E-01	1088	4	2	488
0.0	2.40E+06	1088	4	2	489
2.989E-01	1.213E-01	1088	4	2	490
0.0	2.50E+06	1088	4	2	491
3.028E-01	1.195E-01	1088	4	2	492
0.0	2.60E+06	1088	4	2	493
3.058E-01	1.180E-01	1088	4	2	494
0.0	2.70E+06	1088	4	2	495
3.084E-01	1.171E-01	1088	4	2	496

0.0	2.80E+06	0	0	4	01088	4	2	497
3.113E-01	1.165E-01	-4.240E-04	4.000E-06	4	1088	4	2	498
0.0	2.90E+06	0	0	4	01088	4	2	499
3.137E-01	1.166E-01	-4.440E-04	5.000E-06	4	1088	4	2	500
0.0	3.00E+06	0	0	4	01088	4	2	501
3.157E-01	1.173E-01	-4.680E-04	5.000E-06	4	1088	4	2	502
0.0	3.20E+06	0	0	4	01088	4	2	503
3.216E-01	1.186E-01	-4.810E-04	7.000E-06	4	1088	4	2	504
0.0	3.40E+06	0	0	4	01088	4	2	505
3.271E-01	1.210E-01	-5.350E-04	9.000E-06	4	1088	4	2	506
0.0	3.60E+06	0	0	4	01088	4	2	507
3.321E-01	1.252E-01	-5.480E-04	1.200E-05	4	1088	4	2	508
0.0	3.80E+06	0	0	4	01088	4	2	509
3.367E-01	1.312E-01	-5.400E-04	1.400E-05	4	1088	4	2	510
0.0	4.00E+06	0	0	4	01088	4	2	511
3.418E-01	1.381E-01	-5.780E-04	1.700E-05	4	1088	4	2	512
0.0	4.20E+06	0	0	4	01088	4	2	513
3.476E-01	1.438E-01	-5.920E-04	2.200E-05	4	1088	4	2	514
0.0	4.40E+06	0	0	4	01088	4	2	515
3.537E-01	1.495E-01	-6.160E-04	2.600E-05	4	1088	4	2	516
0.0	4.60E+06	0	0	4	01088	4	2	517
3.596E-01	1.552E-01	-6.410E-04	3.000E-05	4	1088	4	2	518
0.0	4.80E+06	0	0	4	01088	4	2	519
3.654E-01	1.604E-01	-6.740E-04	3.600E-05	4	1088	4	2	520
0.0	5.00E+06	0	0	4	01088	4	2	521
3.713E-01	1.658E-01	-6.910E-04	4.100E-05	4	1088	4	2	522
0.0	5.20E+06	0	0	4	01088	4	2	523
3.770E-01	1.707E-01	-7.030E-04	4.700E-05	4	1088	4	2	524
0.0	5.40E+06	0	0	4	01088	4	2	525
3.821E-01	1.753E-01	-7.400E-04	5.500E-05	4	1088	4	2	526
0.0	5.60E+06	0	0	4	01088	4	2	527
3.870E-01	1.800E-01	-7.320E-04	6.300E-05	4	1088	4	2	528
0.0	5.80E+06	0	0	4	01088	4	2	529
3.916E-01	1.844E-01	-7.660E-04	7.200E-05	4	1088	4	2	530
0.0	6.00E+06	0	0	4	01088	4	2	531
3.966E-01	1.884E-01	-8.190E-04	8.400E-05	4	1088	4	2	532
0.0	6.20E+06	0	0	4	01088	4	2	533
4.009E-01	1.922E-01	-8.170E-04	9.200E-05	4	1088	4	2	534
0.0	6.40E+06	0	0	4	01088	4	2	535
4.049E-01	1.953E-01	-8.200E-04	1.050E-04	4	1088	4	2	536
0.0	6.60E+06	0	0	4	01088	4	2	537
4.092E-01	1.984E-01	-8.480E-04	1.180E-04	4	1088	4	2	538
0.0	6.80E+06	0	0	4	01088	4	2	539
4.130E-01	2.011E-01	-8.700E-04	1.330E-04	4	1088	4	2	540
0.0	7.00E+06	0	0	4	01088	4	2	541
4.168E-01	2.039E-01	-8.630E-04	1.470E-04	4	1088	4	2	542
0.0	7.20E+06	0	0	4	01088	4	2	543
4.198E-01	2.062E-01	-8.140E-04	1.610E-04	4	1088	4	2	544
0.0	7.40E+06	0	0	4	01088	4	2	545
4.231E-01	2.083E-01	-7.800E-04	1.790E-04	4	1088	4	2	546
0.0	7.60E+06	0	0	4	01088	4	2	547
4.260E-01	2.106E-01	-7.500E-04	1.950E-04	4	1088	4	2	548
0.0	7.80E+06	0	0	4	01088	4	2	549
4.291E-01	2.124E-01	-6.990E-04	2.140E-04	4	1088	4	2	550
0.0	8.00E+06	0	0	4	01088	4	2	551
4.316E-01	2.140E-01	-6.410E-04	2.390E-04	4	1088	4	2	552
0.0	8.20E+06	0	0	4	01088	4	2	553
4.342E-01	2.159E-01	-5.640E-04	2.650E-04	4	1088	4	2	554
0.0	8.40E+06	0	0	4	01088	4	2	555
4.362E-01	2.175E-01	-4.670E-04	2.900E-04	4	1088	4	2	556
0.0	8.60E+06	0	0	4	01088	4	2	557
4.384E-01	2.189E-01	-3.500E-04	3.180E-04	4	1088	4	2	558

0.0	8.80E+06	0	0	4	01088	4	2	559
4.403E-01	2.202E-01	-2.490E-04	3.480E-04		1088	4	2	560
0.0	9.00E+06	0	0	4	01088	4	2	561
4.424E-01	2.216E-01	-1.320E-04	3.800E-04		1088	4	2	562
0.0	9.20E+06	0	0	4	01088	4	2	563
4.445E-01	2.223E-01	-1.200E-05	4.110E-04		1088	4	2	564
0.0	9.40E+06	0	0	4	01088	4	2	565
4.463E-01	2.234E-01	1.110E-04	4.480E-04		1088	4	2	566
0.0	9.60E+06	0	0	4	01088	4	2	567
4.482E-01	2.245E-01	2.700E-04	4.840E-04		1088	4	2	568
0.0	9.80E+06	0	0	4	01088	4	2	569
4.498E-01	2.254E-01	4.340E-04	5.220E-04		1088	4	2	570
0.0	1.00E+07	0	0	4	01088	4	2	571
4.517E-01	2.265E-01	6.160E-04	5.600E-04		1088	4	2	572
0.0	1.05E+07	0	0	4	01088	4	2	573
4.553E-01	2.287E-01	1.128E-03	6.820E-04		1088	4	2	574
0.0	1.10E+07	0	0	4	01088	4	2	575
4.589E-01	2.310E-01	1.609E-03	7.830E-04		1088	4	2	576
0.0	1.15E+07	0	0	4	01088	4	2	577
4.621E-01	2.326E-01	2.313E-03	9.250E-04		1088	4	2	578
0.0	1.20E+07	0	0	4	01088	4	2	579
4.651E-01	2.340E-01	3.169E-03	1.083E-03		1088	4	2	580
0.0	1.25E+07	0	0	4	01088	4	2	581
4.674E-01	2.351E-01	4.082E-03	1.231E-03		1088	4	2	582
0.0	1.30E+07	0	0	4	01088	4	2	583
4.701E-01	2.362E-01	5.001E-03	1.429E-03		1088	4	2	584
0.0	1.35E+07	0	0	4	01088	4	2	585
4.725E-01	2.374E-01	6.139E-03	1.600E-03		1088	4	2	586
0.0	1.40E+07	0	0	4	01088	4	2	587
4.750E-01	2.388E-01	7.284E-03	1.781E-03		1088	4	2	588
0.0	1.45E+07	0	0	4	01088	4	2	589
4.775E-01	2.402E-01	8.515E-03	1.971E-03		1088	4	2	590
0.0	1.50E+07	0	0	4	01088	4	2	591
4.801E-01	2.418E-01	9.809E-03	2.171E-03		1088	4	2	592
0.0	0.0	0	0	0	01088	4	0	593
0.0	0.0	0	0	0	01088	0	0	594
2000.0	3.96822	0	0	0	01088	7	4	595
0.0	0.0	0	0	12	11088	7	4	596
0.0	59.3	3.96822	1.5	0.0	0.01088	7	4	597
1.0	0.7238	3.96822	0.0	0.0	0.01088	7	4	598
0.0	0.0	0	0	0	01088	7	0	599
0.0	0.0	0	0	0	01088	0	0	600
0.0	0.0	0	0	0	0	0	0	601

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